Effect of roughness formulation on the performance of a coupled wave, hydrodynamic, and sediment transport model

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A B S T R A C T

A variety of algorithms are available for parameterizing the hydrodynamic bottom roughness associated with grain size, saltation, bedforms, and wave–current interaction in coastal ocean models. These parameterizations give rise to spatially and temporally variable bottom-drag coefficients that ostensibly provide better representations of physical processes than uniform and constant coefficients. However, few studies have been performed to determine whether improved representation of these variable bottom roughness components translates into measurable improvements in model skill. We test the hypothesis that improved representation of variable bottom roughness improves performance with respect to near-bed circulation, bottom stresses, or turbulence dissipation. The inner shelf south of Martha’s Vineyard, Massachusetts, is the site of sorted grain-size features which exhibit sharp alongshore variations in grain size and ripple geometry over gentle bathymetric relief; this area provides a suitable testing ground for roughness parameterizations. We first establish the skill of a nested regional model for currents, waves, stresses, and turbulent quantities using a uniform and constant roughness; we then gauge model skill with various parameterization of roughness, which account for the influence of the wave-boundary layer, grain size, saltation, and rippled bedforms. We find that commonly used representations of ripple-induced roughness, when combined with a wave–current interaction routine, do not significantly improve skill for circulation, and significantly decrease skill with respect to stresses and turbulence dissipation. Ripple orientation with respect to dominant currents and ripple shape may be responsible for complicating a straightforward estimate of the roughness contribution from ripples. In addition, sediment-induced stratification may be responsible for lower stresses than predicted by the wave–current interaction model.

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1. Introduction

1.1. Hydrodynamic bottom roughness in coastal ocean models

Bottom stress is a first-order term in the momentum equations that describe coastal circulation and sediment transport, and an essential component of numerical models that represent these processes. It is also important in the generation of near-bed turbulence and subsequently governs mixing near the bed and the dissipation of surface gravity waves. Bottom stress $\tau_0$ in coastal ocean models is typically parameterized with a linear or quadratic relationship between a drag coefficient $C_d$ and flow velocity $U$ at a specific elevation $z$ above the bottom. The quadratic formulation is

$$\tau_0 = \rho C_D U |U|$$  

(1)

where $\rho$ is fluid density. This is consistent with a logarithmic profile defined by

$$|U| = \frac{\sqrt{\tau_0}}{\rho} \ln \frac{z}{z_0}$$  

(2)

where $z_0$ is the hydrodynamic bottom roughness (simply “roughness” hereafter) length and $\kappa$ is von Kármán’s constant (approximately 0.41). This is strictly true only where the flow is unstratified, fully turbulent, steady, and horizontally uniform. In addition, the velocities are assumed to represent measured or modeled flow (1) within the constant-stress portion of the bottom boundary; (2) well above the viscous sublayer; and/or (3) above the tops of roughness elements that contribute to the bottom drag.

Despite these assumptions, logarithmic profiles are a robust and useful approximation to the near-bottom flow even as the theoretically necessary conditions are relaxed. Therefore, many models formulate bottom stress in terms of a roughness $z_0$, or a Nikuradse roughness length $k_r = 30z_0$ (Nikuradse, 1933).

Roughness lengths are used in coastal ocean models to parameterize drag associated with grain roughness $z_{gra}$, the effect of saltating grains during sediment transport $z_{bst}$, and small-scale bottom topography (ripples and biogenic features) $z_{BF}$. These
roughness lengths, as physical distances, are assumed to be additive (Warner et al., 2008), so bottom-boundary layer calculations use

\[ z_0 = \max[z_{ON} + z_{ST} + z_{QBF}, z_{MIN}] \]

where \( z_{MIN} \) is a lower limit representing viscous drag, with a typical value of \( 5 \times 10^{-5} \text{ m} \) (Soulby, 1997). In some cases, one term may dominate the roughness length, depending on physical forcing and bed composition.

Roughness lengths associated with grain roughness \( z_{ON} \), sediment transport \( z_{ST} \), and bedform roughness length (ripples) \( z_{QBF} \) are estimated as

\[ z_{ON} = 2.5D_{50}/30 \]

(4)

\[ z_{ST} = aD_{50}\cdot a_1 \frac{T_r}{1 + a_2T_r} \]

(5)

\[ z_{QBF} = a_3\eta^2_r/\alpha_r \]

(6)

where \( D_{50} \) is the median grain size (in meters), \( a_1 = 0.068, a_2 = 0.024\ln(100D_{50}^{0.50} + 0.0709\ln(100D_{50}^{0.50}) \), \( T_r \) is the ratio of applied shear stress to the critical erosion shear stress (Wiberg and Rubin, 1989), \( \eta_r \) is ripple height, \( \lambda_r \) is ripple wavelength, and \( a_1 \) is a coefficient that may range from 0.3 to 3 for current-generated ripples (Soulby, 1997). Grant and Madsen (1982) proposed \( a_1 = 0.923 \); Raudkivi (1988) used 0.533; and Nielsen (1992) suggested \( a_1 = 0.267 \) for wave-generated ripples.

Roughness lengths are also used to parameterize the drag created by near-bottom wave-induced turbulence (Grant and Madsen, 1979; Signell et al., 1990). Wave–current interaction models predict an apparent roughness length \( z_{app} \) that is generally larger than the inner \( z_0 \) that represents the drag imposed on wave motions by bottom sediment, saltation, or small-scale bed topography. Conversely, near-bed stratification can reduce the bottom stress and reduce the roughness length. Therefore the computation of stresses in a mixed wave–current environment involves specification of multiple physical roughness contributions and the interaction of those contributions with a wave–current interaction model including, if relevant, the influence of stratification. In this study we refer to the “inner roughness” as the physical roughness perceived by the inner wave-boundary layer (calculated using Eq. (3)), and the “apparent roughness” as the roughness perceived by the outer current boundary layer. The latter is typically calculated using a wave–current interaction model such as Madsen’s (1994).

