

# Model Initialization in a Tidally Energetic Regime: a Dynamically Adjusted Objective Analysis

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## Abstract

A simple improvement to objective analysis of hydrographic data is proposed to eliminate spatial aliasing effects in tidally energetic regions. The proposed method consists of the evaluation of anomalies from observations with respect to circulation model fields. The procedure is run iteratively to achieve convergence. The method is applied in the Bay of Fundy and compared with traditional objective analysis procedures and dynamically adjusted climatological fields. The hydrographic skill (difference between observed and model temperature and salinity) of the dynamically adjusted objective analysis is significantly improved by reducing bias and correcting the vertical structure. Representation of the observed velocities is also improved. The resulting flow is consistent with the known circulation in the Bay.

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## 1. Introduction

Initialization of ocean circulation models remains a challenge for both coastal and large-scale ocean simulations. Several approaches have been used in the past to improve the skill of initialization products: using climatological hydrographic fields (Ezer and Mellor, 1994; Danabasoglu et al., 1996), nudging temperature and salinity observations into model solutions (Malanotte-Rizzoli and Holland, 1986), using objective analysis of observations to generate updated fields (Robinson et al., 1989, 1996), developing various types of inverse methods as Kalman Filters (Fukumori et al., 1993;

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10 Ballabrera-Poy et al., 2001) and adjoint methods (Marotzke and Wunsch,  
11 1993; Kleeman et al., 1995). The appropriateness of each method depends  
12 on the associated goals and available resources. The use of climatological ini-  
13 tialization could require long integrations (even thousands of years) so that  
14 model dynamics and exterior forcings drive model solutions toward equilib-  
15 rium (McWilliams, 1996). The climatological approach is usually preferred in  
16 large scale ocean studies that require long spin-ups. Although climatological  
17 fields can be useful for general and process studies, more realistic initial con-  
18 ditions are necessary for event and hindcast/forecast studies. The simplest  
19 approach is to embed observations into the model mass field using nudging.  
20 A more elaborate approach is to calculate anomalies between observations  
21 and climatological background fields and objectively analyze those anoma-  
22 lies. Finally, a more computationally expensive approach is to produce initial  
23 conditions with adjoint methods or ensemble smoother simulations.

24 Herein we describe an improvement of the traditional objective analysis  
25 technique to include dynamical effects. Instead of calculating the anoma-  
26 lies (departures of the observations from a reference field) with respect to  
27 a climatological background, we compute the anomaly as the difference be-  
28 tween observations and the model solution at the time of the observation.  
29 Applications of this dynamically adjusted objective analysis have been used  
30 in atmospheric (Goerss and Phoebus, 1993; Lorenc et al., 2000) and oceanog-  
31 raphic applications (Carton et al., 2000b; Stammer et al., 2000). In the  
32 current study an iterative approach is used to improve skill and computa-  
33 tional performance. The method is applied in the Gulf of Maine/Bay of  
34 Fundy Region (Figure 1).

35 The Gulf of Maine and Bay of Fundy have been intensely studied for  
36 decades using observations and model simulations. Buoyancy-driven flows,  
37 winds, and tides control the circulation of the Gulf and the adjacent Bay  
38 (Bigelow, 1927; Brooks, 1985; Brooks and Townsend, 1989). The main char-  
39 acteristic of the Bay is the presence of some of the world’s largest tides,  
40 especially the  $M_2$  tidal constituent, with tidal ranges of up to 8 meters at  
41 the mouth and 16 meters at the head of the Bay (Garrett, 1972; Greenberg,  
42 1983). Tidal rectification dominates the resulting residual circulation with  
43 flow into the Bay along the Nova Scotia shelf and outflow along the coast of  
44 New Brunswick and Grand Manan Island (Bigelow, 1927; Greenberg, 1983).  
45 The presence of cyclonic circulation near the mouth of the Bay, caused by  
46 the combination of tidal rectification and a dense water pool in the center  
47 of the Grand Manan basin, forms a persistent gyre with significant impli-

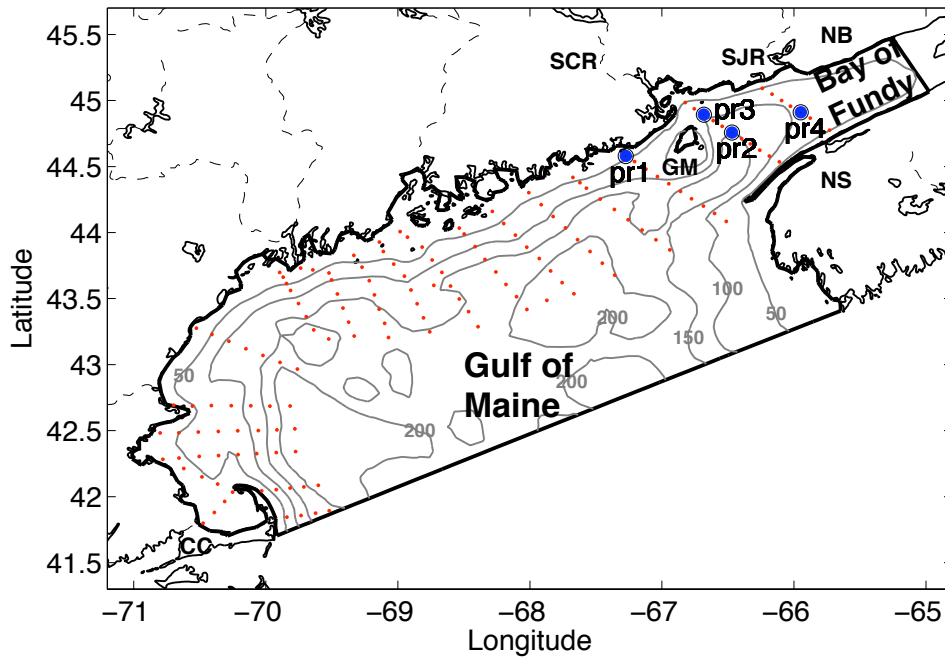


Figure 1: Map of the study region showing the model domain of the Gulf of Maine and Bay of Fundy. Small red dots indicate the horizontal position of the temperature and salinity observations. The blue dots indicate the positions of selected representative observations. The two main rivers near the Bay of Fundy are indicated with thin dashed lines: St. Croix (SCR) and St. John (SJR). The bottom topography contours of 50, 100, 150, and 200 meters are indicated. (GM - Grand Manan Island; NS - Nova Scotia; NB - New Brunswick; CC - Cape Cod).

48 cations for the physics and biology of the region (Aretxabaleta et al., 2008,  
49 2009). Additionally, the seasonally varying river discharge from the St. John  
50 River (Brooks, 1994; Bisagni et al., 1996) influences the near-surface hydro-  
51 graphic structure in the western and southern Bay. In this study we focus  
52 in the June 2006 period for which observations were available from cruises  
53 and moorings. Aretxabaleta et al. (2009) described a relatively strong Bay  
54 of Fundy gyre during June 2006 due to the presence of denser water near the  
55 bottom (compared with previous years and climatological densities).

56 In such an energetic regime as the Bay of Fundy with tidal excursions  
57 on the order of 15-25 km, hydrographic stations conducted during cruise  
58 surveys (usually lasting longer than a week) are subject to large tidal aliasing.  
59 The density gradients estimated from the observations introduce significant  
60 misrepresentations of actual density gradients, for instance when one transect  
61 is measured during ebb tide while the following one is conducted during flood  
62 tide. Here we introduce a method for dynamically adjusted objective analysis  
63 that significantly improves the skill of initialization products in regimes with  
64 large tidal excursions or in the proximity of frontal regions.

## 65 2. Data

66 150 hydrographic stations, as well as along-track ADCP velocity observa-  
67 tions, were collected during June 2006, *R/V Oceanus* cruise OC425 (June 6-  
68 17, 2006) in the Gulf of Maine and Bay of Fundy (Figure 1). The observations  
69 extended from near the coast to the 200-meter isobath. In the current study,  
70 we focus on two transects conducted inside the Bay of Fundy (one in the  
71 central Bay, *T3*, and one near the mouth, *T2*) and another one just outside  
72 of the Bay, *T1* (Figure 2).

73 The observed depth-averaged velocity obtained from the ADCP (Fig-  
74 ure 2) has peak values of  $0.8 \text{ ms}^{-1}$  over the deeper part of the basin and  
75  $1.5 \text{ ms}^{-1}$  over the shallow flanks of the western central Bay. The three-  
76 dimensional structure of the velocity is complex, with large vertical shear in  
77 the bottom and surface boundary layers and small shear in the mid-water  
78 column due to the action of the strong tide. In Figure 2, depth-averaged  
79 velocity is used as an indication of tidal phase and horizontal shear in veloc-  
80 ity. The observed velocities show the data collection inside the Bay included  
81 both phases of the tide, with the transect in the central Bay (*T3*) sampled  
82 predominantly during ebb and the transect nearest the mouth (*T2*) occurring  
83 during flood. The data were collected during peak spring tides.

