

# Parametric study of the physical properties of hydrate-bearing sand, silt, and clay sediments:

## 2. Small-strain mechanical properties

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[1] The small-strain mechanical properties (e.g., seismic velocities) of hydrate-bearing sediments measured under laboratory conditions provide reference values for calibration of logging and seismic exploration results acquired in hydrate-bearing formations. Instrumented cells were designed for measuring the compressional (P) and shear (S) velocities of sand, silts, and clay with and without hydrate and subject to vertical effective stresses of 0.01 to 2 MPa. Tetrahydrofuran (THF), which is fully miscible in water, was used as the hydrate former to permit close control over the hydrate saturation  $S_{\text{hyd}}$  and to produce hydrate from dissolved phase, as methane hydrate forms in most natural marine settings. The results demonstrate that laboratory hydrate formation technique controls the pattern of P and S velocity changes with increasing  $S_{\text{hyd}}$  and that the small-strain properties of hydrate-bearing sediments are governed by effective stress,  $\sigma'_v$ , and sediment specific surface. The S velocity increases with hydrate saturation owing to an increase in skeletal shear stiffness, particularly when hydrate saturation exceeds  $S_{\text{hyd}} \approx 0.4$ . At very high hydrate saturations, the small strain shear stiffness is determined by the presence of hydrates and becomes insensitive to changes in effective stress. The P velocity increases with hydrate saturation due to the increases in both the shear modulus of the skeleton and the bulk modulus of pore-filling phases during fluid-to-hydrate conversion. Small-strain Poisson's ratio varies from 0.5 in soft sediments lacking hydrates to 0.25 in stiff sediments (i.e., subject to high vertical effective stress or having high  $S_{\text{hyd}}$ ). At  $S_{\text{hyd}} \geq 0.5$ , hydrate hinders expansion and the loss of sediment stiffness during reduction of vertical effective stress, meaning that hydrate-rich natural sediments obtained through pressure coring should retain their in situ fabric for some time after core retrieval if the cores are maintained within the hydrate stability field.

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### 1. Introduction

[2] Both compressional velocity ( $V_p$ ) and shear velocity ( $V_s$ ) increase when gas hydrate forms in sediments, as demonstrated by numerous studies conducted with different hydrate formation methods, hydrate forming substances, soils, laboratory cells, and effective stress conditions [Bathe *et al.*, 1984; Berge *et al.*, 1999; Kiefte *et al.*, 1985; Lee *et al.*, 2008; Pandit and King, 1982; Pearson *et al.*, 1986; Priest

*et al.*, 2005; Spangenberg and Kulenkampff, 2005; Stoll, 1974; Stoll and Bryan, 1979; Stoll *et al.*, 1971; Winters *et al.*, 2005; Wittebolle and Segó, 1985]. While the details of these experiments differ, the finding of increasing velocity with increasing hydrate saturation is a consistent result and reflects the impact of hydrate on both the small-strain shear stiffness and the bulk modulus of sediments.

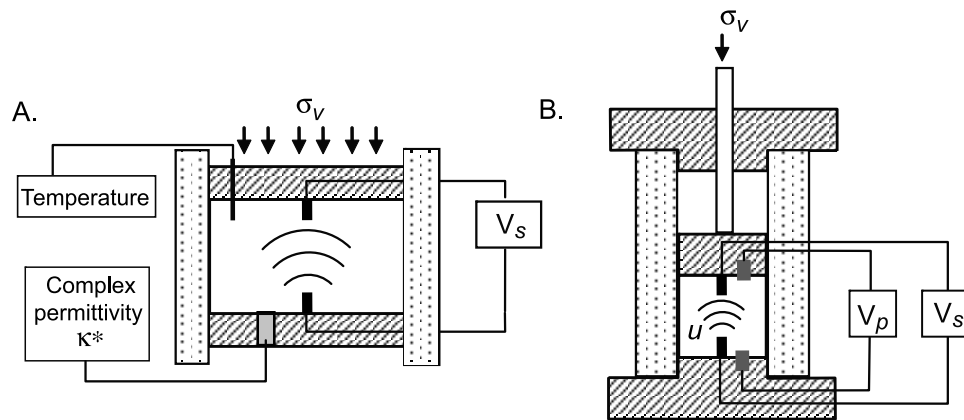
[3] In field settings, seismic velocity data have gained wide applicability in characterizing hydrate-bearing sediments at borehole to regional scales. Borehole sonic logs have often been used to estimate hydrate saturation [e.g., Tinivella and Carcione, 2001; Guerin and Goldberg, 2002]. Vertical seismic profiling [e.g., Holbrook *et al.*, 1996], ocean bottom cable data [Hardage *et al.*, 2006], and analysis of exploration seismic data using seismic attributes, full waveform inversion, and other approaches [e.g., Bangs *et al.*, 1993; Bauer *et al.*, 2008; Dai *et al.*, 2008; Korenaga *et al.*, 1997; Kumar *et al.*, 2007; Westbrook *et al.*, 2008; Zillmer,

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**Figure 1.** Experimental cells built for the small-strain mechanical measurements. (a) The low fluid pressure odometer cell is described by *Lee et al.* [2010a] and accommodates a specimen 4 to 5 cm high and 10 cm in diameter. (b) The high fluid pressure odometer cell (99.5 mm outer diameter; 60 mm inner diameter; 241.5 mm height) is designed for a specimen 4 to 5 cm high and 6 cm in diameter;  $u$  denotes pore pressure.

2006] have also been applied to infer gas hydrate distribution and concentration in natural field settings. In many of these studies, the calibration of seismic velocity as a function of gas hydrate concentration is based on an extension of macroscale and microstructural relationships developed empirically for nonhydrate-bearing sediments.

[4] No study has ever attempted to acquire an exhaustive, internally consistent, laboratory data set documenting small-strain mechanical properties over a range of soil types, effective stress conditions, and gas hydrate saturations. Such a data set is a critical first step for proper calibration of field-based seismic data, which are acquired at lower frequency and average over greater length scales than the laboratory data. This paper reports on  $V_P$ ,  $V_S$ , and small-strain Poisson's ratio for such an exhaustive set of experiments, complementing the electromagnetic data reported by *Lee et al.* [2010b] (hereinafter referred to as paper 1), the thermal conductivity results described by *Cortes et al.* [2009], the strength properties given by *Yun et al.* [2007], earlier results on velocities for sands alone detailed by *Yun et al.* [2005], and summary information provided by *Santamarina and Ruppel* [2010].