1.2. Effects of roughness parameterization in regional ocean models

The initial spatial distribution of roughness length due to grains and small-scale topography is poorly understood in most cases, due to the inherent difficulty of sampling and/or temporally varying conditions. Modern geophysical techniques allow for non-intrusive estimation of sediment grain size, type, and bedform dimensions. From these, a reasonable initial condition can be specified for roughness length. Sediment transport models, in combination with time-dependent ripple models, calculate evolving ripple dimensions, based on grain size, bottom orbital velocities, and near-bed flow velocity.

It may be imperative to incorporate these types of data into regional models, given the evidence for large spatial variability in sediment grain size and bedform type throughout the continental shelf (Goff et al., 2008). However, few studies have quantified the influence of spatially and temporally varying roughness on model skill. Davies and Lawrence (1995), modeling the Irish Sea, found small changes in modeled velocity magnitude when spatial variations in roughness were considered, though changes in residual patterns or bottom shear stress were not addressed. Nicolle and Karpytchev (2007) found improvements in tidal amplitude and phase when “frictional contrast” was implemented in a semi-enclosed basin. This frictional contrast resulted from the presence of hydrodynamically smooth mudflats over a portion of the domain. Lopes and Dias (2007) addressed the spatial variability in roughness while modeling a Portuguese lagoon, but were not able to show that incorporating this roughness improved performance. The roughness contribution of benthic organisms was considered by Seifert et al. (2009); small changes were observed with regards to modeled mean currents, though no information is given with regard to model skill. Lu and Zhang (2006) selected spatially varying bottom friction coefficients using assimilation of altimeter data, resulting in larger coefficients in shallow water. The influence of roughness is not specifically addressed in the study, though it is implied that it may be responsible for unexplained variability in the bottom friction coefficient. Storm surge modeling in the Irish Sea was improved using a wave–current interaction routine that resulted in spatially varying friction (Jones and Davies, 1998). Establishing the need for spatially and temporally variable (simply “variable” hereafter) roughness in hydrodynamic, wave, and sediment transport models requires both intensive field measurements and models that account for roughness elements.

Our goal is to implement several representations of roughness into a realistic coastal ocean model, and determine if there is a quantifiable increase in model skill for near-bed current magnitude, direction, bottom shear stress, and turbulence dissipation. These representations include a logarithmic velocity method with uniform and constant (simply “uniform” hereafter) roughness, the wave–current interaction method of Madsen (1994) with uniform inner roughness, and wave–current interaction with an inner roughness that accounts for ripple evolution.

Sorted grain-size features near the Martha’s Vineyard Coastal Observatory (MVCO) may provide enhanced roughness in nearshore areas due to gradients in grain size and ripple dimensions (Goff et al., 2005), and provide a suitable case for this study. The parameterization of these features can be achieved by considering the effect of variable grain-size and ripple geometry, though it is not clear what effect this parameterization has on near-bed circulation and bottom stresses. It is also not clear whether incorporating variable roughness actually increases model skill. Intensive measurements of velocity and wave parameters over the sorted grain-size features near MVCO enable us to investigate the performance of regional models with variable roughness. We first describe the field setting and data collection, followed by a description of the numerical model, and the skill assessment methodology.

2. Site description and field data

2.1. Hydrodynamic setting

The MVCO is located on the southeast New England Shelf, 1.5 km offshore of the southern edge of Martha’s Vineyard (Fig. 1). The MVCO consists of a shore lab, air-sea interaction tower (15 m isobath), and a subsurface node (12 m isobath). The 12 m node is located 1.5 km south of the shoreline, and provides continuous cabled power for oceanographic equipment. Tidal currents at MVCO are dominated by the alongshore component (approaching 0.5 m/s at spring tide), while the cross-shore component is significantly smaller (0.1 m/s). Tidal range is over 1 m during spring tides. The largest waves arrive from the south with heights exceeding 4 m and maximum wave periods in excess of 10 s. During the field study described here, maximum significant wave height was 2 m. The steeply sloping beaches and rocky coastline on the southern edge of Martha’s Vineyard suggest that intertidal processes, e.g., wetting and drying, are not important to inner-shelf circulation.
Hydrodynamics near the MVCO are influenced by larger regional patterns, highlighting the need for multiple nested grids and increased nearshore grid resolution. Subtidal-frequency circulation over the inner shelf of southeastern New England is characterized by predominantly westward flow, caused by geostrophic and barotropic forcing, though seasonal variability is observed due to stratification in the spring and fall (Shearman and Lentz, 2003). Tidal forcing is influenced by the Gulf of Maine (to the north) and the mid-Atlantic Bight (to the south). Offshore of the MVCO, He and Wilkin (2006) identified M2 maximum tidal amplitudes of 1 m, depth-averaged currents approaching 1.5 m/s, and tidal residual circulation (depth-averaged) under 0.1 m/s, using a hybrid data assimilation modeling technique. Winds and waves along the northeast coast of the US are influenced by “northeasters” (Butman et al., 2008), which typically occur between the late fall and spring. These storm systems can produce winds exceeding 20 m/s and significant wave heights over 7 m on the inner shelf (National Buoy Data Center, www.nbdc.noaa.gov; buoy 44018; Fig. 3).

2.2. Sorted grain-size features

Geophysical surveys revealed the presence of sorted grain-size features near the MVCO (Goff et al., 2005). Sorted grain-size features are commonly associated with sandy nearshore and inner shelf regions (Cacchione et al., 1984; Murray and Thieler, 2004). They exhibit sharp alongshore gradients in grain-size and relatively gentle bathymetric changes in the alongshore direction. Sorted grain-size features near MVCO consist of bathymetric lows with coarse (0.5 mm) sand and large ripples (heights of 0.10–0.15 m, wavelengths of 0.6–0.8 m) and bathymetric highs with fine sand (0.125 mm) and small ripples (heights of 0.01 m, wavelengths of 0.1 m). The features extend from the shallowest region surveyed (6 m) to depths of 17 m, 3 km offshore, with a maximum alongshore width of less than 1 km. Goff et al. (2005) demonstrated changes in the fine/coarse sand boundaries (tens of meters on the monthly timescale), but found little migration of the bathymetric features over the decadal timescale. The features are underlain by a coarse sand and gravel layer (Goff et al., 2005). Murray and Thieler (2004) hypothesized that these features arise through self-organization and feedback between roughness, enhanced turbulence, and winnowing of fine sediments from the bed.