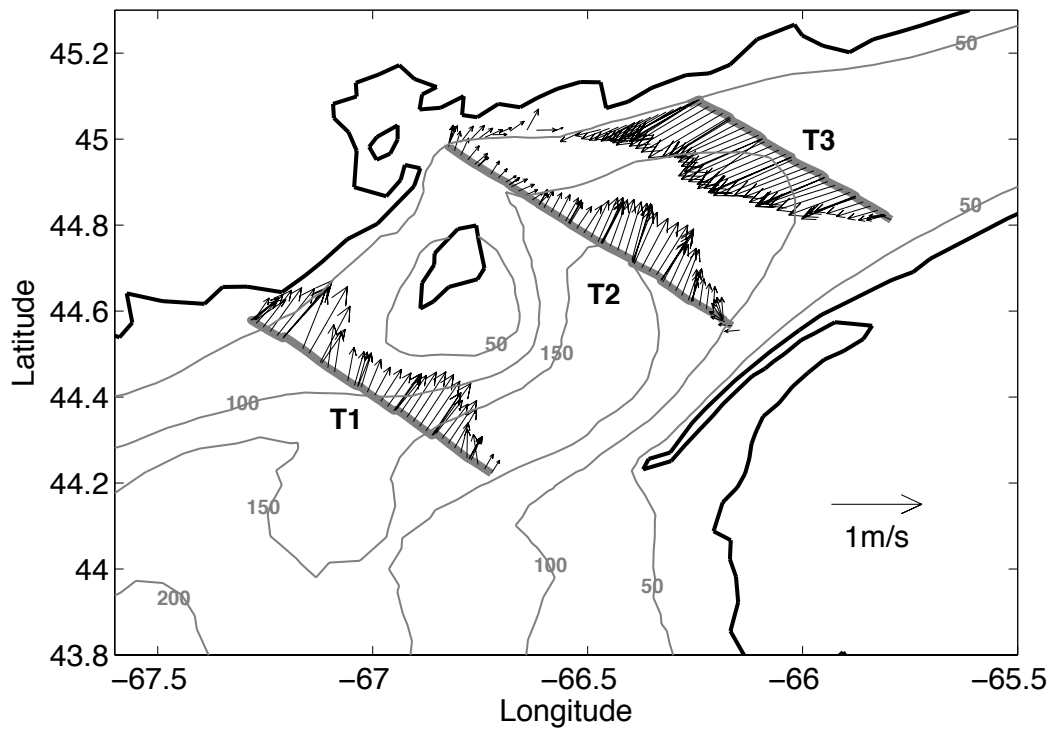


Figure 2: Observed (ADCP) depth-averaged velocity in the proximity of the Bay of Fundy. The three transects conducted in (or in the proximity of) the Bay have been labeled: **(T1)**, just outside the Bay in the northwestern Gulf of Maine; **(T2)**, near the mouth of the Bay; and **(T3)**, across the central Bay. Bottom topography contours of 50, 100, 150, and 200 meters are indicated.

84 The reference temperature and salinity used as background conditions  
 85 are specified from the Gulf of Maine climatology described in Lynch et al.  
 86 (1996). These climatological fields have been successfully used in several  
 87 previous studies of the Gulf of Maine and Bay of Fundy circulation (Lynch  
 88 et al., 1997; He et al., 2005; Aretxabaleta et al., 2008).

### 89 3. Estimating initial model hydrography

#### 90 3.1. General theory

91 Following the notation by Ide et al. (1997), consider a 3D primitive equa-  
 92 tion model  $M(\mathbf{x}, \gamma)$ , where in this case  $\mathbf{x} = (S, T)$  is the (column) vector  
 93 representing hydrography and  $\gamma$  are the remaining parameters of the model.  
 94 The initial hydrography is  $\mathbf{x}_0 = [S_0, T_0]$ , where  $T_0$  is the initial tempera-  
 95 ture field and  $S_0$  is the initial salinity. In this notation, the subscript 0  
 96 refers to fields at the initial time. We can introduce a penalty function,  
 97  $J = -2\log(L([S_0, T_0]|\mathbf{y}^\circ))$  (where  $L$  is the likelihood) which penalizes misfit  
 98 to the data ( $\mathbf{y}^\circ$ , observations) and departures from climatology ( $\mathbf{x}_c$ ):

$$J = (\mathbf{y}^\circ - \mathbf{H}\mathbf{M}(\mathbf{x}_0, \gamma))^T \mathbf{R}^{-1} (\mathbf{y}^\circ - \mathbf{H}\mathbf{M}(\mathbf{x}_0, \gamma)) + (\mathbf{x}_0 - \mathbf{x}_c)^T \mathbf{P}_0^{-1} (\mathbf{x}_0 - \mathbf{x}_c) \quad (1)$$

99 Here,  $\mathbf{R}$  is the observational error covariance matrix,  $H$  is the measure-  
 100 ment operator that, in our case, is assumed to be linear,  $\mathbf{P}$  is the model error  
 101 covariance matrix with  $\mathbf{P}_0$  being its value for the initial condition, and  $\mathbf{x}_c$   
 102 is the climatological estimate of  $\mathbf{x}_0$ . In the 4DVAR variational method (Ben-  
 103 nett, 1992; Wunsch, 1996) one seeks to minimize  $J$  as a function of  $\mathbf{x}_0$ . For  
 104 a general nonlinear model,  $M$ , constructing the solution that minimizes  $J$   
 105 can be challenging and computationally expensive. An alternative approach  
 106 is to assume that the optimal estimate of  $\mathbf{x}_0$  is a linear function of the mis-  
 107 fit between the model and data, leading to Gauss-Markov smoothing. Bold  
 108 characters represent linear operators, following Ide et al. (1997). It is easy  
 109 to show that minimizing  $J$  with respect to  $\mathbf{x}_0$  is solved by:

$$\hat{\mathbf{x}}_0 = \mathbf{x}_c + \mathbf{A}_0 \mathbf{P} \mathbf{H}^T (\mathbf{H} \mathbf{P} \mathbf{H}^T + \mathbf{R})^{-1} (\mathbf{y}^\circ - \mathbf{H} \mathbf{M}(\mathbf{x}_c, \gamma)) \quad (2)$$

110 where  $\mathbf{A}_0$  is the matrix projecting the full space-time model vector onto the  
 111 initial time point. The matrix  $\mathbf{P}$  represents the full space-time model error  
 112 covariance matrix. Typically simplifications (e.g., Monte Carlo approxima-  
 113 tions) of this matrix are made, however for a 3D primitive equation model

114 even this approach can be numerically expensive. Herein, we assume that  $\mathbf{P}_0$   
 115 corresponds to the error covariance of the climatological fields ( $\mathbf{P}_0 = \mathbf{P}_c$ ).

116 To avoid these computational burdens, time and the dynamic evolution  
 117 of  $T$  and  $S$  can be ignored, leading to the penalty function of static fields  
 118 (3DVAR):

$$J = (\mathbf{y}^o - \mathbf{H}_0 \mathbf{x}_0)^T \mathbf{R}^{-1} (\mathbf{y}^o - \mathbf{H}_0 \mathbf{x}_0) + (\mathbf{x}_0 - \mathbf{x}_c)^T \mathbf{P}_0^{-1} (\mathbf{x}_0 - \mathbf{x}_c) \quad (3)$$

119 Here  $\mathbf{H}_0$  represents the measurement operator  $\mathbf{H}$  without the temporal com-  
 120 ponent. Then:

$$\hat{\mathbf{x}}_0 = \mathbf{x}_c + \mathbf{P}_0 \mathbf{H}_0^T (\mathbf{H}_0 \mathbf{P}_0 \mathbf{H}_0^T + \mathbf{R})^{-1} (\mathbf{y}^o - \mathbf{H}_0 \mathbf{x}_c) \quad (4)$$

### 121 3.2. Objective analysis

122 In this study, we refer to Objective Analysis (OA) as the particular form of  
 123 statistical interpolation also commonly referred to as Optimal Interpolation  
 124 (Lorenc, 1981, 1986). The OA method requires the specification of the two  
 125 covariance functions ( $\mathbf{R}$  and  $\mathbf{P}_0$ ) to compute the vector of optimal linear  
 126 weights,  $\lambda^j$ , for the interpolation to node  $j$ :

$$\hat{\mathbf{x}}^j = \mathbf{x}^j + \lambda^j \cdot (\mathbf{y}^o - \mathbf{H}_0 \mathbf{x}). \quad (5)$$