## 2. Devices and Methods

[5] Two laboratory cells were designed and built to study hydrate-bearing sediments under zero lateral strain conditions (Figure 1). The low fluid pressure cell operates at atmospheric fluid pressure and was used to gather complex permittivity, compressibility and  $V_S$  data. The electromagnetic data acquired on hydrate-bearing sediments with this cell were reported in paper 1. The high-pressure cell can sustain fluid pressure in excess of 20 MPa. The main advantage of this cell is that the high fluid pressure ensures complete liquid saturation, a necessity since P velocity can decrease by an order of magnitude if saturation falls from 100% to 99%. S velocities are less sensitive to small changes in saturation, meaning that they can be properly measured even in the lower pressure cell. Both cells allow a maximum vertical effective stress of  $\sigma'_v = 3$  MPa. The

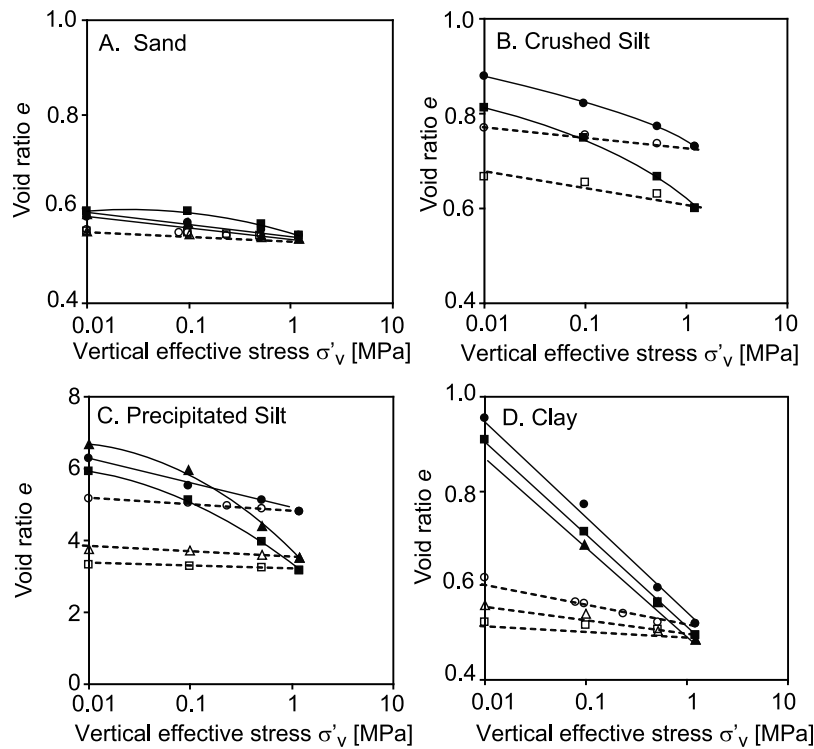
specimen height for these cells ranges between 40 mm and 50 mm to obtain adequate compressibility and wave propagation data.

[6] Pinducers (Valpey Fisher, model VP1093) are used to generate and detect P waves. Bender elements, preferred to shear plates for their superior coupling characteristics, are used for S velocity measurements [*Lee and Santamarina*, 2005]. The sensor pairs are installed in the top cap and in the bottom plate of the cells. The source crystals are connected to signal generators, and the signal from the receiver crystals are amplified then digitized and stored using an oscilloscope operating at a sampling rate at least ten times higher than the frequency band of the measurements. The signal generator is also connected to the digital storage oscilloscope so that input and output signals can be compared to determine travel time.

[7] As detailed by *Lee et al.* [2007] and in paper 1, tetrahydrofuran (THF) was selected as the hydrate former for these experiments. This permitted us to form hydrate from dissolved phase and to obtain both well-controlled hydrate saturations and samples that are inferred to be homogeneous.

[8] Soils, specimen preparation, and measurement procedures for the lower pressure cell are described in paper 1. Only a few details differ for the high-pressure cell: (1) The vertical stress  $\sigma'_v$  is applied in four loading steps: 0.04, 0.5, 1, and 2 MPa; (2) the specimen temperature can range between 20°C to -10°C and is controlled by circulating coolant in the chamber that surrounds the cell; and (3) all  $S_{\text{hyd}} = 0.5$  specimens are prepared with a 60% THF solution to allow for rapid cooling without ice formation (excess THF). Note that for the electromagnetic measurements described in paper 1 it is critical that the  $S_{\text{hyd}} = 0.5$  specimens have excess water, not excess THF. Thus, the  $S_{\text{hyd}} = 0.5$  specimens described in paper 1 were formed with a 10%, not 60%, THF solution.

[9] The test sequence for both the low and high fluid pressure cells consists of loading to a predetermined vertical effective stress, cooling to form hydrate, warming to dissociate hydrate, and then loading to next loading stage. Values of  $V_P$  and  $V_S$  were determined at each stage. A final stage of unloading was imposed on the hydrate-bearing



**Figure 2.** Void ratio versus vertical effective stress for (a) sand, (b) crushed silt, (c) precipitated silt, and (d) clay with pore fluids of deionized water as circles; 10% THF (converts to  $S_{hyd} = 0.5$  after hydrate formation) as triangles; and 21% THF (converts to  $S_{hyd} = 1.0$  after hydrate formation) as squares. The data sets are from low fluid pressure cell. The load is applied at a temperature above the phase transformation to hydrate so that specimens are hydrate-free when loaded (solid line and symbols). Specimens are unloaded (dashed line and open symbols) at a temperature below phase transformation (with hydrates). The loading and unloading “paths” do not truly reflect the experimental sequence, which consisted of loading followed by phase transformation and then unloading within the hydrate stability field at the end of the final loading and hydrate formation cycle. Note that the results for precipitated silt (Figure 2c) are shown on a different scale for void ratio.

specimen within the low-fluid pressure cell following the last loading step in order to study the impact of retrieval of samples from in situ (field) conditions and their analysis at ambient conditions.

**3. Results**

[10] Test results are summarized next, starting with the evolution of sediment porosity during loading, followed by S and P velocity results. The complete experimental data set is given by Lee [2007].