2.3. Field data

The U.S. Geological Survey performed a bathymetry and sidescan sonar survey of the study area in August, 2007, using a 234-kHz interferometric multibeam sonar, a dual-frequency 100/500 kHz sidescan-sonar system, and real-time kinematic positioning with a differential global positioning system. The resulting
digital elevation model had a 4-m horizontal grid resolution, an estimated horizontal accuracy of ~0.2 m, and vertical precision of ~0.10 m (Denny et al., 2009). This bathymetry was merged with a new 1° digital bathymetric grid constructed by R. Signell (pers. comm.) for the region (41.0–42.4°N, 71.2–69.7°W) using all digital sounding data available from the National Geophysical Data Center (www.ngdc.noaa.gov; Fig. 1). Remaining data gaps were filled by digitizing smooth sheets from older non-digital surveys. The sounding data were adjusted from mean low water or mean lower-low water datums to mean sea level using the NOAA VDatum model for the Gulf of Maine and merged with 1 arc-second land topography. The soundings were gridded using the Generic Mapping Tools (GMT; Wessel and Smith, 1998). The sidescan backscatter amplitudes from the August survey clearly delineate the coarse and fine patches (Fig. 2). Grain-size analyses of bottom samples collected during instrument deployment at 8, 12, and 16-m sites in September 2007 revealed that the sediment distribution within each patch was unimodal with representative sizes of 0.5 mm in coarse patches, and 0.125 mm in finer patches.

Current, wave, and stress measurements were made using a variety of instruments, at multiple depths, over both fine and coarse patches (Fig. 2; Table 1). All acoustic Doppler velocimeters (ADVs) were placed near-bed (<2 mab) to enable measurement of near-bed velocity and wave orbital velocity. Acoustic Doppler current profilers (ADCPs) measured at elevations beginning ~3 m from the bottom to the surface. At sites PV1 – PV6, 68-min bursts were collected every 4 h, while 30-min bursts were collected every 1 h at all other ADV sites. ADCPs collected data every 15 min at the MVCO, and 6 min at the USGS site. Wave statistics were calculated from ADV data using the PUV method.

Bottom stresses were calculated at sites USGS and NODE using three methods: log-profile, inertial-dissipation (Huntley, 1988), and covariance techniques (Trowbridge, 1998; Trowbridge and Elgar, 2001). These methods produce estimates of distinct quantities (shear, dissipation, and stresses, respectively), that are related depending on conditions. However, the covariance technique is deemed the most reliable, as it is the most representative estimate of near-bottom kinematic stress (Sherwood et al., 2006).

Fig. 2. Model domain for highest-resolution model grid (grid 4). Acoustic backscatter amplitude from side-scan sonar mosaic reveal sorted grain-size features near the MVCO. Light gray indicates higher backscatter and coarse sand; dark gray indicates lower backscatter and fine sand. Data locations range from a depth of 8 m (CS8, FS8) to 13 m (PV6). Depth contours (2-m interval, relative to MLW) are show in white. Bottom tiles show sample transect of depth and side-scan sonar signal over sorted grain-size features, with fine and coarse patches.
3. Numerical experiments

Our approach for testing roughness parameterizations focuses on the development of a realistic model of the MVCO region. Nesting from the basin-scale down to the scale of sorted grain-size features is necessary to account for subtidal forcing and wave propagation. We evaluate general model performance, using a uniform roughness, at the multiple nest levels using water level and depth-averaged velocity at one location (MVCO), and then test whether performance for near-bed circulation, bottom shear stress, and turbulence dissipation at near-bed sites is improved by including various roughness parameterizations. Skill assessment with respect to near-bed quantities essentially amounts to a model validation process for near-bed model physics.

3.1. Community Sediment Transport Modeling System

We use the Community Sediment Transport Modeling System (CSTMS; Warner et al., 2008), an open-source numerical modeling system that provides for two-way coupling of the Regional Ocean Modeling System (ROMS) with SWAN, an open-source wave model (Booij et al., 1999). ROMS is a three-dimensional, free surface, terrain-following numerical model that solves finite-difference approximations of the Reynolds–averaged Navier–Stokes equations using the hydrostatic and Boussinesq assumptions (Chassignet et al., 2000; Haidvogel et al., 2000) with a split-explicit time stepping algorithm (Shchepetkin and McWilliams, 2005; Haidvogel et al., 2008). It uses a horizontal curvilinear Arakawa C grid and vertical stretched terrain-following coordinates. We used the generic length-scale method to represent a two-equation \((k-\varepsilon)\) turbulence submodel in our calculations of eddy viscosity (Umlauf and Burchard, 2003; Warner et al., 2005). SWAN solves wave-averaged transport equations for wave action density (energy density divided by relative frequency) and accounts for shoaling, refraction, wind-wave generation, wave breaking, bottom dissipation, and nonlinear wave-wave interactions. Further details regarding the SWAN model are documented by Booij et al. (1999). Specific details for parameter specification, boundary conditions, and model coupling are included below.