127 where

$$\lambda^j = \mathbf{P}_0^j \mathbf{H}_0^T (\mathbf{H}_0 \mathbf{P}_0 \mathbf{H}_0^T + \mathbf{R})^{-1} \quad (6)$$

128 In OA, the model error covariance,  $\mathbf{P}_0$ , is usually further simplified (Ghil and  
 129 Malanotte-Rizzoli, 1991; Ide et al., 1997) by an approximate error covariance,  
 130  $\mathbf{B}$ , that includes the variances (empirical) in a diagonal matrix,  $\mathbf{D}$ , and the  
 131 time-independent correlations,  $\mathbf{C}$ .

$$\mathbf{B} = \mathbf{D}^{1/2} \mathbf{C} \mathbf{D}^{1/2} \quad (7)$$

132 After these approximations, the resulting weights are:

$$\lambda^j = \mathbf{B}_0^j \mathbf{H}_0^T (\mathbf{H}_0 \mathbf{B}_0 \mathbf{H}_0^T + \mathbf{R})^{-1} \quad (8)$$

133 Statistical interpolation of oceanic data using objective analysis has been  
 134 extensively described in the literature (Bretherton et al., 1976; Denman and  
 135 Freeland, 1985; Wunsch, 1996). Several studies in the Gulf of Maine have  
 136 used OA to estimate hydrographic and biological fields (Lynch et al., 1996;

137 McGillicuddy et al., 1998; Lynch and McGillicuddy, 2001). A recent imple-  
 138 mentation of the OA method, called OACI (Objective Analysis for Circula-  
 139 tion Initialization, Smith (2004)) has been successfully used for model ini-  
 140 tialization (He et al., 2005; Aretxabaleta et al., 2009). The approach consists  
 141 of a simple implementation of a four-dimensional objective analysis method  
 142 (Cressie, 1993). The software interpolates the residual (data to be interpo-  
 143 lated minus background estimate of 3D field) onto any regular or irregular  
 144 grid. The algorithm allows for the two configurations described in Cressie  
 145 (1993) depending on the availability and quality of the background estimate:  
 146 1) simple kriging, assuming a zero mean; and 2) ordinary kriging, which as-  
 147 sumes an unknown mean that is estimated during the procedure. For the  
 148 rest of this study, we called this method “traditional objective analysis.”

### 149 3.3. An iterative approach

150 For the present goal of inferring initial conditions from a non-synoptic  
 151 ( $t_1 \leq t \leq t_2$ ) survey, the procedure produces one initial condition for  $t = t_0$   
 152 by assuming the observations were nearly synoptic,  $t \sim t_0$ . We partly rein-  
 153 troduce the influence of the remaining parameters of the primitive equation  
 154 model in Equation 4 by computing

$$\hat{\mathbf{x}}_0 = \mathbf{x}_c + \mathbf{P}_0 \mathbf{H}_0^T (\mathbf{H}_0 \mathbf{P}_0 \mathbf{H}_0^T + \mathbf{R})^{-1} (\mathbf{y}^o - \mathbf{H}M(\mathbf{x}_c, \gamma)) \quad (9)$$

155 In this expression the model,  $M$ , remains non-linear instead of the previous  
 156 linearization used for the traditional objective analysis (Section 3.2).

157 We now can create an iterative version, where  $\mathbf{x}_0^1 = \mathbf{x}_c$ , so that the non-  
 158 linear effects of the model are reintroduced in our prediction,

$$\mathbf{x}_0^{j+1} = \mathbf{x}_0^j + \mathbf{P}_0 \mathbf{H}_0^T (\mathbf{H}_0 \mathbf{P}_0 \mathbf{H}_0^T + \mathbf{R})^{-1} (\mathbf{y}^o - \mathbf{H}M(\mathbf{x}_0^j, \gamma)) \quad (10)$$

159  $\mathbf{P}_0$  remains constant through the iterations of the method. In general the  
 160 model covariance matrix could present small deviations from the background  
 161 (initial) model covariance, but in our method the assumption is the deviations  
 162 are negligible.

163 The iterative OA approach can be simplified to a traditional OA com-  
 164 ponent and a non-linear dynamic component. Our iterative dynamic OA  
 165 method (Figure 3) consists of five steps: 1) a circulation simulation initialized  
 166 with climatological fields (same as prior simulation to be described in Sec-  
 167 tion 3.4); 2) computation of the anomalies between observations and model  
 168 fields; 3) objective analysis of the anomalies (using OACI, Smith (2004));



169 4) adjustment of the initial conditions of the model with the objectively  
170 analyzed anomalies; 5) a circulation simulation using the updated initial  
171 conditions. Steps 2-5 are iterated to achieve convergence. In the application  
172 described herein, three iterations were sufficient to achieve convergence (less  
173 than 5% change between successive anomaly estimates). A similar approach  
174 without the iterative part has been previously described by Carton et al.  
175 (2000a) and Bennett (2002).

### 176 3.4. Oceanographic model

177 The primitive equation model “Quoddy” (Lynch and Werner, 1991) used  
178 herein has been extensively applied to the study of coastal circulation in the  
179 Gulf of Maine and adjacent areas (Lynch et al., 1996, 2001; Naimie, 1996; He  
180 et al., 2005). Quoddy is a three-dimensional, fully nonlinear, prognostic, tide-  
181 resolving, finite element model. To demonstrate the new analysis method, we  
182 apply it to a domain that includes most of the Gulf of Maine from Cape Cod  
183 to southwestern Nova Scotia and north up to the Bay of Fundy (Figure 1).  
184 We focus our evaluation in the proximity of the Bay where tidal effects are  
185 especially strong. The finite element mesh includes fine horizontal resolution  
186 of 2-3 km near the coast increasing to around 8 km in the deep basins of the  
187 Gulf of Maine. Tidal forcing is included for five tidal constituents ( $M_2, S_2,$   
188  $N_2, O_1,$  and  $K_1$ ) using best estimates of the tidal boundary conditions (ele-  
189 vations and velocities) from climatological simulations (Lynch et al., 1996).  
190 Boundary conditions for temperature, salinity and residual elevation are also  
191 initialized from climatology (Lynch et al., 1996) but are updated to avoid  
192 inconsistencies at the boundary by using the interior values during times of  
193 outflow through the edge. Hourly wind stress from National Data Buoy Cen-  
194 ter (NDBC) station 44027 (Jonesport, ME) is enforced as surface boundary  
195 condition. Heat flux estimates are extracted from the NCEP/NCAR Re-  
196 analysis (Kalnay et al., 1996), while river discharge is obtained from U.S.  
197 Geological Survey and Water Survey of Canada stream gauge stations. The  
198 circulation model is run for the duration of a cruise period during June 2006  
199 plus an additional four days prior to the cruise to provide some spin-up time  
200 for initial and boundary conditions.

201 We refer to the first run of the circulation model (CIPR, initialized with  
202 climatology) as the “prior”, which does not include objective analysis for  
203 generation of initial condition. The final circulation simulation, after conver-  
204 gence is achieved through several OA/model iterations, is called the “poste-  
205 rior” circulation (CIPO). It is important to distinguish between the posterior