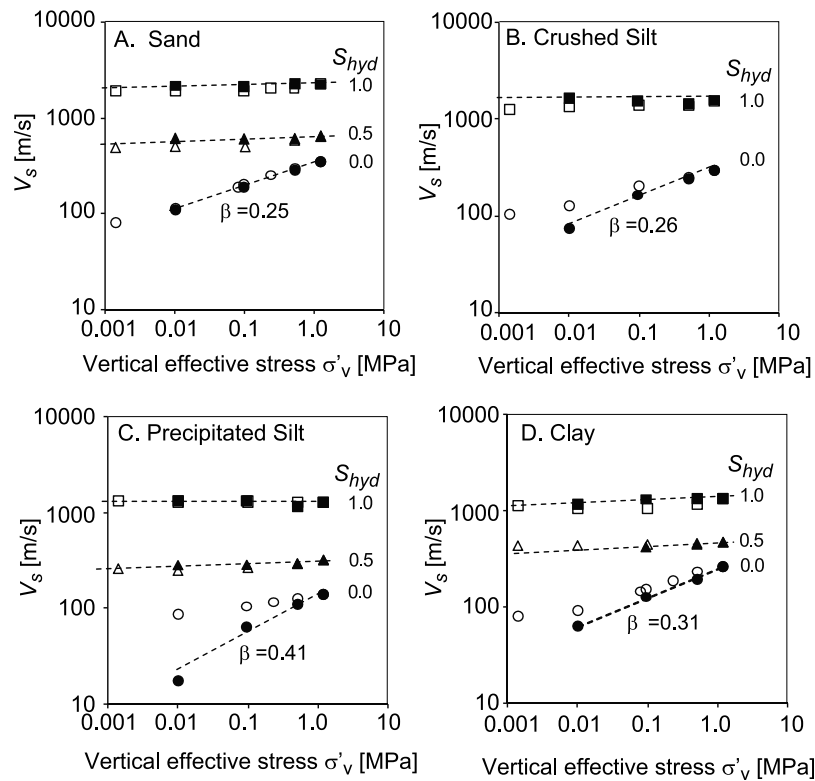
**3.1. Compressibility of Sediments Without Hydrates**

[11] As shown in paper 1, the sediment porosity  $n$  decreases as the vertical effective stress  $\sigma'_v$  increases. Following the standard data reduction approach in geomechanics, Figure 2 shows the porosity cast in terms of void ratio  $e = n/(1 - n)$  as a function of applied vertical effective stress  $\sigma'_v$ . The compression index  $C_c$ , summarized for these experiments in Table 1, is the slope of the normal consolidation line on a plot of void ratio versus  $\log(\sigma'_v/1 \text{ kPa})$ . The sediment compressibility increases with the specific surface of sedi-

**Table 1.** Compression Index  $C_c$  and Swelling Index  $C_s$  for Different Soil Types and for Pore Fluid Mixtures in the Absence of Hydrates

Sediment	Specific Surface	Compression Index $C_c$			Swelling Index $C_s$		
		Fluid <sup>a</sup> 0% THF 100% H <sub>2</sub> O	Fluid <sup>b</sup> 10% THF 90% H <sub>2</sub> O	Fluid <sup>c</sup> 21% THF 79% H <sub>2</sub> O	Fluid <sup>a</sup> 0% THF 100% H <sub>2</sub> O	Fluid <sup>b</sup> 10% THF 90% H <sub>2</sub> O	Fluid <sup>c</sup> 21% THF 79% H <sub>2</sub> O
Sand	0.019	0.02	0.03	0.03	0.01	0.01	0.01
Crushed silt	0.113	0.08	-	0.12	0.03	-	0.03
Clay	36.5	0.21	0.20	0.20	0.05	0.04	0.02
Precipitated silt	120	0.70	1.40	1.40	0.14	0.12	0.05

<sup>a</sup>Corresponds to  $S_{hyd} = 0$  (no hydrate).  
<sup>b</sup>Produces  $S_{hyd} = 0.5$  once hydrate forms.  
<sup>c</sup>Produces  $S_{hyd} = 1$  once hydrate forms.



**Figure 3.** S velocity as a function of vertical effective stress in log-log space for (a) sand, (b) crushed silt, (c) precipitated silt, and (d) clay. The slope  $\beta$  is labeled only for the case of  $S_{hyd} = 0$  (circles). Triangles denote  $S_{hyd} = 0.5$ , and squares represent  $S_{hyd} = 1.0$ . Solid symbols show the loading path, while open symbols and dashed lines denote the unloading data. The description of loading and unloading “paths” is the same as in Figure 2.

ments (Table 1). Sand and crushed silt specimens have stable fabrics that remain unaltered by applied stress and therefore  $C_c$  values are low. Precipitated silt and clay specimens are characterized by high specific surface and exhibit high compressibility. The compressibility is affected by pore fluid permittivity, which decreases with increasing THF concentration (paper 1). While loading is imposed on specimens without hydrates, the hydrate formation-dissociation cycles in the  $S_{hyd} = 0.5$  and  $1.0$  specimens affect the  $C_c$  values for some soils.

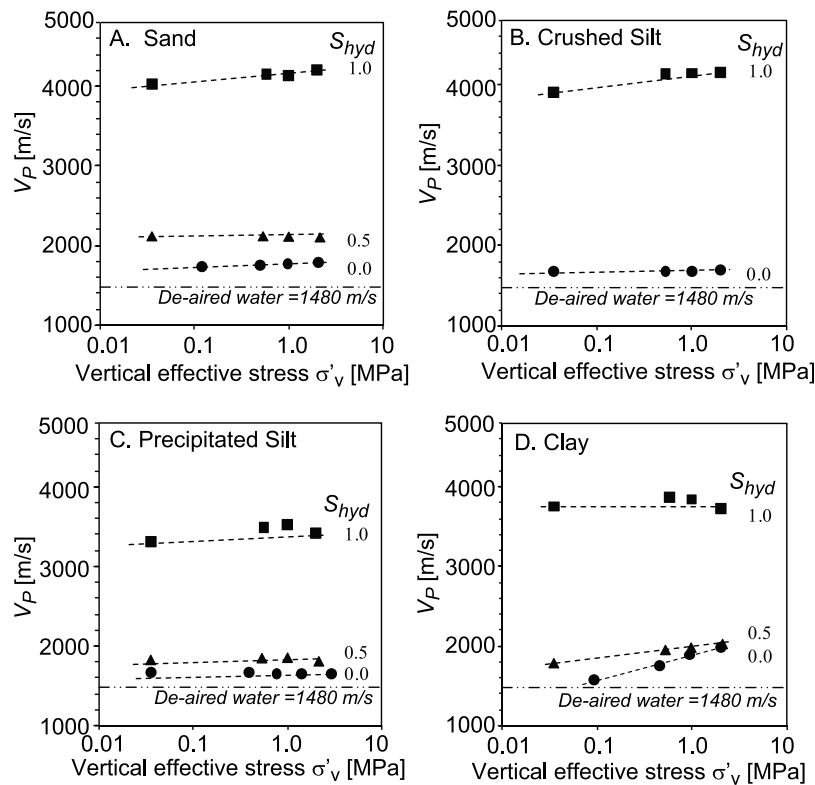
[12] We highlight the relevance of specific surface as a single index parameter that captures grain size, the presence of fines in coarse grained sediments, the transition from round coarse particles to platy fine grains, mineralogy (e.g., clay particles have submicron sizes, and each clay mineral has its own range of specific surface), and dual porosity characteristics. Specific surface inherently accounts for fabric development, stiffness-stress relationships [e.g., *Yun et al.*, 2007], and the impact of hydrate formation on sediments.