3.2. Bottom-boundary layer

Bottom stresses were determined in the bottom-boundary layer routines of ROMS, which offer a range of options (Warner et al., 2008). We present three different approaches to these calculations here. In the simplest case, we specified a uniform roughness \(z_0\) that determined bed stresses consistent with a logarithmic speed profile in the bottom computational cell. A more complex computation parameterized wave–current boundary layer processes (following Madsen, 1994) and, when waves were present, produced enhanced drag on the mean flow and increased bed stresses that were particularly important for sediment transport. At this second level of complexity, a uniform inner roughness length required as input to the wave–current calculation was specified, but the resulting apparent roughness acting on the mean flow varied with depth and wave conditions, derived from our SWAN wave model simulations. At the third and highest level of complexity, roughness calculations were fully dynamic and the inner roughness length provided to the wave–current routine accounted for local grain size, saltation (Wiberg and Rubin, 1989), and ripple height and wavelength (Eq. (6); Grant and Madsen, 1982; Raudkivi, 1988; Nielsen, 1992). These calculations do not account for more complex aspects of ripple geometry such as shape or orientation.

Ripple geometry (height, wavelength, and crest orientation) were determined using the time-dependent approach developed by Soulsby and Whitehouse (2005; hereafter SW05). The SW05 model, as we implemented it in ROMS, postulated that ripples on a mobile bed tend toward an equilibrium geometry that depends on sediment characteristics, wave conditions, current velocity, and the relative strength of waves versus mean currents. The rate at which ripple geometry evolved toward equilibrium values was determined by transport conditions and amount of disequilibria. For example, ripple heights evolved according to

\[
\frac{d\eta_r}{dt} = \frac{\beta}{T} (\eta_{eq} - \eta_r) \tag{7}
\]

where \(\eta_r\) was the extant ripple height, \(\eta_{eq}\) was the equilibrium height for the extant conditions (waves, currents, and sediment size), \(\beta\) was a rate coefficient that depended on transport rate (wave mobility number or non-dimensionalized excess shear stress), and \(T\) was a time scale (wave period or ratio of ripple mass/transport rate). When conditions were below threshold for mobilization, ripples were frozen in their pre-existing state. Otherwise, approximate solutions for Eq. (7) (and analogous formulae for ripple wavelength and orientation) were used to evolve ripple heights (wavelengths and orientations) toward equilibrium. The SW05 model was derived empirically from a large set of lab and field observations, and had the advantage of handling time-dependent evolution of ripple geometry for both waves and currents. The equilibrium values, rate coefficients, and time scales switched, depending on whether waves or currents generate the larger Shields parameters. In our ROMS implementation, bed stresses were calculated at each time step \((\Delta t = 4\ s\) at finest grid resolution) using bed roughness calculated with Eq. (6) and ripple heights and wavelengths from the previous time step, and these bed stresses were used to update ripple geometry for model output and stress calculations in the next time step.
3.3. Model nesting and coupling methodology

We used one-way grid nesting at four levels of resolution to provide boundary conditions for our numerical experiment. In one-way grid nesting applications, the coarser grid provides hydrodynamic information to the finer grid, but not vice versa. This can lead to discontinuities between computed solutions on the child grid and boundary conditions from the parent grid, but use of radiation conditions will allow the boundary condition to relax in consideration of the computed solution.

We ran the wave model SWAN on a coarse grid (grid 1; 5-km resolution) for the entire US East Coast (R. He, North Carolina State University, pers. comm.), forcing with parametric time series of wave height, period, and direction from the Western North Atlantic model output of WAVEWATCH-III (Tolman, 1999), and wind components from the North American Mesoscale model (Rogers et al., 2005). At this grid level, a JONSWAP spectrum (Hasselmann et al., 1973) with 20-degree directional spreading was imposed. SWAN propagated the waves specified at the boundary, generated waves within the domain with the provided winds, and computed two-dimensional wave spectra (frequency and direction) through time over the domain. We used the modification of Rogers et al. (2003), which moves wave energy from the high-frequency portion of the spectrum to the low-frequency portion. This counteracted the tendency of SWAN to overly dissipate low-frequency swell waves. Skill (Brier Skill Score, see below) for wave height exceeded 0.8 at nearby NDBC buoys (44004, 44008, 44018; on US East Coast grid). In all experiments, wave effects were restricted to bottom-boundary layer calculations, and were not considered for computation of radiation stresses or mass transport. Pending implementation of additional methods such as the vortex-force formulation (Uchiyama et al., 2009) renders these effects beyond the scope of this paper.

We ran both ROMS and SWAN on an intermediate grid (grid 2) with a domain encompassing southern New England at 1000-m resolution (Fig. 3). Two-dimensional wave spectra from grid 2 were used for wave boundary conditions. Hydrodynamic boundary forcing was specified as time-series of water level, depth-averaged velocity, temperature, and salinity, all interpolated from the grid 2 model output. Radiation conditions were specified for depth-averaged velocity following Flather (1976) and for water level following Chapman (1985). These boundary conditions allowed the model to relax the imposed boundary values for outward-propagating volume transport and gravity waves (e.g., western boundary velocity during westward flow). Two-way coupling was performed by passing computed fields at 10-min intervals.

The numerical experiments discussed in this paper were performed on the finest grid (grid 4), which represented the region south of Martha’s Vineyard at 200-m resolution (Fig. 3). Two-dimensional wave spectra from SWAN computations on grid 3 were used as wave boundary conditions for grid 4, and water level, currents, temperature, and salinity from ROMS output on grid 3 were used to apply hydrodynamic forcing for grid 4 in the same fashion as described above. However, we adjusted the amplitude of current speeds to improve model agreement with acoustic Doppler current measurements at MVCO. In simulations made without this adjustment, depth-averaged velocity was overestimated while water level was well predicted (Fig. 4). We used T-TIDE (Pawlowicz et al., 2002) to identify the phase and amplitude of major tidal waves.
constituents in the MVCO data and model output, and multiplied the grid 3 output by a factor of 0.86 before using it as input to grid 4. This improved the Brier skill score (defined below) for modeled vs. measured depth-averaged current speed at MVCO from 0.76 to 0.84 (Fig. 4) and had little effect on the model skill for water level or current direction. Disagreement between the model and data on the subtidal timescale may be due to the neglect of wave effects or errors in the subtidal forcing at the 1 km grid level. Significant wave height, wave direction, bottom wave period, and orbital velocity at site MVCO were modeled with varying skill (Fig. 4).