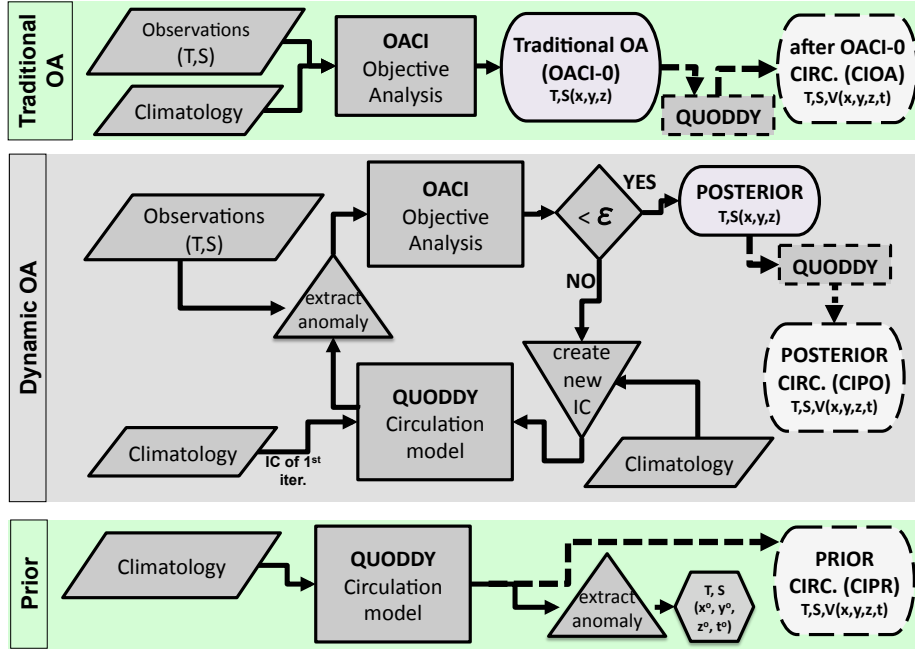


Figure 3: Schematic diagram of the procedure followed. The top box corresponds to the traditional OA approach, which produces 3D (for all positions,  $x, y, z$ ) hydrographic initialization fields (OACI-0) and, after going through the circulation model, results in 4D (all positions and times in the simulation,  $x, y, z, t$ ) flow called CIOA. The bottom box represents the single pass through the circulation model initialized from climatology, that results in the prior 4D ( $x, y, z, t$ ) flow (CIPR) and the anomaly extracted at the location of the observations (only for  $x^o, y^o, z^o, t^o$ ). The central box corresponds to the iterative dynamical objective analysis. A decision is made to terminate the iterations when the global change in the hydrographic 3D field between successive iterations is less than a threshold ( $\epsilon = 0.05$ ). If the threshold is not satisfied, a new set of initial conditions is generated that combine the climatology with the new 3D hydrographic fields. When the threshold is satisfied, a final pass through the circulation model produces the 4D flow field (CIPO). Dashed lines represent additional circulation model simulations and their output.

206 hydrographic initial condition, valid for all discretized spatial locations at  
207  $t = t_0$ , and the posterior circulation, valid for all discretized spatial locations  
208 and times.

## 209 4. Results and Discussion

210 Five estimates of the hydrographic conditions during June 2006 can be  
211 constructed (Table 1) and their skill evaluated by comparison with observa-  
212 tions:

- 213 • Climatological fields: assuming that the conditions during June 2006  
214 matched the long-term mean.
- 215 • Traditional objective analysis (OACI-0): assuming the circulation can  
216 be neglected in the computation, i.e., all the observations during June  
217 2006 are synoptic.
- 218 • Prior simulation: assuming the circulation model evolution of the cli-  
219 matological fields on short time scales can result in an appropriate  
220 representation of the real hydrographic structure (no assimilation of  
221 observations). Therefore it is equivalent to a hypothesis that the de-  
222 partures from climatology can be simulated by using realistic forcing  
223 on short time scales. This solution provides estimates of the field valid  
224 at the observation locations and times ( $T, S(x^o, y^o, z^o, t^o)$ ), but not an  
225 initialization field (for  $T, S(x, y, z)$  at  $t = t_0$ ).
- 226 • First iteration analysis: projecting the observations into the anomalies  
227 calculated from the prior model simulation instead of the climatological  
228 fields.
- 229 • Posterior analysis: using the iterative dynamically adjusted objective  
230 analysis to provide an updated initial condition while considering the  
231 effects of circulation.

### 232 4.1. Model-data Comparison

233 In this section an evaluation of the quality of the procedure is conducted  
234 by extracting, from the global 3D estimates, several subsampled fields: 1)  
235 surface temperature (SST); 2) vertical T and S profiles at specific locations;  
236 and 3) a vertical transect across the mouth of the Bay.

	Background	Observations	Circulation effects
Climatological	Climatology	Not included	NO
Traditional OA	Climatology	Included	NO
Prior analysis	Climatology	Not included	YES
1 <sup>st</sup> Iter. analysis	Model prior	Included	YES
Posterior analysis	Model penult.	Included	YES

Table 1: Characteristics of the different hydrographic fields.

237 We extract the SST from the full 3D analysis to understand whether  
238 the method is able to recover the observed horizontal spatial structure. The  
239 observed SST (Figure 4b) is higher than climatology (Figure 4a) in the north-  
240 western Gulf of Maine and especially in the western Bay of Fundy (Root Mean  
241 Square (RMS) difference 1.7 °C). The observed SST hints at a southwest to  
242 northeast temperature gradient with higher values north of Grand Manan Is-  
243 land. The traditional objective analysis results in local corrections off Nova  
244 Scotia that are larger than necessary (Figure 4c) but still reduces the differ-  
245 ence with observations (RMS difference 0.9 °C). The surface temperature of  
246 the prior circulation solution (Figure 4d) is a slight dynamical modification  
247 of the climatological field (RMS, 1.8 °C). The resulting changes introduced  
248 by the first iteration of the dynamic objective analysis (Figure 4e) are more  
249 consistent with the observed values and produce a significant decrease in  
250 RMS difference (0.7 °C). In this case, the central part of the Bay near the  
251 gyre is modified too severely (due to large near-surface anomalies), resulting  
252 in higher than observed temperatures, that are resolved by the method in  
253 the following iteration. Surface temperature after the final iteration of the  
254 dynamical analysis (Figure 4f) shows values (RMS 0.4 °C) and structures  
255 (reproduction of the large scale gradients) consistent with observations.

256 Modifications introduced by the dynamically adjusted objective analysis  
257 are more evident in the comparison of the changes of selected profiles (loca-  
258 tions indicated in Figure 1) between climatological background, observations,  
259 and dynamical estimates (Figure 5). Each profile location represents a differ-  
260 ent dynamical regime within the Bay: profile 1 is outside the Bay and under  
261 the direct influence of the St. Croix river plume; profile 2 is in the center of  
262 the Bay of Fundy gyre (Aretxabaleta et al., 2009); profile 3 is directly affected  
263 by the St. John river plume; and profile 4 is near the axis of the Bay, out-  
264 side the edge of the gyre. The climatological vertical temperature structure  
265 differs significantly (except for profile 2) from observations throughout the

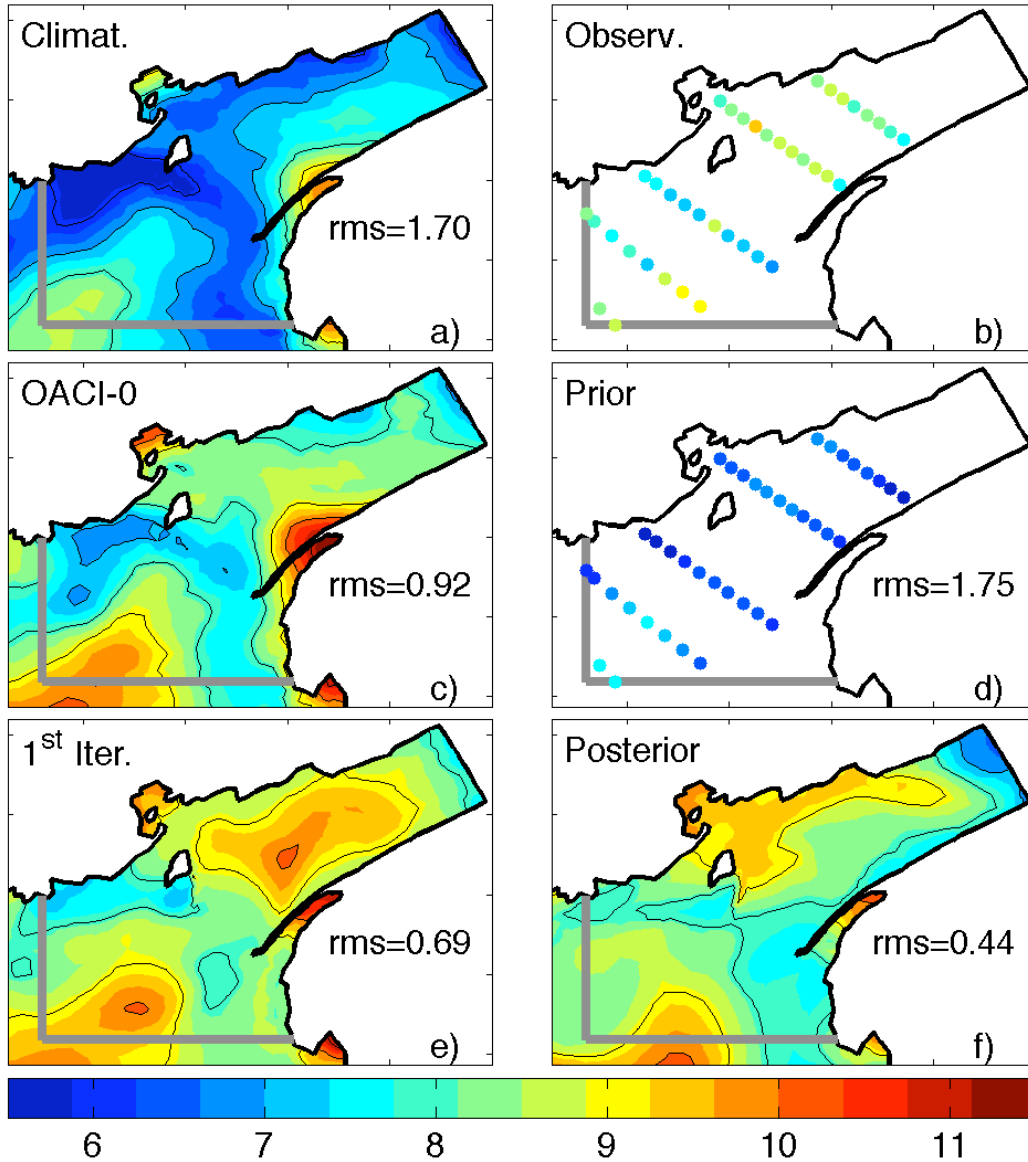


Figure 4: Surface temperature ( $^{\circ}\text{C}$ ) estimates for different procedures and rms difference with observations. (a) Climatological, (b) observations, (c) simulation with no circulation adjustments (OACI-0), (d) prior estimate (one run of the circulation model), (e) field estimate after OA of observations into prior field (1<sup>st</sup> iteration), (f) posterior estimate (after the final iteration through the model procedure). The rms difference with observations inside the region indicated by the gray line is shown for each panel.