### 3.2. Shear Velocity

[13] Contact stiffness between neighboring particles determines the sediment skeletal stiffness, which in turn controls the shear velocity of sediments. The importance of contact stiffness means that we expect a Hertzian-type power relation between velocity and the vertical effective

stress to hold in this case:  $V_S = \alpha(\sigma'_v/\text{kPa})^\beta$  where  $\alpha$  and  $\beta$  are fitting parameters and kPa is included as a divisor to render the expression in parentheses unitless. The factor  $\alpha$  is the shear wave velocity at  $\sigma'_v = 1$  kPa, and the  $\beta$  exponent reflects the nature of contact behavior and the extent of fabric alterations as stress conditions change. This power equation becomes a line when plotted in log-log space,  $\log(V_S) = \log \alpha + \beta \log(\sigma'_v/\text{kPa})$  as in Figure 3. This scale also allows us to compare  $V_S$  values that range over nearly 2 orders of magnitude. Because the  $V_S$  data acquired with the high fluid pressure cell superimpose on those from the low-pressure cell, we show only the low-pressure  $V_S$  data. The shear stiffness of soils without hydrates ( $S_{hyd} = 0.0$ ) increases with the vertical effective stress, and the slope  $\beta$  is greater in high specific surface sediments than in low specific surface sediments.

[14] Figure 3 shows that the S velocities are much higher for hydrate-bearing specimens than for the same specimens having only water as the pore filling material.  $V_S$  is less than  $650 \text{ m s}^{-1}$  in all sediments and at all stress levels when  $S_{hyd} \leq 0.5$ ; however  $V_S$  reaches 1200 to  $2300 \text{ m s}^{-1}$  in sediments with  $S_{hyd} = 1.0$ . The S velocity increases with hydrate saturation owing to an increase in skeletal shear stiffness. For experiments in sands with fine increments in  $S_{hyd}$ , the transition in shear stiffness occurs at  $S_{hyd} \approx 0.4$  [*Berge et al.*, 1999; *Yun et al.*, 2005], a transition also inferred by *Guerin and Goldberg* [2002] based on analysis



**Figure 4.** P velocity as a function of vertical effective stress in log linear space for (a) sand, (b) crushed silt, (c) precipitated silt, and (d) clay. Hydrate saturation  $S_{hyd}$  is indicated by circles for 0, triangles for 0.5, and squares for 1.0. Data are shown only for the loading step.  $V_p$  for de-aired water is provided for reference. Dashed lines show data trends, not best fits. Note that these data were collected only in the high-pressure cell.

of borehole sonic logs. At higher  $S_{hyd}$ , which includes data presented here for  $S_{hyd} = 0.5$  and 1, the presence of hydrates has a significant impact on shear stiffness and becomes more important than the stiffening effect associated with the vertical effective stress. At high hydrate saturations, the small strain shear stiffness becomes insensitive to changes in the vertical effective stress. In fact,  $\beta$  is approximately zero for  $S_{hyd} = 1.0$ . Implications of these results are explored further in section 4.3.

### 3.3. Compressional Velocity

[15] The compressional velocity for water saturated sediments is controlled by the bulk modulus of the water phase. Thus, the  $V_p$  results for the specimens with  $S_{hyd} = 0$ , shown in Figure 4, start near the velocity for de-aired water ( $V = 1480 \text{ m s}^{-1}$ ), and exhibit a minor increase with increasing vertical effective stress due to decreased porosity and increased sediment skeletal stiffness during consolidation. There is some increase in  $V_p$  when the hydrate concentration increases from 0 to 0.5 and a pronounced increase when the hydrate concentration changes from 0.5 to 1. The results for sand, precipitated silt and clay shown in Figure 4 are in agreement with earlier data reported by Yun *et al.* [2005], which also demonstrated no major change in  $V_s$  of sands until hydrate saturation exceeded  $\sim 0.4$ .

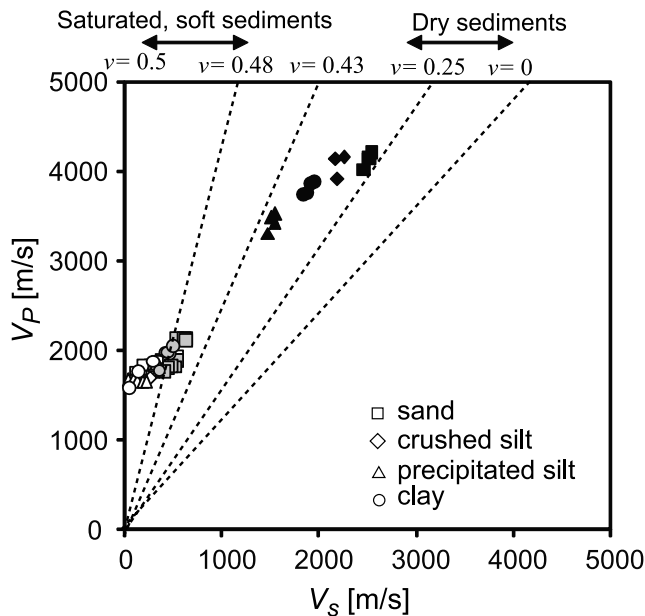
### 3.4. Unloading Data

[16] Unloading of the specimens, which was conducted at low temperatures to preserve the hydrates for the  $S_{hyd} = 0.5$  and 1.0 samples, results in volume expansion, as shown in Figure 2. The swelling index  $C_s$  is the slope of the decompression line on the plot of void ratio  $e$  versus the logarithm of the effective stress  $\sigma'_v$  plot. Calculated  $C_s$  values are summarized in Table 1.  $C_s$  varies little across the range of  $S_{hyd}$  values for low specific surface soils (sand).  $C_s$  is larger for higher specific surface sediments and increases with decreasing  $S_{hyd}$ . This means that volume expansion during unloading is restricted at high hydrate saturation [e.g., Lee *et al.*, 2010a].

[17] Figure 3 shows  $V_s$  values for samples in their loaded and unloaded states. The values of  $V_s$  are higher during unloading than during loading in sediments without hydrates due to the higher interparticle coordination and locked-in strain when sediments have been preloaded. With a few exceptions,  $V_s$  remains almost constant during the unloading of hydrate-bearing specimens with  $S_{hyd} = 0.5$  and 1.0.