Fig. 4. Comparison of measured and modeled (1) water level, (2) depth-averaged velocity, (3) significant wave height, (4) wave direction (direction waves are coming from), (5) bottom wave period, (6) bottom orbital velocity, and (7) ripple height at the MVCO. In the modified case, the amplitude of the velocity boundary condition was adjusted as a sensitivity test. Water level was minimally affected by the modification. Ripple heights are from adjacent fine (125 µm) and coarse (500 µm) sediment regions.
Orbital velocity, which exerts the most influence on ripple geometry, is overestimated by approximately 25% during the last wave event of the period; this would lead to a 25% increase in calculated equilibrium ripple height (Wiberg and Harris, 1994). Orbital velocity is also overestimated during low-energy periods, but ripples are not dynamic under these conditions. The orbital velocity skill score of 0.79 is towards the upper range of performance reported by Wiberg and Sherwood (2008), where orbital velocity was estimated using local surface wave measurements.

Sediment transport (suspended load and bedload) was activated for the grid 4 experiments. The model was initialized with a single bed layer and bimodal sediment distribution, with exclusively 0.5-mm sand in the coarse regions and exclusively 0.125-mm sand in the fine regions, as delineated by the regions of low (dark) and high (bright) acoustic backscatter amplitude, respectively (Fig. 2). Ripple dimensions were initialized with height \( \eta_i = 0.1 \text{ m} \) and wavelength \( \lambda_i = 0.6 \text{ m} \) on the coarse patches, and \( \eta_i = 0.01 \text{ m} \) and \( \lambda_i = 0.1 \text{ m} \) on the fine patches, based on diver observations and previous studies (Goff et al., 2005; Tratkovski, 2007). Transport during our three-week model simulations produced mixed sediment in computational cells at the coarse–fine boundaries, but did not alter the boundaries. The computed ripple height over fine and coarse domains, along the 12 m isobath, demonstrates the response of the sediment bed to wave forcing (Fig. 4). As wave orbital velocity increased during the event of 9/03/2007, coarse sand ripple heights decreased from the initial value to an equilibrium value of 0.03 m, while fine sand ripple heights increased to 0.02 m. The two subsequent large wave events increased coarse sand ripple heights to a maximum of 0.06 m, and slightly decreased fine sand ripple heights. Modeled ripple geometries are well constrained with \( \eta_i \) ranging between 0.02 and 0.06 m and \( \lambda_i \) ranging between 0.16 and 0.45 m near the MVCO location. These geometries are consistent with diver observations and Tratkovski’s (2007) observations for lower-energy periods during the 2005 field campaign at MVCO.

3.4. Model simulations and skill assessment

Three numerical experiments were conducted on the finest grid (grid 4) to evaluate different implementations of roughness: (1) uniform roughness with \( z_{0g} = 0.0001 \text{ m} \) (case UR); (2) variable apparent roughness \( z_{0gr} \) computed from the wave–current interaction bottom-boundary layer model with inner roughness based on the sum of simulated sediment transport \( z_{0st} \) and grain roughness \( z_{0gr} \) (case WC); and (3) same as case WC with the addition of ripple-roughness contribution \( z_{0rp} \) as input to the wave–current bbl model (case RR). The effective roughness of the wave–current apparent roughness and the ripple-induced roughness is expected to be an order of magnitude greater than that of grains or saltation. Therefore case WC mainly represents the effect of wave–current interaction and the calculated apparent roughness, using a uniform inner roughness. The simulation spanned 9/11/2007–9/23/2007, a period which covered a full spring-neap cycle, and three wave events exceeding 1 m at site MVCO.

We used the Brier skill score and the graphic method of Taylor (2001) to assess changes in model performance. The Brier skill score (Murphy and Epstein, 1989) varies between 1 for perfect skill and negative infinity for poor skill, and is defined as

\[
BSS = 1 - \frac{\sum_{i=1}^{n}(x_i - y_i)^2}{\sum_{i=1}^{n}(x_i - \bar{x})^2}
\]

where \( n \) is the number of points in a time series for model-data comparison, \( x_i \) is \( i \)th observation in the measurements, \( y_i \) is the corresponding modeled value, and \( \bar{x} \) is a point in a null-model time-series. The null-model used here is the mean of the time-series.

The BSS, used with hourly data (\( n = 540 \)), evaluated relative errors in model results at the tidal timescale; model performance in a residual sense can be evaluated by inspecting means over the simulation period. The Taylor diagram allowed us to compare model results with data in terms of correlation, standard deviation, and RMS difference, on a single plot. Values were normalized by the standard deviation of the data to allow data of differing types to be presented on the same scale.

4. Results

4.1. Model skill: current magnitude and direction in the water column

Skill for current speed in the upper water column (9.2–12.7 mab) at the MVCO ADCP was highest for case UR and lowest for case RR; the converse was true in the lower part of the measured water column (Table 2). Depth-averaged velocity skill was minimally affected by roughness changes, and depth-averaged directional skill was maximized under case RR. At site USGS, current magnitude skill peaked under case UR at all depths, though direction was simulated best with case WC.

The general near-surface westward flow was retarded under case RR, with the influence maximized between the 10 and 14-m isobath (Fig. 5). The increase in drag due to the ripple-roughness contribution was responsible for the reduction in flow velocity. Reduced near-surface skill at both ADCP sites for case RR indicated that this reduction in westward flow was inconsistent with observations. Conversely, under case UR residual westward velocities at the deepest ADCP bins (3.22 mab) were overestimated; increasing roughness reduced these velocities in line with observations.