266 entire water column, with climatology being 1 – 2 °C colder in profiles 1, 3  
267 and 4. The apparently parallel posterior and climatology temperature pro-  
268 files for stations 3 and 4 present in fact differences ranging 0.8 – 1.5 °C.  
269 Meanwhile, the climatological salinity in these three profiles is 0.5 – 1 saltier  
270 than the observations. The observed hydrographic characteristics of profile 2  
271 (Figure 5d,e,f) are closer to climatological values, especially for temperature.

272 The T/S diagrams (Figure 5a,d,g,j) demonstrate the ability of the method  
273 to reproduce the characteristics of the observations. The density differences  
274 shown by the T/S curves of the climatological and prior profiles illustrate  
275 significant inconsistencies with the observations. The posterior curves are  
276 considerably improved, and in general match the observed density varia-  
277 tions. There are instances, such as the temperature in the middle of the  
278 water column from profile 2 (Figure 5e), during which the model may have  
279 overestimated the tidal mixing resulting in reduced vertical gradients.

280 The stratification observed during June 2006 is generally stronger than  
281 the long-term average. The dynamic effect of the model alone (prior) is  
282 the reduction of the climatological stratification caused by the strong tidal  
283 mixing in the Bay. Hence, the prior temperature profiles diverge even more  
284 from observations, while the prior salinity approaches the measured struc-  
285 ture. Introduction of the dynamic objective analysis significantly improves  
286 the temperature and salinity match with observations, providing vertical  
287 stratification that is more realistic than the one present in the prior esti-  
288 mate. The corrections are larger for temperature, although corrections for  
289 salinity are significant in the areas downstream of the St. John and St. Croix  
290 river plumes (profiles 1 and 3, Figure 5c,i).

291 Accurate representations of the hydrographic conditions inside the Bay  
292 of Fundy have been shown to be critical for the simulation of the circulation  
293 (Aretxabaleta et al., 2009). The intensity of the persistent gyre near the  
294 mouth of the Bay is strongly affected by the density structure, especially the  
295 dense water pool in the basin at the entrance of the Bay. To visualize the ef-  
296 fect of the dynamic objective analysis on hydrographic structure, we examine  
297 a transect near the mouth of the Bay of Fundy (*T2*, Figure 2). The observa-  
298 tions (Figure 6b) exhibit a strong low density signal in the northwestern part  
299 of the transect resulting from the fresh water influence from the St. John  
300 river plume. High density values in the central part of the basin (50-150 m)  
301 are associated with the dense water pool. The climatological density across  
302 the mouth of the Bay is too high near the surface and too low in the lower  
303 part of the water column over the deep basin (Figure 6a) compared with

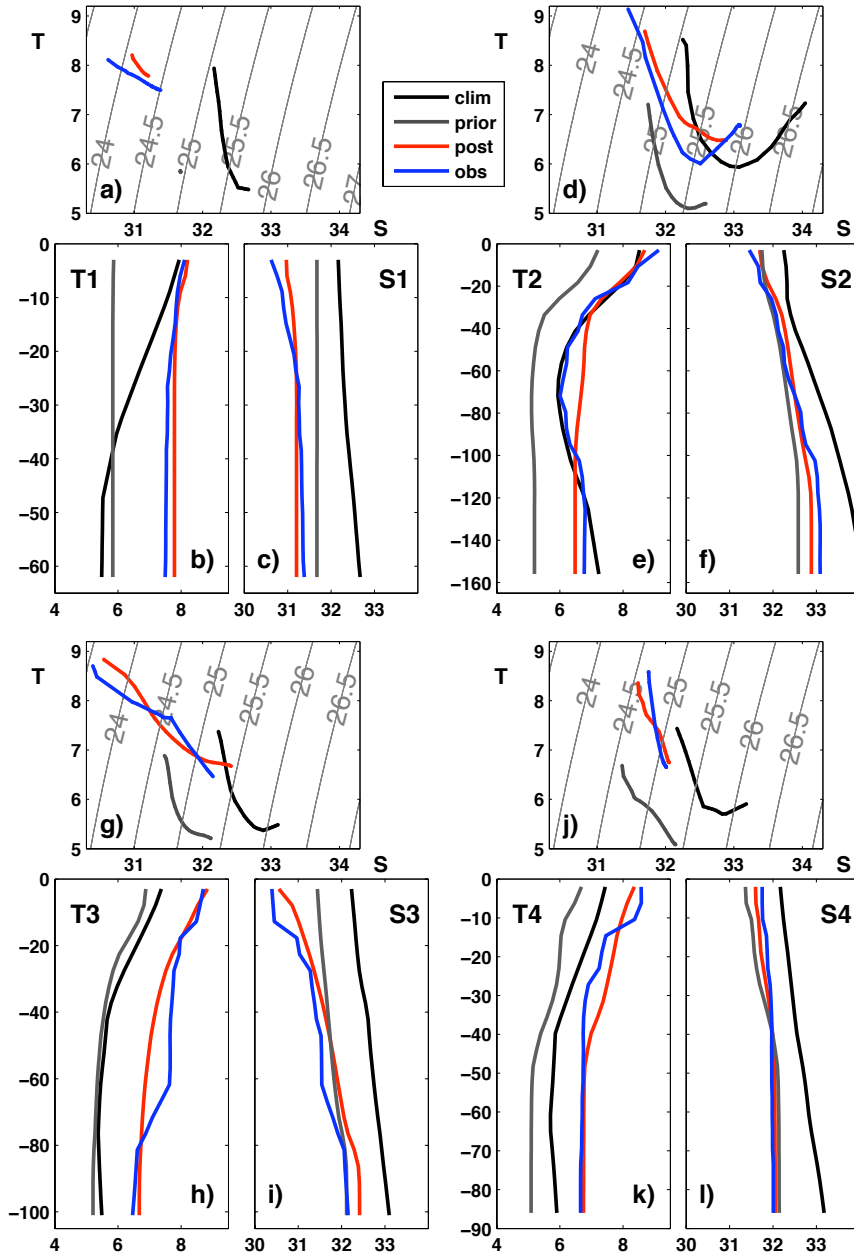


Figure 5: T/S diagrams (**a,d,g,j**), temperature (**b,e,h,k**) and salinity (**c,f,i,l**) profiles at four selected locations in or near the Bay of Fundy (profile location in Figure 1). Climatological values are represented with black lines, prior estimates with dark grey lines, posterior estimates with red and observed values with blue. Note that the prior T/S line is compressed to almost a point in panel **a**.

304 observations (Figure 6b). Traditional objective analysis of the observations  
305 (Figure 6c) results in a near-surface low density (salinity) plume with values  
306 lower than observed and an eastward displacement of the density maximum.  
307 The effect of the circulation model on the climatology (prior, Figure 6d) is an  
308 increase of near-surface density from climatological values in the western side  
309 and an erosion of the deep density maximum. The first iteration (Figure 6e)  
310 exhibits deep density values larger than observed. The near-surface effect of  
311 the St. John river plume and the increased density in the dense water pool  
312 are reproduced by the dynamical objective analysis procedure (Figure 6f),  
313 with vertical stratification similar to observations.

#### 314 *4.2. Hydrographic Skill*

315 The global (three-dimensional) skill of the method is shown using his-  
316 tograms of the departure from observations (anomaly, Figure 7), and evalu-  
317 ating bias, standard deviation, and RMS differences (Table 2). The obser-  
318 vational error specified for the OA method (approximation to the  $\mathbf{R}$  matrix)  
319 can be considered as a benchmark for the global skill. The values specified,  
320 1.0 °C for temperature and 0.25 for salinity, are taken as approximations to  
321 the standard deviation of the difference between observations and the OA  
322 method without dynamic adjustments (OACI-0).