## 4. Discussion

[18] The propagation velocity of small-strain elastic waves is determined by the medium's stiffness and mass den-



**Figure 5.** Small-strain Poisson's ratio inferred from  $V_P$  and  $V_S$  for  $S_{\text{hyd}} = 0$  (open symbols),  $S_{\text{hyd}} = 0.5$  (gray symbols), and  $S_{\text{hyd}} = 1.0$  (solid symbols), with the soil type as given by the legend. Data obtained at all effective stress levels are plotted here.

sity  $\rho$  [ $\text{kg m}^{-3}$ ]. The small-strain wave propagation velocities can be expressed in terms of the bulk modulus  $B$  [Pa], the constraint modulus  $M$  [Pa], and the shear modulus  $G$  [Pa] using standard expressions from elasticity:

$$V_P = \sqrt{\frac{M}{\rho}} = \sqrt{\frac{B + \frac{4}{3}G}{\rho}}, \quad (1)$$

$$V_S = \sqrt{\frac{G}{\rho}}, \quad (2)$$

$$\frac{V_P}{V_S} = \sqrt{\frac{M}{G}} = \sqrt{\frac{2(1-\nu)}{1-2\nu}}, \quad (3)$$

where  $\nu$  is the small-strain Poisson's ratio of the medium. These expressions allow us to study the effect of hydrates on the small strain Poisson's ratio and the bulk modulus.

#### 4.1. Small-Strain Poisson's Ratio

[19] The small-strain Poisson's ratio  $\nu$  of dry sediments is very small (e.g., 0.05 to 0.15) because deformations localize at interparticle contacts and the fabric remains constant [Santamarina et al., 2001]. At the other extreme are liquid-saturated soft sediments where  $B \gg G$  and  $\nu$  approaches 0.5. Figure 5 shows our  $V_P$  and  $V_S$  data, with superposed curves corresponding to different values of small-strain Poisson's ratio according to (3). Results show the evolution from a fluid-controlled bulk modulus where  $\nu$  approaches 0.5 for specimens subject to low vertical effective stress and lacking hydrate, to high skeletal stiffness where  $\nu$  approaches 0.25 at increasing vertical stress and particularly when  $S_{\text{hyd}} = 1.0$ .

We underscore that these results give small-strain values of Poisson's ratio for the water-saturated sediment, rather than for the granular skeleton, and should not be used for the analysis of large-strain drained processes in hydrate-bearing sediments. For other reasons, we have advised caution in extrapolating large-strain experimental results on hydrate-bearing sediments to Poisson's ratio in natural settings [Yun et al., 2007].

#### 4.2. Bulk Modulus

[20] Using (1) and (2), the bulk modulus of the hydrate-bearing sediment  $B_{\text{hbs}}$  can be calculated using the measured  $V_P$  and  $V_S$  values, as shown in Figure 6. We can also estimate bounds for the bulk modulus of hydrate-bearing sediments knowing the volume fraction and bulk moduli of components and assuming their spatial arrangement. Extreme bounds for  $B_{\text{hbs}}$  can be computed as the arithmetic mean and the harmonic mean. The Hashin-Shtrikman (hereafter HS) bounds [Hashin and Shtrikman, 1963] shown in Figure 6 assume either that the stiffest (upper bound) or the softest (lower bound) components form shells around the other components. The bulk moduli of the individual components for our specimens (e.g., water, hydrate, and soil grains) are superimposed on Figure 6 as reference values. The results demonstrate that the bulk modulus of hydrate-bearing sediments is limited by the soft components and remains near the lower HS bound for  $S_{\text{hyd}} \leq 0.5$ . The presence of hydrates filling the pore space when  $S_{\text{hyd}} \approx 1.0$  causes a pronounced change in the interaction among components, and the bulk modulus  $B_{\text{hbs}}$  moves toward the upper HS bound.

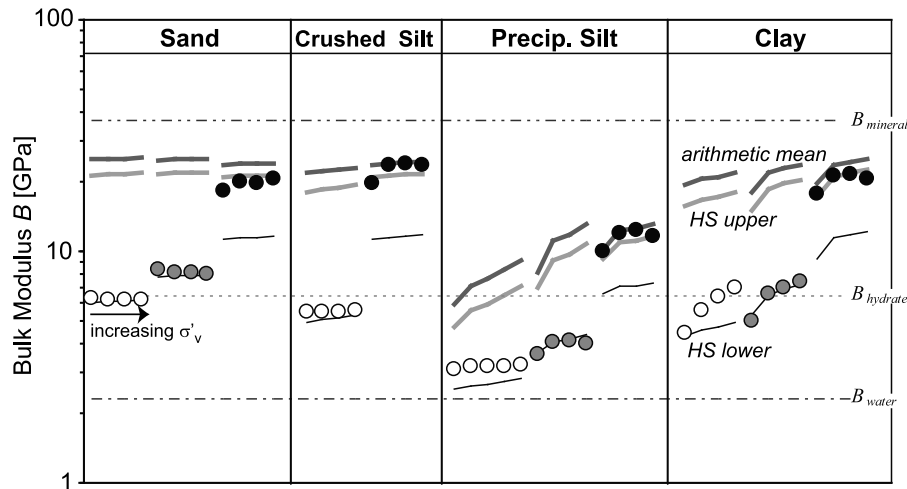
#### 4.3. Material Models

[21] Velocity-stress trends for sediments without hydrates allow us to extract the  $\alpha$  and  $\beta$  parameters in the power expression  $V_S = \alpha(\sigma'_v/\text{kPa})^\beta$  from section 3.2. Experimentally determined  $\beta$  values show that  $\beta = 0$  in solids,  $\beta$  approaches 0 for cemented soils, the Hertzian  $\beta = 1/6$  is obtained with densely packed round sands,  $\beta \approx 0.25$  for rough or angular sand and silt particles (specific surface range  $< 0.1 \text{ m}^2 \text{ g}^{-1}$ ),  $\beta \approx 0.30$  for low-plasticity clays (specific surface range  $\sim 10 \text{ m}^2 \text{ g}^{-1}$ ), and  $\beta \geq 0.40$  in high-plasticity clays (specific surface range  $> 100 \text{ m}^2 \text{ g}^{-1}$ ) [Santamarina et al., 2001]. For sediments lacking hydrates, the  $\beta$  values we obtain from analysis of our data are in agreement with these reference values (Figure 3). In particular, the high  $\beta$  value for precipitated silt is consistent with the high initial porosity and pronounced compressibility during loading, as observed in Figure 2c.

