Metrics of hurricane-ocean interaction: vertically-integrated or vertically-averaged ocean temperature?

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Abstract. The ocean thermal field is often represented in hurricane-ocean interaction by a metric termed upper Ocean Heat Content (OHC), the vertical integral of ocean temperature in excess of 26°C. High values of OHC have proven useful for identifying ocean regions that are especially favorable for hurricane intensification. Nevertheless, it is argued here that a more direct and robust metric of the ocean thermal field may be afforded by a vertical average of temperature. In the simplest version, dubbed $T_{100}$, the averaging is from the surface to 100 m, a typical depth of vertical mixing by a category 3 hurricane. OHC and $T_{100}$ are well correlated over the deep open ocean in the high range of OHC, $\geq 75 \text{kJ cm}^{-2}$. They are poorly correlated in the low range of OHC, $\leq 50 \text{kJ cm}^{-2}$, in part because OHC is degenerate when evaluated on cool ocean regions, $\leq 26^\circ\text{C}$. OHC and $T_{100}$ can be qualitatively different also over shallow continental shelves: OHC will generally indicate comparatively low values regardless of the ocean temperature, while $T_{100}$ will take on high values over a shelf that is warm and upwelling neutral or negative. In so far as the ocean thermal field alone is concerned, these warm, shallow continental shelves would appear to be as favorable for hurricane intensification as are warm, deep ocean regions.

1 Hurricanes and the ocean

Hurricanes draw energy from the ocean in the form of sensible and latent heat fluxes that result from very high wind speeds and a rather small temperature difference between the subtropical atmosphere and warmer sea surface, typically only a few °C (Emanuel, 1999). Hurricanes are known to cool the sea surface by anywhere from 1 to 4°C (Fig. 1; Leipper and Volgenau, 1972; Price, 1981; Zedler et al., 2002; D’Asaro et al., 2007), locally, which is enough to reduce significantly or even reverse the hurricane-ocean temperature difference. This hurricane-induced cooling of the sea surface must reduce the hurricane-ocean heat flux and thus hurricane intensity to some degree (Bender et al., 1993; Schade and Emanuel, 1999; Cione and Uhlhorn, 2003). This paper considers the ways in which the ocean generally, and this phenomenon in particular, might be represented within a hurricane-ocean forecasting system.

1.1 Observations, forecasts, and a hierarchy of ocean models

The ocean component of a hurricane forecasting system can take one of several different forms. In the most comprehensive version, ocean initial (or present state) temperature (and salinity) data $T_i(x, y, z)$, here presumed given may be combined with a three-dimensional (3-D) ocean circulation and mixing model that may in turn be coupled to a highly resolved weather prediction model. These comprehensive, coupled air-sea models can be used to make detailed forecasts of specific storms (Ginis, 2002; Bender et al., 2007; Chen et al., 2007; Halliwell et al., 2008) and will soon be a primary forecast tool in some weather centers. Existing weather prediction models now make reasonably good forecasts of a hurricane track (Marks et al., 1998), which is dependent mainly upon the surrounding, large-scale wind field. The intensity of a given hurricane is by comparison much more difficult to forecast reliably, and, as suggested above, is likely to be dependent in part upon interaction between the hurricane and the underlying ocean.

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The emphasis of this paper will be mainly upon ocean models at the other extreme of complexity, in which the same initial ocean data and an understanding of the salient ocean mixing and thermodynamics are combined into a metric (DeMaria et al., 2005),

\[ M(x, y) = F(T_i(x, y, z), \ldots) \]  

that, with appropriate interpretation, provides forecast guidance regarding hurricane-ocean interaction. The function \( F \), which is the object of this paper, evaluates, integrates or averages over depth, \( z \), to yield a two-dimensional, mappable variable, or metric. The ellipsis indicates that more than the thermal field alone is likely to be relevant. For any specific forecast, a forecast hurricane track is presumed to be available, and thus the relevant position(s) \((x, y)\) are presumed known.