4.2. Model skill: near-bed current magnitude and direction

Near-bed current magnitudes were modeled with similar skill as currents higher in the water column, though the effect of roughness was varied between measurement locations (Fig. 6). At most sites, case UR produced the highest skill, though performance for case WC declined only slightly overall, and showed skill increases at 4 of 10 sites. Case RR showed a minimal increase in skill from case UR at two sites; both are located near the MVCO location. There was a pattern to the changes in skill; increasing roughness corresponded to increased skill at southeastern sites, and decreased skill at western sites. The same trend was observed for current direction.

Decreased skill at the western sites was largely due to changes in the timing of velocity, due to increased drag for case RR. Though flood and ebb magnitudes appeared to be congruent with observa-

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<td>0.60</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9.2–12.7 mab</td>
<td>0.68</td>
<td>0.45</td>
<td>0.63</td>
<td>0.47</td>
<td>0.60</td>
<td>0.45</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Depth-averaged</td>
<td>0.74</td>
<td>0.54</td>
<td>0.72</td>
<td>0.55</td>
<td>0.72</td>
<td>0.63</td>
<td></td>
<td></td>
</tr>
<tr>
<td>USGS</td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.2–6.2 mab</td>
<td>0.85</td>
<td>0.64</td>
<td>0.85</td>
<td>0.69</td>
<td>0.84</td>
<td>0.65</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.2–9.2 mab</td>
<td>0.85</td>
<td>0.60</td>
<td>0.84</td>
<td>0.66</td>
<td>0.81</td>
<td>0.60</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9.2–12.7 mab</td>
<td>0.80</td>
<td>0.50</td>
<td>0.74</td>
<td>0.51</td>
<td>0.67</td>
<td>0.40</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Depth-averaged</td>
<td>0.85</td>
<td>0.67</td>
<td>0.83</td>
<td>0.70</td>
<td>0.79</td>
<td>0.62</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
tions for case RR (Fig. 7), increased drag altered the phasing of flood and ebb tides, thereby reducing skill on the tidal timescale. De-meaned flood and ebb directions were largely unchanged between cases. Mean velocity directions were shifted clockwise with increased roughness (Figs. 5 and 7), consistent with observations at five of the near-bed sites. Both the data and model showed a general mean near-bed circulation to the west; the modeled westward flow diverged near the 12-m isobath, though the data did not display that divergence. Poorer agreement at the shallowest sites may be due to the neglect of wave radiation stresses in the model or instrument compass problems.

Cases UR and WC appeared largely indistinguishable with regard to current magnitude and direction on the Taylor diagram, while case RR appeared to increase error at most sites (Fig. 8). Standard deviations for velocity magnitude were closer to the data in case RR, as the tidal timescale velocity magnitudes were lowered by increased roughness. The velocity phasing errors for case RR were not represented in the standard deviation values, but were evident in the lowered correlation values. Typical error metrics such as bias, RMSE, and normalized RMSE suggest lower error for case RR, but do not account for the reduced temporal correlation due to excessive drag (Table 3).

In the frequency domain, modeled near-bed currents at site USGS for case UR matched the phase of the dominant $M_2$ constituent, though the amplitude was modeled best under case RR (Table 4). Case RR gave rise to larger errors for $M_2$ phasing, which

Fig. 5. Vector differences (cases UR-case RR) for time-mean near-surface and near-bed current velocities.
is evident in the Brier Skill Score, but not RMSE values. For total amplitude, case WC generated the least error. The frequency domain analysis demonstrates the difficulty of simulating magnitudes and phasing while simultaneously testing bottom roughness parameterizations and boundary conditions.

4.3. Model skill: bottom shear stress and turbulence dissipation

Skill for current-induced shear stresses was maximized using an inner roughness that was substantially smaller than typical parameterizations (Table 5). The addition of wave–current interaction (and the increased apparent roughness) yielded larger stresses (Figs. 8 and 9); skill was still reasonable though decreased relative to case UR. Case RR, with the addition of ripple roughness, significantly overestimated stresses. In terms of turbulence dissipation, case WC performed with the highest skill, while case UR and case RR underestimated and overestimated dissipation, respectively. Error for case RR was increased during wave-affected periods, when modeled ripples were larger (09/01/07–09/04/07; 09/10/07–09/14/07), and production of turbulence was greater. Sediment-induced stratification may have also been present during these periods, which would dampen turbulence and reduce shear stress. The higher skill for case UR with respect to stresses, and case WC with respect to dissipation, suggests that performance of wave–current interaction and turbulence closure routines were maximized with different values of roughness. We also tested the effect of vertical resolution by varying the vertical stretching parameter to increase near-bed vertical resolution. Under case WC, increased near-bed resolution did not increase skill for stresses (or near-bed currents); this suggests that the original vertical resolution was sufficient to describe the velocity profile and for computations of turbulence and shear stress.

5. Discussion

5.1. Effect of roughness on model skill

The response of modeled current magnitudes and directions to roughness formulation suggests that near-bed circulation is not better-predicted by including spatial and temporal variation in hydrodynamic bottom roughness. Skill was improved higher in the water column at two of the ten sites (MVCO and USGS); this is consistent with increases in near-bed skill at those same sites. However all other near-bed sites showed a decrease in skill when ripple roughness was activated, due to a substantial increase in drag over the coarse sand patches. The hypothesis that inclusion of ripple-induced roughness (with the present parameterization) increases model performance is therefore not supported; use of uniform bed roughness (which may be tuned to maximize skill) along with a wave–current interaction routine performs with the best overall skill with respect to current magnitude, direction, and stresses. Comparison of the individual contribution of roughness components (Table 6) indicates that ripple-induced roughness is the dominant term in the increased apparent roughness.
Overestimation of orbital velocity by the wave model (Fig. 4) may lead to an overestimate of ripple height (and inner roughness), but this study shows that with the lowest published values of $\alpha$, (and therefore ripple-induced roughness) the skill of the hydrodynamic model is reduced. There is more uncertainty in the parameterization of ripple-induced roughness than uncertainty in the wave and ripple models. Further work will test the skill of time-dependent ripple models in the nearshore environment.