[22] For hydrate-bearing sediments, we chose a general model that resembles the mathematical form of theoretical expressions for cemented soils [Fernandez and Santamarina, 2001] and that combines the stress-dependent sediment response with the stiffness of the hydrate mass [Santamarina and Ruppel, 2010]:

$$V_S = \sqrt{\left(\frac{V_{\text{hyd}} S_{\text{hyd}}^2}{n}\right)^2 \theta + \left[\alpha \left(\frac{\sigma'_v + \sigma'_h}{2 \text{ kPa}}\right)^\beta\right]^2}, \quad (4)$$

where the factor  $\theta$  reflects the microstructural relationship between hydrate and the grains and the  $\alpha$  and  $\beta$  values are



**Figure 6.** Bulk moduli of hydrate-bearing sediments  $B_{\text{hbs}}$  computed using the measured  $V_P$  and  $V_S$  values for (from left to right) sand, crushed silt, precipitated silt, and clay. Open circles denote  $S_{\text{hyd}} = 0.0$ , gray circles correspond to  $S_{\text{hyd}} = 0.5$ , and solid circles represent  $S_{\text{hyd}} = 1.0$ . Each set of 4 or 5 measurements within a single  $S_{\text{hyd}}$  value for each soil correspond to vertical effective stress from 0.04 to 2.12 MPa, ordered in terms of increasing vertical stress to the right. Thin black curves show lower HS bounds, which are the same as the harmonic mean. Light gray and dark gray curves correspond to upper HS bounds and the arithmetic mean, respectively. These bounds were computed using volume fractions and the properties of components (hydrate, water, and mineral) as denoted by the dashed lines. The bulk modulus of the sediment skeleton  $B_{\text{sk}}$  is computed from  $G_{\text{sk}} = V_S^2 \rho$  assuming  $\nu_{\text{sk}} = 0.15$ .

extracted from tests conducted on sediments lacking hydrates. Measured and predicted  $V_S$  for all specimens we tested are plotted in Figure 7a. In all cases, we find  $\theta \leq 0.15$  for our experiments forming hydrate from dissolved phase THF. *Santamarina and Ruppel* [2010] note that  $\theta$  should be substantially larger for hydrate formed in the presence of a gas phase in unsaturated media.

[23] As discussed by *Yun et al.* [2005], the measured  $V_P$  should not be used to determine  $V_S$  for water-saturated hydrate-bearing sediments. Measurement errors in  $V_P$  near low values of  $S_{\text{hyd}}$  are magnified in the estimation of  $V_S$  [*Yun et al.*, 2005]. Conversely the measured  $V_S$  can be combined with the bulk modulus for each component to calculate  $V_P$  based on a Biot-Gassmann type formulation. For low stiffness  $B_{\text{sk}}$  of the skeleton relative to mineral grain bulk modulus  $B_m$ ,  $V_P$  can be written as

$$V_P^2 = V_S^2 \left[ \frac{4}{3} + \frac{2(1 + \nu_{\text{sk}})}{3(1 - 2\nu_{\text{sk}})} \right] + \frac{1}{\rho} \left[ \frac{n(1 - S_{\text{hyd}})}{B_w} + \frac{nS_{\text{hyd}}}{B_{\text{hyd}}} + \frac{1 - n}{B_{\text{min}}} \right]^{-1}, \quad (5)$$

where subscripts hbs, w, min, and hyd denote the hydrate-bearing sediment, water, mineral grains, and hydrate, respectively, and  $\nu_{\text{sk}}$  is the small strain Poisson's ratio for the skeleton, which is typically  $0.1 \pm 0.05$ . Equation (5) is modified from *Santamarina et al.* [2001] to include hydrate. Measured  $V_P$  and  $V_P$  predicted from (5) are plotted in Figure 7b.

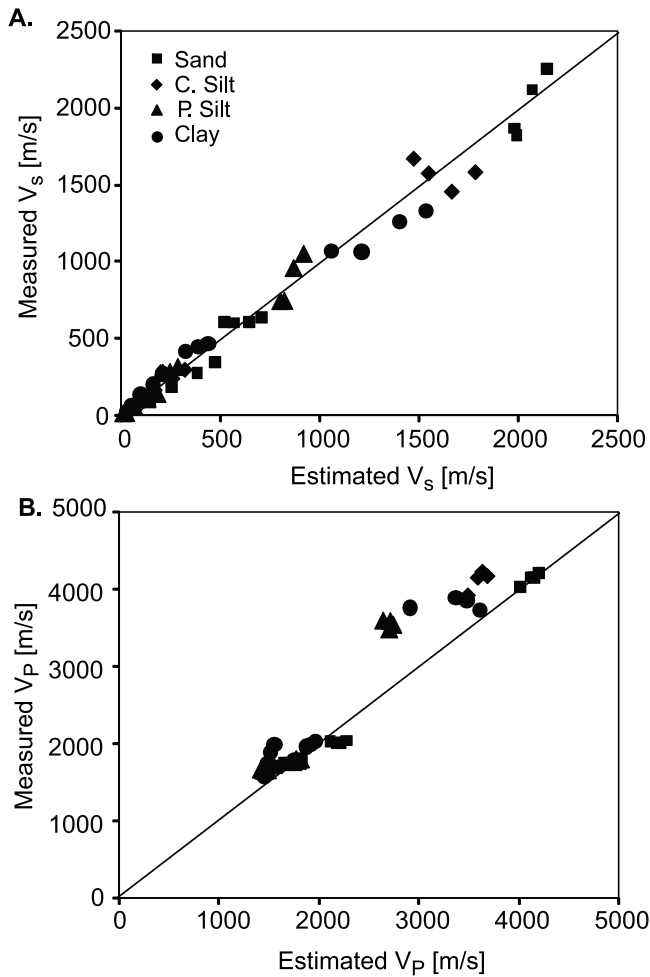
#### 4.4. Hydrate Formation Technique and Seismic Velocities

[24] Many researchers have used effective media models to predict the small-scale mechanical properties of saturated

sediments with and without gas hydrates [e.g., *Chand et al.*, 2006; *Digby*, 1981; *Dvorkin et al.*, 1994; *Helgerud et al.*, 1999; *Jakobsen et al.*, 2000; *Walton*, 1987]. For the analysis of field-scale seismic data, studies typically adopt *Wyllie's* macroscale time-averaged empirical equation [*Wyllie et al.*, 1958] and infer hydrate saturation, thereby inherently assuming a particular microstructural relationship among sediment grains, pore fluid, and gas hydrate [*Bangs et al.*, 1993; *Korenaga et al.*, 1997; *Lee and Collett*, 2001; *Lee et al.*, 1996; *Wood et al.*, 1994].

[25] In practical terms, the cementation model, in which gas hydrate grows at grain contacts, leads to rapid increases in both  $V_P$  and  $V_S$  with increasing  $S_{\text{hyd}}$ , even for small values of  $S_{\text{hyd}}$ . A model in which gas hydrate grows within the pores (pore filling model) produces no appreciable increase in  $V_S$  with increasing  $S_{\text{hyd}}$  until  $S_{\text{hyd}}$  is large enough that gas hydrate begins to affect both the skeletal stiffness (important for  $V_S$ ) and the bulk modulus (important, along with skeletal stiffness, for  $V_P$ ). An intermediate model in which gas hydrate nucleates on grains and grows into pore space was proposed by *Yun et al.* [2005, 2007] to explain small-strain data from sands and large-strain data from a range of sediment types, respectively. This model produces minor cementation and increases in  $V_S$  for  $S_{\text{hyd}} \leq 0.4$  since hydrate rarely forms at the contacts between grains in the absence of a free gas phase [*Yun et al.*, 2005].