323 The climatological temperature (Figure 7a, Table 2) has a large bias  
324 (1.5 °C) and standard deviation (1.6 °C). The traditional objective analysis  
325 (Figure 7c) slightly reduces the bias in temperature (1.4 °C) and decreases  
326 the standard deviation. The fact that the bias is only slightly modified is  
327 the result of ordinary kriging (Cressie, 1993), which assumes an unknown  
328 mean that is estimated and removed during the procedure. The effect of  
329 just the circulation (prior) on temperature (Figure 7e) is to decrease the  
330 standard deviation (0.9 °C) from the climatological initial condition while  
331 slightly increasing the bias. The first iteration of the dynamical OA method  
332 (Figure 7g) results on the removal of most of the bias in temperature while  
333 producing a significant decrease in its standard deviation. The posterior  
334 estimate of temperature resulting from the dynamical method (Figure 7i)  
335 reduces temperature bias (0.03 °C) and standard deviation (0.6 °C).

336 Climatological salinity (Figure 7b, Table 2) is negatively biased (-0.4)  
337 with respect to observations and has a high standard deviation (0.9). The  
338 traditional objectively analyzed salinity (Figure 7d) reduces the bias (-0.3)  
339 and decreases the standard deviation (0.3) by eliminating the large depart-  
340 ures from observations. The prior salinity (Figure 7f) shows a standard



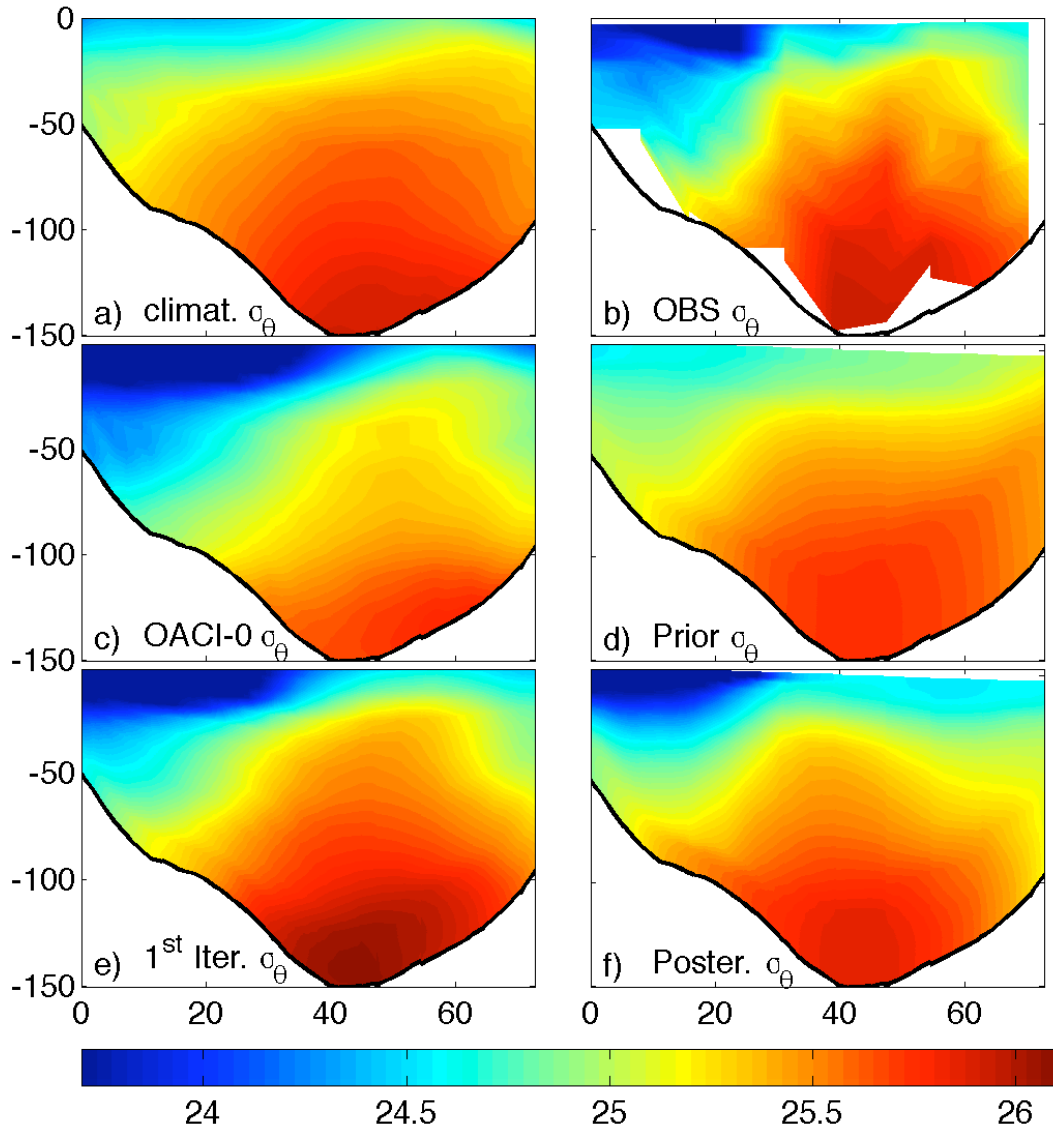


Figure 6: Density transect ( $\sigma_\theta$ ) across the mouth of the Bay of Fundy ( $T2$  in Figure 2). (a) Climatological, (b) observations, (c) traditional (OACI-0) objective analysis (no circulation) (d) prior estimate (after one pass through the circulation model, no observations), (e) first iteration of the dynamical OA (observations projected into the prior) and (f) posterior estimate (after the final pass through the dynamical analysis procedure). X-axis distance in km from the northwestern-most station in the transect (closest to New Brunswick).

341 deviation reduction from climatological values (0.5) while decreasing the size  
 342 of the bias by 60% from the climatological value. After objectively analyzing  
 343 the observations into the prior (first iteration of the dynamical system, Fig-  
 344 ure 7h) the bias is almost completely removed and the standard deviation is  
 345 reduced from the prior values. The final iteration of the dynamically objec-  
 346 tively analyzed salinity (Figure 7j) maintains low bias ( $-0.02$ ) while slightly  
 347 reducing the standard deviation (0.3), resulting in RMS differences of the  
 348 same order as the prescribed observational error.

	temperature			salinity		
	bias	std	rms	bias	std	RMS
Climat.	1.49	1.59	2.18	-0.43	0.91	1.01
OACI-0	1.44	1.11	1.82	-0.30	0.32	0.44
Prior	1.54	0.91	1.79	-0.18	0.48	0.51
1 <sup>st</sup> Iter.	0.15	0.65	0.67	-0.03	0.30	0.31
Posterior	0.03	0.56	0.56	-0.02	0.29	0.29

Table 2: Global skill statistics corresponding to the histograms in Figure 7 evaluated as the departure from observations (anomaly) for temperature and salinity. The bias, standard deviation, and RMS difference are calculated for each method and field.

### 349 4.3. Cross-validation Analysis

350 In order to determine the robustness of the solution, we conduct a set of  
 351 cross-validation experiments. We progressively remove increasing number of  
 352 stations (10% to 50% removal) at random from the analysis and repeat the  
 353 experiment 100 times for each percentage. This approach represents a partial  
 354 assimilation of the observations following a Monte Carlo approach allowing  
 355 the comparison between removed observations and posterior estimates. We  
 356 also conduct four additional experiments for which entire transects from the  
 357 vicinity of the Bay of Fundy are systematically removed. The results of the  
 358 analysis are determined with the metric given by

$$\mathbf{CV} = \frac{rms [G(p_{extr})]}{rms [G^o(p_{extr})]} \quad (11)$$

359 where  $G$  is the departure from observations of the hydrographic variables  
 360 (temperature and salinity) for the posterior estimate evaluated at the stations  
 361 removed from the analysis ( $p_{extr}$ ) and  $G^o$  is the departure of that magnitude  
 362 from the posterior analysis including all the stations evaluated at the same