Our approach involved first maximizing skill using a uniform roughness at all grid levels, with a given set of boundary conditions, and then varying roughness parameterization at the finest grid level. Alternatively, a spatially variable roughness could have been implemented at all scales (e.g. using depth as a surrogate for roughness where bedform data were not available), and boundary conditions could be altered for agreement. That exercise, however, does not produce insight towards the effect of bottom roughness parameterization on regional applications where bottom roughness length is unknown, but thought to be highly variable (i.e. over sorted bedforms). Tuning roughness length at the multiple near-bed sites, using data assimilation, does not provide guidance for regional applications or model development either. The implementation of boundary conditions and bottom roughness...
parameterization must depend on the goals of the modeling study and the availability of field data. If boundary conditions are known with high accuracy, then data assimilation of near-bed currents may help describe variability in bed friction. In the case presented here, the actual nature of the bed is well known, but the implementation of the bed in ocean models must still be tested rigorously. Our results suggest that the parameterization of roughness due to ripples is more complicated than Eq. (6), and requires further investigation with regards to ripple shape and orientation. Ideally, the influence of ripples should be a function of orientation, where drag is minimized in situations of bedform-parallel tidal currents and maximized for bedform-normal tidal currents. Testing such an algorithm would require a field setting where wave direction is not consistently normal to the tidal currents (unlike the setting described here).

There are two general approaches to model tuning: a top-down and a bottom-up approach. With the former, if modeled water levels and currents over the domain are accurate, then the bottom-boundary layer formulation is considered adequate. With the latter

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### Table 3

Bias, root-mean-square error (RMSE), and normalized root-mean-square error (NRMSE) for modeled near-bed current magnitudes at all sites, for three cases.

<table>
<thead>
<tr>
<th>Site ID</th>
<th>Bias (m/s)</th>
<th>RMSE (m/s)</th>
<th>NRMSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>PV1</td>
<td>-0.03</td>
<td>-0.02</td>
<td>-0.01</td>
</tr>
<tr>
<td>PV2</td>
<td>-0.04</td>
<td>-0.03</td>
<td>-0.01</td>
</tr>
<tr>
<td>PV3</td>
<td>-0.04</td>
<td>-0.03</td>
<td>-0.01</td>
</tr>
<tr>
<td>PV4</td>
<td>-0.04</td>
<td>-0.03</td>
<td>-0.01</td>
</tr>
<tr>
<td>PV5</td>
<td>-0.03</td>
<td>-0.03</td>
<td>-0.01</td>
</tr>
<tr>
<td>PV6</td>
<td>-0.04</td>
<td>-0.03</td>
<td>-0.01</td>
</tr>
<tr>
<td>FS8</td>
<td>-0.02</td>
<td>0.00</td>
<td>0.02</td>
</tr>
<tr>
<td>CS8</td>
<td>-0.04</td>
<td>-0.02</td>
<td>0.01</td>
</tr>
<tr>
<td>USGS</td>
<td>-0.02</td>
<td>-0.02</td>
<td>0.00</td>
</tr>
<tr>
<td>NODE</td>
<td>-0.02</td>
<td>-0.02</td>
<td>0.00</td>
</tr>
</tbody>
</table>

---

### Table 4

Observed and modeled tidal constituents for five largest observed constituents, at site USGS. Sum of all constituents includes constituents not shown in table.

<table>
<thead>
<tr>
<th>Constituent</th>
<th>Observed Amplitude (m/s)</th>
<th>Case UR Amplitude (m/s)</th>
<th>Case WC Amplitude (m/s)</th>
<th>Case RR Amplitude (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>M2</td>
<td>0.116</td>
<td>0.149</td>
<td>0.138</td>
<td>0.114</td>
</tr>
<tr>
<td>S2</td>
<td>0.025</td>
<td>0.033</td>
<td>0.028</td>
<td>0.023</td>
</tr>
<tr>
<td>K1</td>
<td>0.017</td>
<td>0.017</td>
<td>0.014</td>
<td>0.009</td>
</tr>
<tr>
<td>O1</td>
<td>0.014</td>
<td>0.011</td>
<td>0.010</td>
<td>0.005</td>
</tr>
<tr>
<td>M6</td>
<td>0.011</td>
<td>0.011</td>
<td>0.009</td>
<td>0.008</td>
</tr>
<tr>
<td>Sum of all constituents</td>
<td>0.218</td>
<td>0.256</td>
<td>0.237</td>
<td>0.187</td>
</tr>
</tbody>
</table>
5.2. Wave–current interaction and ripple roughness parameterization

Model skill in terms of circulation was affected minimally by parameterization of roughness (Fig. 8), but bottom stresses were significantly overestimated using standard values of parameter $a_r$. Using measured near-bed and wave orbital velocities, Madsen’s (1994) wave–current model was used to estimate current stresses. The derived estimates agreed with the covariance stress estimates when an average $z_0 = 1 \times 10^{-4}$ m was used (the uniform value used above). This is significantly less than the roughness associated with 0.01 m high and 0.1 m long ripples ($a_r = 0.267$, $z_0 \sim 2.7 \times 10^{-4}$ m), but larger than the roughness associated with the sand grains themselves ($z_0 = k_s/30 = 2.5D_{50}/30 = 1 \times 10^{-5}$ m for 125 µm sand). At each measurement time, a $z_0$ was found that maximizes agreement between the derived stresses and covariance stress estimates. This time series of $z_0$ (not shown) demonstrated large fluctuations that may be due to physical changes in roughness, or inherent noise in the measurement process (Gross et al., 1993). There was little coherence between calculated $z_0$ and physical measurements such as wave height or wave orbital velocity (a surrogate for ripple formation). This suggests that use of an intermediate $z_0$ (more than the grain contribution, but less than ripple contribution using typical values of $a_r$) can be used to adequately model current-induced stresses, though this may be due to the relative alignment of the dominant currents and ripple crests, the shape of the ripples, or sediment-induced stratification. There is a directional trend to the model-data mismatch: stresses generated by westward flows are consistently overestimated by the model (in comparison to eastward flows). This may indicate the presence of sediment stratification during westward (ebb) flows.