[26] The pattern of  $V_P$  and  $V_S$  changes as a function of  $S_{\text{hyd}}$  can be used to compare various laboratory studies and demonstrate the differences in velocities related to hydrate formation method. Figure 8 shows the measured velocity data for sands at all values of vertical effective stress for this study, along with data from other hydrate-bearing sand studies and theoretical curves for various models of hydrate



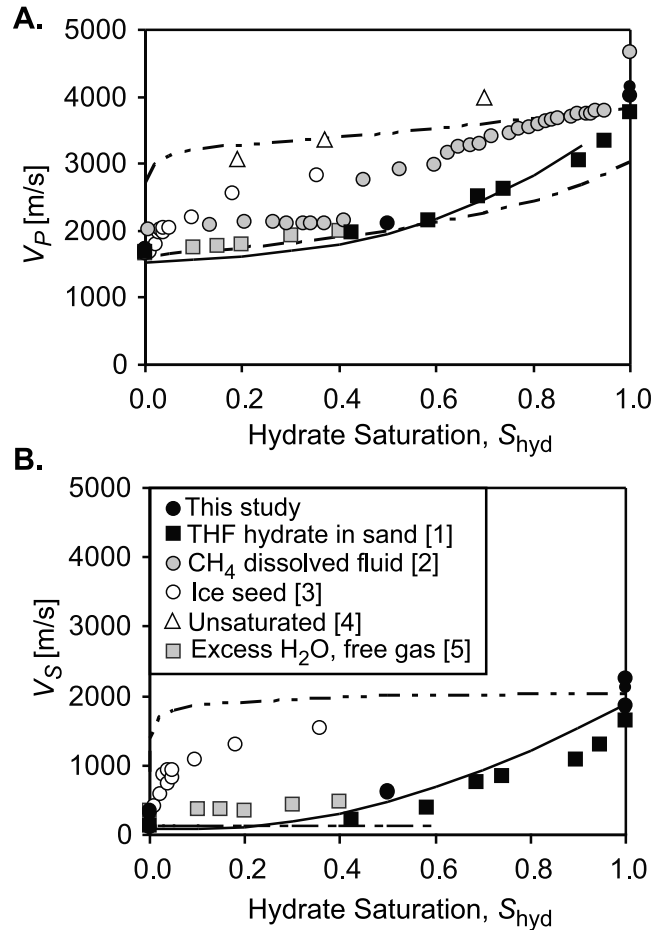
**Figure 7.** Validation of predictive models given by equations (4) and (5) for (a)  $V_s$  and (b)  $V_p$ . Measured versus estimated velocities are shown for all soils (symbols as given in the legend), hydrate saturations, and vertical effective stress levels. Parameters are  $\alpha = 80 \text{ m s}^{-1}$ ,  $\beta = 0.25$ , and  $\theta = 0.15$  for sand;  $\alpha = 50 \text{ m s}^{-1}$ ,  $\beta = 0.26$ , and  $\theta = 0.12$  for crushed silt;  $\alpha = 10 \text{ m s}^{-1}$ ,  $\beta = 0.41$ , and  $\theta = 0.13$  for precipitated silt; and  $\alpha = 23 \text{ m s}^{-1}$ ,  $\beta = 0.31$ , and  $\theta = 0.07$  for clay.

distribution with respect to grains within sediments [Lee, 2007].

[27] The velocity data for hydrate synthesized in soils by percolating gas through unsaturated sediments [Winters *et al.*, 2005] agrees well with the cementation model that predicts a significant increase in small-strain skeletal stiffness with relatively small amounts of hydrate. Gas hydrate formed in this way tends to develop at the menisci between grains, thereby cementing the grains. Likewise, the formation of hydrate by the ice seed method of Stern *et al.* [1996] and Priest *et al.* [2005] preferentially forms hydrate at grain contacts. As the ice melts, water clings to mineral surfaces and contacts, which become the nucleation sites for methane hydrate growth. This leads to an early increase in skeletal stiffness.

[28] Small-strain stiffness does not increase significantly until  $S_{\text{hyd}} > 0.4$  [Yun *et al.*, 2005] in specimens synthesized

by flushing saturated soils with water containing a dissolved phase hydrate former. In this case, hydrates tend to nucleate on grain surfaces and grow into the pore space. The P wave velocity results of Spangenberg and Kulenkampff [2005], obtained with dissolved methane as the hydrate former, are also shown in Figure 8 for comparison with the THF results. When the hydrate volume fraction exceeds  $S_{\text{hyd}} > 0.4$ , the hydrate mass touches more than one particle and can contribute to interparticle coordination, skeletal stability and



**Figure 8.** The impact of hydrate formation method on measured P and S velocities in hydrate-bearing sediments. References are (1) Yun *et al.* [2005] for THF hydrate with no effective vertical stress; (2) Spangenberg and Kulenkampff [2005] for  $\text{CH}_4$  hydrate formed from dissolved phase, with the vertical effective stress unspecified; (3) Priest *et al.* [2005] for  $\text{CH}_4$  hydrate formed from ice seed with  $\sigma'_v = 590 \text{ kPa}$ ; (4) Winters *et al.* [2005] for  $\text{CH}_4$  hydrate formed in unsaturated condition with  $\sigma'_v = 230\text{--}270 \text{ kPa}$ ; (5) Priest *et al.* [2009] for  $\text{CH}_4$  hydrate formed with excess water method with  $\sigma'_v = 500 \text{ kPa}$ . The solid theoretical curve was computed using (4) for  $V_s$  and (5) for  $V_p$  assuming  $\alpha = 80 \text{ m/s}$ ,  $\beta = 0.25$ ,  $\theta = 0.15$ ,  $B_{\text{hyd}} = 5.6 \text{ GPa}$ ,  $B_{\text{min}} = 36 \text{ GPa}$ ,  $B_w = 2.0 \text{ GPa}$ ,  $G_{\text{hyd}} = 2.4 \text{ GPa}$ , and  $G_{\text{min}} = 45 \text{ GPa}$ . The pore-filling model (dash-dotted curve) was computed at  $\sigma'_v = 0.01 \text{ MPa}$ . The cementation model (dash-double dotted curve) was computed at  $\sigma'_v = 2.1 \text{ MPa}$ . The pore-filling model and the cementation model suggested by Dvorkin and Nur [1996] are used to calculate theoretical curves.



stiffness [Yun *et al.*, 2005]. Specimens with hydrate formed in excess water and free gas by Priest *et al.* [2009] behave similar to those with hydrate formed with dissolved methane, since hydrate starts to form around gas bubbles, which reside in the pore space.