One metric of this sort is the initial sea surface temperature,

\[ SST_i(x, y) = T_i(x, y, z = 0). \]  

It is well known that \( SST_i \geq 26^\circ C \) is a necessary condition for the formation of hurricanes (Miller, 1958; Tonkin et al., 2000 and references therein). Of course, we don’t need (1) to help us find \( SST \), but \( SST_i \) is almost certainly not the entire story.
for hurricane-ocean interaction. It was noted at the beginning that SST cools significantly during a hurricane passage. Closely related is that SST is likely to be representative of only the upper few tens of meters of the water column and it is expected that hurricanes will interact with (very roughly) the upper 100 m of the ocean. The physical mechanism(s) of hurricane-ocean interaction and the depth over which interaction is appreciable are among the central issues for determining an appropriate $F$.

1.2 Upper Ocean Heat Content, an integral of the ocean temperature

The first ocean metric that took account of the subsurface ocean temperature, called upper Ocean Heat Content (OHC), was written down by Leipper and Volgenau (1972) almost forty years ago

$$\text{OHC}(x, y) = \rho_0 C_p \int_{Z_{26}}^{0} (T_i(x, y, z) - 26)dz,$$

and is today widely used in operational, hurricane forecasting (Goni and Trinanes, 2003; DeMaria et al., 2005; and see especially the informative, recent review by Mainelli et al., 2008). The leading factors, $\rho_0=1025$ kg m$^{-3}$ and $C_p=4.0 \times 10^3$ J kg$^{-1}$°C$^{-1}$ are sea water density and heat capacity and the lower limit of integration for OHC is the depth of the 26°C isotherm, $Z_{26}$. The reference temperature, 26°C, is an average (dry bulb) temperature in the subtropical atmospheric boundary layer and so $T_i(x, y, z=0)−26$ is a measure of the thermal disequilibrium between the atmosphere and the initial state of the ocean. Aside from $\rho_0$ and $C_p$, which are effectively constants, OHC has an obvious interpretation as how much (temperature $\times$ thickness) ocean temperature at a given $(x, y)$ exceeds the reference temperature, 26°C, and expressed as a heat content. Notice that in the usual case that ocean temperature is monotonically increasing toward the surface, water having a temperature less than 26°C will make no contribution to OHC. A consequence is that OHC can not show how far below the reference temperature the ocean temperature may be, an issue that arises in Sect. 3.1.2.$^1$

$^1$The quantity defined by Eq. (3) has also been called hurricane heat potential (Leipper and Volgenau, 1972), and tropical cyclone heat potential (Goni and Trinanes, 2003). To the extent that “heat content” implies conservation properties, these might be better names (and see Warren (2006) on this common usage of “heat”). Conservation issues are of two kinds, roughly thermodynamic and fluid dynamic. OHC is not conserved under mixing because of changes in density and heat capacity. These errors are very small in the present context, but can be almost completely avoided by use of potential enthalpy (McDougall, 2003). A much bigger conservation error may arise from the lower limit of integration for OHC, the depth of the 26°C isotherm, $Z_{26}$. In the presence of vertical mixing near $Z_{26}$, which occurs commonly (Fig. 1b and c, and D’Asaro et al., 2007), this lower limit is not a material surface whose motion would be connected by continuity with the surrounding fluid. To appreciate the consequence, imagine that vertical mixing within the ocean surface layer (no hurricane-ocean heat flux) acts to cool the surface layer, eventually below 26°C. OHC will vanish as the surface layer cools below 26°C and the depth $Z_{26}$ moves upward through the sea surface. This decrease of OHC in a given column is not necessarily balanced by a gain at some other location in the domain; OHC may simply disappear as a result of sufficient vertical mixing and cooling of the surface layer. This non-conservation is not at issue for the interpretation of any single map of OHC, but it can be pernicious when OHC is used in an analysis. For example, estimates of time-changing (usually decreasing) OHC during a hurricane passage may lead to overestimates of the magnitude of the inferred hurricane-ocean heat exchange, even if vertical and horizontal advection are accounted appropriately. The phrase “upper ocean heat content” has also been used in large-scale ocean climate contexts to mean the temperature integral over the (fixed) upper 750 m of the ocean (Willis et al., 2004).
OHC takes on the largest values, $\text{OHC} \geq 100 \, \text{kJ cm}^{-2}$, over oceanic regions having a comparatively warm, thick surface layer, often in association with a subtropical gyre interior or an associated western boundary current system, the Kuroshio or the Gulf of Mexico’s Loop Current (Shay et al., 2000; Halliwell et al., 2008) being important examples. A significant correlation between these high OHC features and hurricane intensification has been found in late summer conditions in which the pre-hurricane SST field is often quasi-uniform horizontally (Figs. 2 and 3). Extensive testing and forecasting experience has thus shown that high range OHC, roughly $\text{OHC} \geq 60 \, \text{kJ cm}^{-2}$, provides significant information on the ocean thermal field beyond that provided by the SST field alone (Goni and Trinanes, 2003; Scharoo et al., 2006; McTaggart-Cowan et al., 2007; Lin et al., 2008; Mainelli et al., 2008; see also Sun et al., 2006).