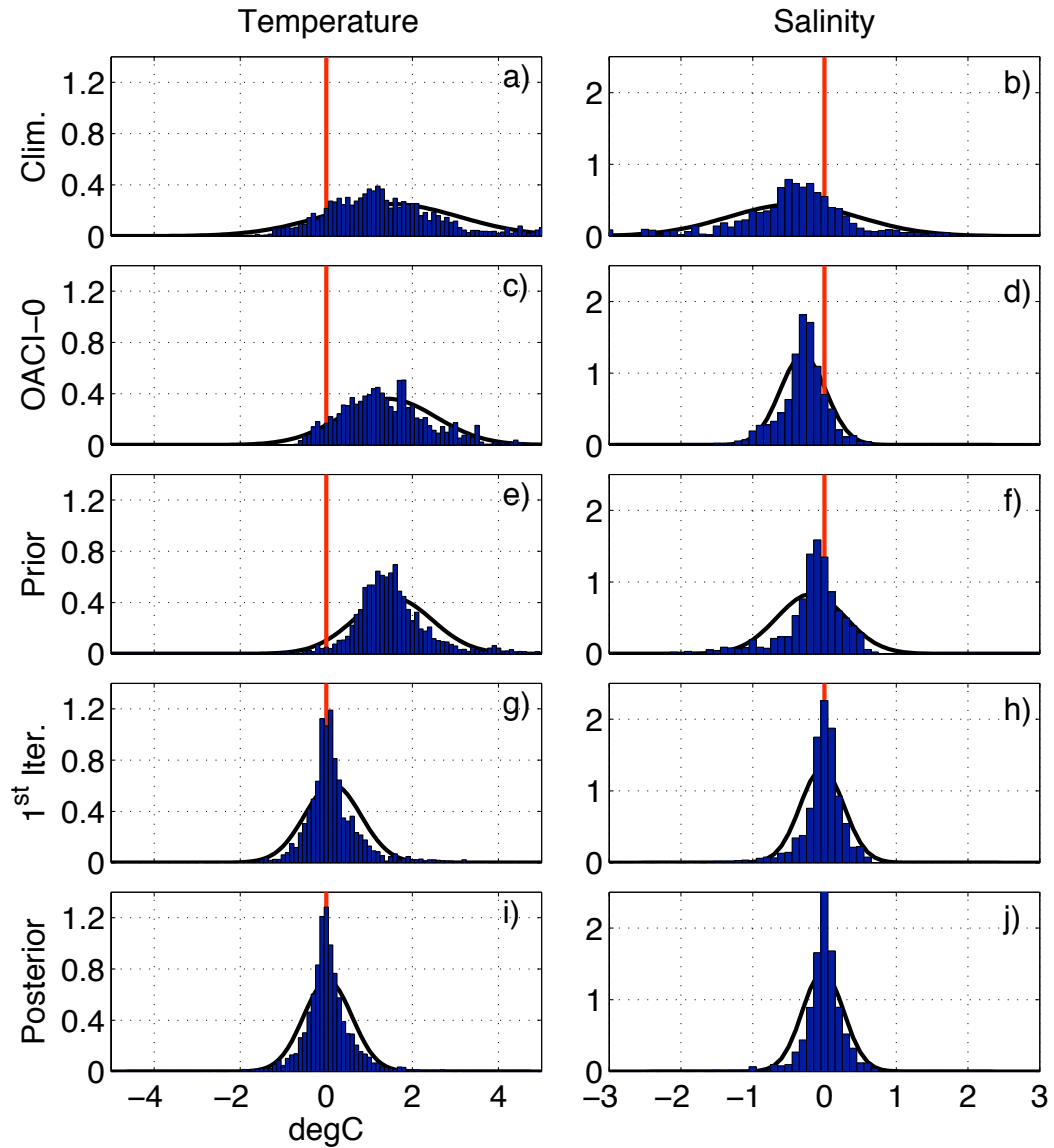


Figure 7: Global skill evaluated as the departure from observations (anomaly) for temperature (left panels) and salinity (right panels). Climatological (**a**, **b**); traditional (OACI-0) objective analysis (**c**, **d**); prior, before OA (**e**, **f**); after the first (**g**, **h**) iteration of the dynamical objective analysis; and, finally, posterior dynamical objective analysis (**i**, **j**) probability density functions are presented (blue histograms). The normal probability density function with the same mean and standard deviation is presented for reference (black curve). Statistical values for bias, standard deviation and RMS difference for these distributions are given in Table 2.

363 points ( $p_{extr}$ ). For the extreme case of including all the stations,  $CV$  would  
 364 have a value of 1.

	10%	20%	30%	40%	50%	transect	climat.	prior
T	1.12	1.17	1.23	1.28	1.44	2.06	3.52	3.03
S	1.04	1.12	1.14	1.23	1.36	2.26	3.85	2.80

Table 3: Cross-validation results: Average CV (Equation 11) for the 100 experiments for each percentage of station removal (10% to 50%). The column label transect is the average CV for the four transect removal experiments. The climatological (*prior*) CV values are calculated as the ratio between the hydrographic climatological (*prior*) values (i.e., all observations removed) and the posterior analysis including all stations.

365 The random removal of 10% of the data results in temperature and salin-  
 366 ity fields qualitatively similar to the analysis using all the stations (not  
 367 shown). The CV values (Table 3) are close to 1, which indicates that the  
 368 method is robust and that the removal of a small percentage of the data  
 369 does not deteriorate the solution significantly. Nevertheless, in some cases  
 370 the removal of 10% of data from specific critical areas (e.g., near the mouth  
 371 of the St. John river plume or near the central part of the gyre) is sufficient  
 372 to produce a significant degradation of model performance locally. The pro-  
 373 gressive removal of more stations (20-50%) increases the difference from the  
 374 original (best case) fields reaching CV values of 1.44 for temperature and 1.36  
 375 for salinity. The worst-case scenario in which all observations are removed  
 376 (climatology) results in CV values larger than 3.5. The prior analysis (with  
 377 all stations removed, no OA) produces CV values around 3. When single  
 378 transects are systematically removed, the resulting fields show a significant  
 379 worsening in CV values (larger than 2 for both T and S) even though they  
 380 only represent 20-30% of the total data available in the Bay area. Removal  
 381 of transects in the vicinity of the mouth to the Bay ( $T1$  and  $T2$  in Figure 2)  
 382 is especially damaging resulting in CV values that approach the worst-case  
 383 scenario.

#### 384 4.4. Dynamical Implications

385 The focus herein has been on estimating the quality of the best estimates  
 386 of the initialization fields based on a comparison between observed and ob-  
 387 jectively analyzed temperature and salinity. The requirements for the best  
 388 initial conditions are not only that they should match the hydrographic ob-  
 389 servations but they should also provide the best skill for the circulation. The

390 best estimate of the circulation for June 2006 comes from a hindcast (HC)  
391 study (Aretxabaleta et al., 2009) that focused on describing the characteris-  
392 tics and variability of the Bay of Fundy gyre. The June 2006 HC simulation  
393 used dynamic OA for initialization, but it differs from the simulations pre-  
394 sented in the current study because it also used assimilation of shipboard  
395 ADCP velocities as well as current meters located at GOMOOS moorings A,  
396 B, E, I, J, L, and M ([www.gomoos.org](http://www.gomoos.org)). In the HC simulation, two differ-  
397 ent inverse models for velocity assimilation were used: a frequency-domain  
398 inversion to improve the model estimate of the tidal constituents and a time-  
399 domain adjoint to provide sub-tidal adjustments. A complete validation of  
400 the HC solution is available in Aretxabaleta et al. (2009). To summarize, the  
401 HC yielded hydrographic rms skill of 0.7 °C for temperature, 0.4 for salinity  
402 and circulation skill around 0.1 m s<sup>-1</sup> for the entire Gulf of Maine domain.

403 We use the HC as a benchmark for assessing the skill of the velocity  
404 predictions derived from the dynamic OA procedure. The time- and depth-  
405 averaged residual circulation for the period of the cruise from the HC simu-  
406 lation is presented in Figure 8f.

407 The problem of comparing flows resulting from Quoddy simulations ini-  
408 tialized from the fields described herein (e.g., CIPR, CIPO) with our bench-  
409 mark HC is that Quoddy includes the effects of several factors (e.g., wind,  
410 density field, tides, river discharge, heat flux) that are not easily separated.  
411 In order to quantify the effects of the various initialization procedures on the  
412 density-driven flow, we calculated the steady-state residual circulation for  
413 each case by running a simplified circulation model (FUNDY5, Lynch and  
414 Werner (1987)). FUNDY5 is a linearized version of Quoddy in the frequency-  
415 domain that allows the separation of the different components of the circula-  
416 tion. FUNDY5 has been successfully applied in a number of coastal regimes  
417 (Lynch et al., 1992, 1996; Blanton et al., 2003; Ribergaard et al., 2004). The  
418 simplified circulation model uses the average mixing and friction from the  
419 time-domain solution to represent the effect of tidal mixing.