[29] Based on the comparison of trends obtained with THF [Yun *et al.*, 2005; this study] and those obtained with dissolved methane by Spangenberg and Kulenkampff [2005], we conclude that the nucleation and growth of THF hydrate are similar to those of methane hydrate formed from dissolved phase, particularly at low  $S_{\text{hyd}}$ .

#### 4.5. Unloading Data: Simulating Pressure Coring

[30] When vertical effective stress on a specimen is reduced, the specimen expands, causing tension on cementing agents at grain contacts. This often produces an irrecoverable reduction in stiffness, a phenomenon commonly observed in cemented soils subjected to decreased vertical effective stress [Baig *et al.*, 1997; Fernandez and Santamarina, 2001].

[31] The unloading data presented in section 3.4 and Figure 2 can be used to explore the impact of decreased vertical effective stress on hydrate-bearing sediments. The experimental conditions that produce a drastic reduction in vertical effective stress without dissociation of the hydrate represent a good analogy for coring hydrate-bearing sediments using pressure coring methods. During modern pressure coring as carried out within the Integrated Ocean Drilling Program and other deepwater drilling expeditions [e.g., Schultheiss *et al.*, 2008], cores ~1 m long are retrieved from hydrate-bearing sediments with the complete release of vertical effective stress ( $\sigma'_v \approx 0$ ) but maintenance of the pore fluid (hydrostatic) pressure. In field applications, pressure core temperatures are often not maintained within the hydrate stability field during core recovery (except in the corer described by Takahashi and Tsuji [2005]), but cores are quickly chilled upon reaching the ship. In our laboratory experiments, temperatures are maintained within the hydrate stability field during the entire unloading history.

[32] The volume expansion and S velocity data shown in Figures 2 and 3 for the unloading cycle indicate that, for  $S_{\text{hyd}} \geq 0.5$ , the presence of hydrate in the specimens hinders swelling and locks in stiffness, at least during the 2 h (sand and crushed silt) to 4 day (clay and precipitated silt) duration of these unloading tests. In field settings, retrieval of a pressure core would take a maximum of a few hours, meaning that sediments with intermediate saturations of hydrate could largely retain their structure as long as the core remains within the hydrate stability field. Note that our data set includes specimens with only three values of  $S_{\text{hyd}}$  (0, 0.5, and 1), so we cannot determine the hydrate saturation that marks the transition between sediments that will be strongly affected by the release of vertical effective stress and those that may maintain their structural integrity during retrieval. We suspect that the transition likely coincides with  $S_{\text{hyd}} \approx 0.4$ , which our previous work has shown to be a saturation level that is associated with a marked increase in skeletal stiffness, at least in sands [Yun *et al.*, 2005].

[33] These unloading results suggest that the probability of sampling hydrate-bearing sediments without disturbing the original sediment fabric increases when the in situ vertical effective stress is low, sediments have low specific

surface, and the hydrate saturation is high. A similar conclusion was reached by Lee *et al.* [2008], who studied synthetic hydrates formed in natural sediments from the deepwater Gulf of Mexico. In all cases, the specimen should be restored to the in situ fluid pressure, vertical effective stress, and temperatures within the hydrate stability field as soon as possible to minimize hydrate dissociation, fluid migration, and later hydrate reformation in new locations within the core.

## 5. Conclusions

[34] Systematic experiments conducted on sand, silts, and clay specimens containing synthetic (THF) hydrate formed from dissolved phase to obtain pore-space hydrate saturations of 0, 0.5, and 1 and subject to vertical effective stress ranging from 0.04 to 2 MPa reveal the following:

[35] 1. The small-strain properties of hydrate-bearing sediments are governed by the state of effective stress, hydrate saturation, and the soil's specific surface. In this context, specific surface is a single soil index that captures grain size, mineralogy and related particle level interactions.

[36] 2. The S velocity increases with hydrate saturation owing to an increase in skeletal shear stiffness. For experiments in sands subjected to minimal vertical effective stress and with fine increments in  $S_{\text{hyd}}$ , the transition in shear stiffness occurs at  $S_{\text{hyd}} \approx 0.4$ . At higher  $S_{\text{hyd}}$ , which includes data presented here for  $S_{\text{hyd}} = 0.5$  and 1, the presence of hydrates has a significant impact on shear stiffness and becomes more important than the stiffening effect associated with the vertical effective stress. At these elevated hydrate saturations, the small strain shear stiffness also becomes insensitive to changes in the vertical effective stress.

[37] 3. The P velocity increases with hydrate saturation due to the increase in both the bulk modulus of pore-filling phases due to fluid-to-hydrate conversion and the shear modulus of the skeleton.

[38] 4. The small-strain Poisson's ratio approaches  $\nu \approx 0.5$  in water-saturated sediments with neither gas nor hydrates and subjected to a low vertical effective stress. When the vertical effective stress is high and in particular when the hydrate saturation is high, the sediment exhibits high skeletal stiffness and Poisson's ratio may decrease to  $\nu = 0.25$ . These values of Poisson's ratio are applicable only to small-strain conditions and cannot be used to analyze the large-strain drained response of hydrate-bearing sediments.

[39] 5. The bulk modulus of hydrate-bearing sediments is limited by soft components and remains near the Hashin-Shtrikman (HS) mixture lower bound for  $S_{\text{hyd}} \leq 0.5$ . However, the presence of hydrates filling the pore space at  $S_{\text{hyd}} \approx 1.0$  causes a pronounced change in the interaction among components, and the bulk modulus  $B_{\text{hbs}}$  moves toward the HS mixture upper bound.

[40] 6. The laboratory technique used to form hydrate has a significant impact on the rate that  $V_P$  and  $V_S$  increases with increasing  $S_{\text{hyd}}$ . Based on this paper and our previous work, we infer that formation of hydrate by bubbling gas through unsaturated sediment will lead to rapid increase in  $V_S$  at low  $S_{\text{hyd}}$ . Hydrate formation using ice seeds also leads to rapid rates of  $V_P$  and  $V_S$  changes with increasing  $S_{\text{hyd}}$ . Hydrate formation from dissolved phase leads to slower  $V_P$  and  $V_S$  increases with increasing  $S_{\text{hyd}}$ . Hydrate nucleates on grain

surfaces and initially grows into pores before grains become interconnected for  $S_{\text{hyd}} \geq 0.4$  [e.g., Yun et al., 2005].

[41] 7. Mathematical relationships based on mechanistic concepts, not mere fitting, are proposed to estimate S and P velocity as a function of the hydrate saturation, vertical effective stress, and sediment-dependent parameters (e.g., specific surface).

[42] 8. At  $S_{\text{hyd}} \geq 0.5$ , the presence of hydrate in sediments hinders expansion and stiffness degradation during the reduction of vertical effective stress, as long as the temperature and fluid pressure are maintained within the hydrate stability field. This finding implies that in situ fabric and sediment characteristics may be preserved when recovering pressure cores from sediments with high hydrate saturation.

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