Table 5

<table>
<thead>
<tr>
<th>Stress skill</th>
<th>Data</th>
<th>Case UR</th>
<th>Case WC</th>
<th>Case RR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>–</td>
<td>0.61</td>
<td>0.51</td>
<td>0.29</td>
</tr>
<tr>
<td>Mean stress value (Pa)</td>
<td>0.041</td>
<td>0.036</td>
<td>0.048</td>
<td>0.072</td>
</tr>
<tr>
<td>Dissipation skill</td>
<td>–</td>
<td>0.45</td>
<td><strong>0.50</strong></td>
<td>0.32</td>
</tr>
<tr>
<td>Mean dissipation value (W/kg)</td>
<td>$1.53 \times 10^{-6}$</td>
<td>$0.65 \times 10^{-6}$</td>
<td>$0.94 \times 10^{-6}$</td>
<td>$2.20 \times 10^{-6}$</td>
</tr>
</tbody>
</table>

Fig. 9. Comparison of measured and modeled current-induced stresses and turbulence dissipation from three roughness cases.

Table 6

Example of mean and maximum modeled apparent outer roughness ($z_{0\text{app}}$) in the presence of waves, and inner roughness ($z_0$) contributions from ripples ($z_{app}$), sediment grains ($z_{0\text{gr}}$), and saltation ($z_{0\text{salt}}$). All values are from fine and coarse sand model locations, at 12 m depths, nearest the MVCO. All values in meters.

<table>
<thead>
<tr>
<th>Roughness</th>
<th>125 µm sand</th>
<th>500 µm sand</th>
</tr>
</thead>
<tbody>
<tr>
<td>$z_{0\text{app}}$ (with uniform $z_0$)</td>
<td>$2.0 \times 10^{-7}$</td>
<td>$2.0 \times 10^{-9}$</td>
</tr>
<tr>
<td>$z_{0\text{app}}$ (with calculated $z_0$)</td>
<td>$9.0 \times 10^{-8}$</td>
<td>$3.5 \times 10^{-7}$</td>
</tr>
<tr>
<td>$z_{0\text{gr}}$</td>
<td>$8.0 \times 10^{-3}$</td>
<td>$1.0 \times 10^{-3}$</td>
</tr>
<tr>
<td>$z_{0\text{salt}}$</td>
<td>$5.0 \times 10^{-5}$</td>
<td>$5.0 \times 10^{-5}$</td>
</tr>
<tr>
<td>$z_{0\text{app}}$ (with calculated $z_0$)</td>
<td>$2.0 \times 10^{-6}$</td>
<td>$8.9 \times 10^{-6}$</td>
</tr>
</tbody>
</table>
Although inclusion of ripple-induced roughness produces minor changes in model skill, the physical presence of ripples on the seabed generates increased turbulence, thereby retaining coarser fractions, winnowing finer fractions, and preserving grain-size distributions. The stress measurements (via the covariance technique) may have been affected by sediment-induced stratification; this may account for traditional values of $a_r$ producing modeled bottom stresses in excess of measurements. This would tend to dampen turbulence and reduce bottom shear stress, while model estimates (unstratified conditions) would overestimate stresses under the same flow, wave, and bedform conditions. It should also be noted that the turbulence model used here (in combination with the wave–current interaction routine) may not be optimal for simulating stresses and turbulence under a wave field; other methods such as Mellor’s (2002) method should be tested in a similar context. These limitations of the model preclude a definitive determination of the correct parameterization of roughness with regards to bottom shear stress, but the findings regarding circulation are unaffected.

6. Conclusion

We developed a regional model for hydrodynamics, waves, and sediment transport on the southern New England inner shelf, where dynamic bedforms alter the physical roughness and presumably, the hydrodynamic roughness. We found that use of variable roughness in this coastal ocean model does not significantly improve skill for circulation, stresses, or turbulence dissipation, despite a large contrast in physical roughness. The widely used method of varying a uniform roughness to maximize agreement with data appears to generate the same level of skill with respect to circulation; patterns of sediment transport, however, will be dependent on local gradients in roughness and bottom shear stress. Performance with respect to stresses may have been complicated by the effect of sediment-induced stratification; unrepresented stratification within the model may account for overestimation of stresses. The relationship between ripple geometry and roughness is modulated by a coefficient ($a_r$) which has a wide range in the literature; this range probably reflects missing information related to ripple geometry (e.g. shape, skewness). The value of $a_r$ may also be dependent on the orientation of the ripples with respect to the dominant flow direction. In our study area, wave crests are oriented roughly parallel to shore, and dominant currents are in the alongshore direction. Therefore it is possible that the flow field does not perceive the aligned ripples as additive drag elements.

This study did not investigate the importance of hydrodynamic roughness on spatial patterns of sediment transport (due to data limitations), but it is assumed that large contrast in ripple heights maintains turbulence over coarse deposits and prevents deposition of finer sand fractions. Further work is needed to address the partitioning of form drag and skin friction within the model: sediment transport is initiated by the skin friction component, but turbulence is affected by the combined contribution with spatial variations over the ripple field, which highlights the need for consistent modeling of each component. Maintenance of the sorted grain-size features at the study location (and for sediment transport in general) depends on a feedback between roughness, turbulence, and advection of finer fractions away from regions of larger ripples (Murray and Thieberger, 2004). The features here have maintained position over yearly timescales, and this mechanism must be partially responsible. Further study, using the time-dependent ripple model, will elucidate the event-scale formation of ripple fields, the associated turbulence, and advection of sediment on the inner shelf.

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References