420 The steady-state circulation resulting from climatological density (Fig-  
421 ure 8a) is relatively weak, yet still includes a signature of the cyclonic gyre  
422 (Aretxabaleta et al., 2008). Traditional objective analysis results in unre-  
423 alistic circulation features (Figure 8b), such as an anticyclonic circulation  
424 in the Bay and a strong outflow west of Grand Manan. We believe the in-  
425 consistent circulation results from tidal aliasing and a lack of a dynamical  
426 constraint. The depth-averaged circulation associated with the dynamically  
427 evolved climatological fields (prior, Figure 8c) results in the recovery of the

428 climatological structure of the gyre and the adjacent northwestern Gulf of  
429 Maine circulation, but underestimates the strength of the gyre when com-  
430 pared with the reference hindcast simulation (Figure 8f). The circulation  
431 associated with the hydrographic fields from the first iteration of the dy-  
432 namic OA (Figure 8d) exhibits a gyre that is stronger than in the hindcast,  
433 extending farther into the Bay. The steady-state circulation response to the  
434 posterior density field (Figure 8e) exhibits similar features, consistent with  
435 the observed intensification of the gyre (Figure 8f) during June 2006 (Aretx-  
436 abaleta et al., 2009).

437 The preceding provides qualitative assessment of the time-averaged veloc-  
438 ity field. In order to compute the differences between predicted and observed  
439 velocities in the time domain, the final forward Quoddy simulation is needed  
440 (Figure 3, CIOA, CIPR, CIPO). This final simulation allows quantification  
441 of skill (Table 4) with regard to not only ADCP velocities (Figure 2), but  
442 also from drifter trajectories. Nine drifters were released along the transect  
443  $T2$  across the Bay of Fundy as part of a multi-year Lagrangian study of  
444 the Gulf of Maine (Manning et al., 2009). The differences between observed  
445 and modeled trajectories are expressed as a velocity error that represents the  
446 mean rate of separation between simulated and observed drifters providing  
447 an integrated measure of skill for short period of times (0.5 – 2 days). The  
448 drifter-derived velocities were not assimilated in the HC simulation (Aretx-  
449 abaleta et al., 2009) or in our current experiments. This skill metric is again  
450 compared with the benchmark provided by the fully assimilative hindcast  
451 simulation.

452 The difference between modeled and observed velocities decreases slightly  
453 from CIPR (Quoddy initialized with climatology) to the initialization from  
454 the first iteration product; a further reduction is achieved using the poste-  
455 rior as initialization (CIPO). The iterative procedure reduces the difference  
456 between the simulation initialized with the traditional OA (CIOA) and the  
457 reference hindcast (HC) simulation by 50%. Similar improvement is evident  
458 when the skill is estimated in terms of drifter separation rate. Of course,  
459 we do not expect CIPO to match the ADCP observations as much as the  
460 HC does, as these data were assimilated into the latter. Interestingly, CIPO  
461 exhibits skill comparable to the HC in terms of the drifter observations.

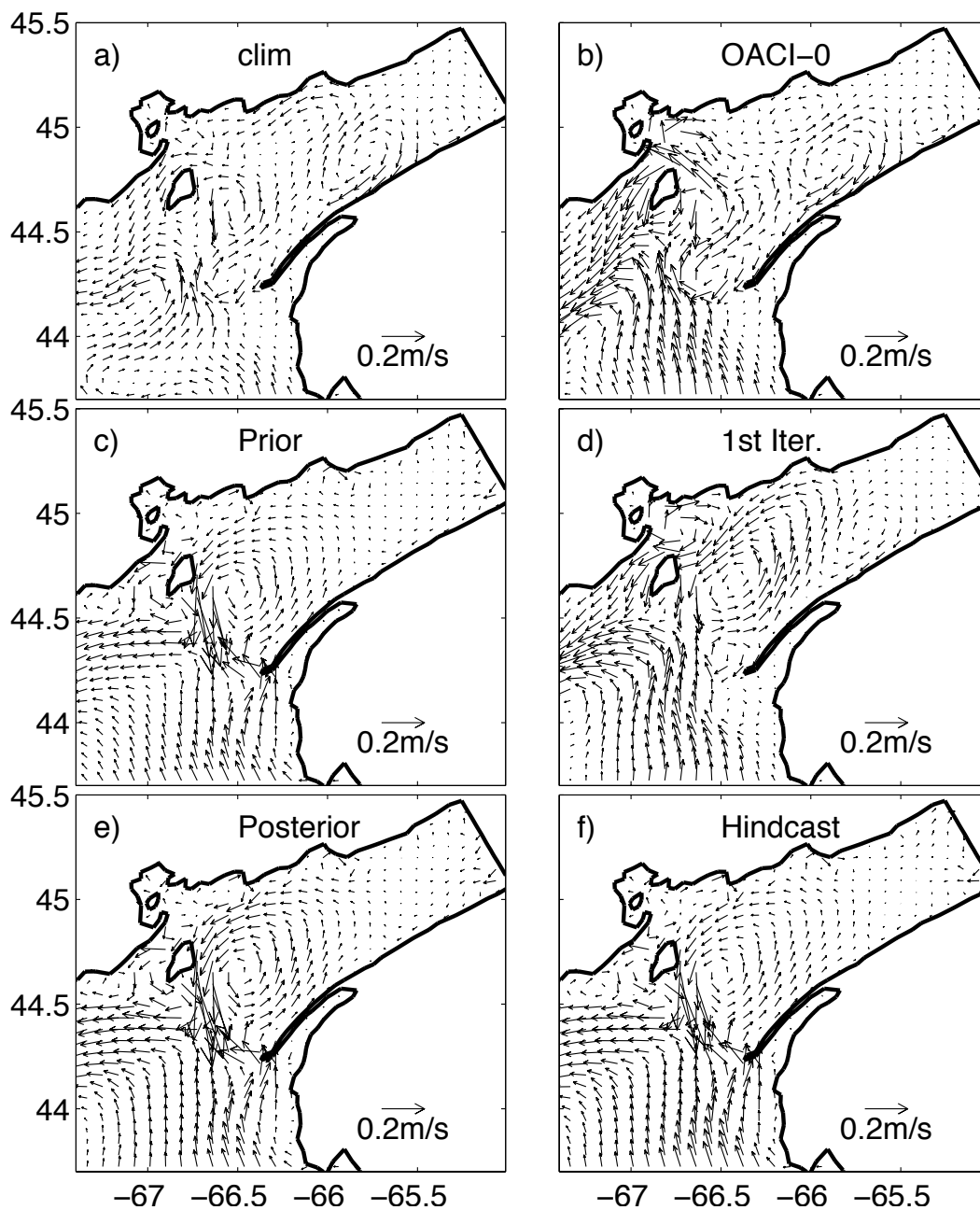


Figure 8: Residual steady-state response (depth-averaged velocity) to the density fields calculated with the different methods using the frequency-domain linear model FUNDY5: (a) Climatological response, (b) traditional objective analysis, (c) prior (no OA), (d) first iteration, and (e) posterior estimates. The averaged flow during the cruise period computed in the hindcast simulation (Aretxabaleta et al., 2009) is included in panel (f).

	Observ.	CIOA	CIPR	CI1 <sup>st</sup>	CIPO	HC
IC		OACI-0	climat.	1 <sup>st</sup> iter.	posterior	posterior
ADCP	0.551	0.159	0.157	0.152	0.147	<i>0.134</i>
drifters	0.385	0.088	0.088	0.082	0.079	0.078

Table 4: Circulation skill, in the proximity of the Bay, of Quoddy simulations initialized using the different hydrographic fields. The first row is the initialization field. The second row is the RMS size of difference ( $\text{m s}^{-1}$ ) between model and observed velocities, except for the first column that corresponds to the size of the observed shipboard ADCP velocity. The HC value is italicized because these data were assimilated and thus the difference constitutes a metric of misfit rather than skill. The third row is the averaged separation rate ( $\text{m s}^{-1}$ ) between observed and model drifters for the different model simulations. For the location of the drifter release, refer to Aretxabaleta et al. (2009). The last column corresponds to the hindcast results included in Aretxabaleta et al. (2009).

## 462 5. Conclusions

463 Dynamical evaluation of anomalies is presented as an alternative to tradi-  
464 tional objective analysis methods for the generation of initialization of short-  
465 term hindcast/forecast simulations. The method is much faster and com-  
466 putationally less expensive than other data assimilation procedures such as  
467 ensemble methods (3-4 circulation model runs in our method versus normal  
468 ensemble sizes requiring 50-100 members).

469 In this application, dynamical objective analysis reduced both temper-  
470 ature and salinity biases to near-zero values. In addition, standard devia-  
471 tions of the misfits were significantly reduced. We hypothesize that these  
472 improvements are attributed primarily to the correction of tidal aliasing of  
473 observations in the Bay. The resulting circulation exhibits skill approaching  
474 that of a hindcast simulation that includes both hydrographic and velocity  
475 data assimilation (Aretxabaleta et al., 2009). We expect the dynamical ob-  
476 jective analysis procedure described herein to be particularly useful in regions  
477 of large tidal amplitude and/or in the proximity of sharp gradients such as  
478 fronts.

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