There are also observations that do not fit comfortably within an OHC framework. At one level anomalies are not surprising; ocean thermal conditions, no matter how they are represented, are not the sole nor necessarily the most important determinant of hurricane intensity. Large-scale wind and humidity distributions are at least as important, and internal variability occurs within hurricanes on small spatial and time scales that are very difficult to predict (Marks et al., 1998). One notable, apparent anomaly has real consequences for forecasting, viz., the correlation between hurricane intensity and high range OHC noted above disappears within the low range of OHC, $0 \leq \text{OHC} \leq 60 \, \text{kJ cm}^{-2}$. Thus, while high values of OHC are found to favor hurricane intensification, low values of OHC are found to have no significant, consistent effect, either positive or negative. Low range OHC is therefore excluded from some forecast and analysis schemes (Mainelli et al., 2008). This loss of correlation between hurricane intensity and low range OHC is considered in some detail in Sects. 3.1.2 and 3.2.1. The upshot will be that OHC does not bear a consistent relationship to SST in cool, deep ocean conditions or in shallow water and so OHC would not be expected to be a useful metric in those common conditions. To be fair to Leipper and Volgenau (1972), this critique amounts to applying OHC outside of the warm, deep ocean conditions that they envisioned. However, maps of OHC (Goni and Trinanes, 2003) and statistical analyses using OHC as the ocean metric (DeMaria et al., 2005; Mainelli et al., 2008) necessarily include all oceanic regions where hurricanes occur, and not excluding regions with small or vanishing OHC. Thus...
the parameter space of cool SST and shallow water is unavoidable in a discussion of ocean metrics that are intended for more than a qualitative interpretation, the intent here.

1.3 The goal and the plan of this paper

The object of the present work is a new, rationalized ocean metric for use within a hurricane-ocean forecasting or analysis scheme. The scope of this paper is limited to the ocean half of hurricane-ocean interaction, and the approach will be to build upon the extensive history of OHC reviewed above, while also making use of 3-D ocean models and guidance from ocean process field studies that were unavailable when OHC was proposed. The starting point is a review of the mechanisms that cause sea surface cooling during a hurricane passage, Sect. 2.1. This leads to the hypothesis that a vertical average of upper ocean temperature is a more relevant metric than is OHC, a vertical integral of ocean temperature, Sect. 2.2. The consequences of averaging vis-a-vis integrating are explored in Sect. 3; Sect. 3.1 considers the deep, open ocean, and Sect. 3.2 considers a continental shelf. A summary of the present results and remarks on future research are in the concluding Sect. 4.

2 The oceanic mechanisms of hurricane-ocean interaction

Heat content is not a substance that is transferred from the ocean into the atmosphere simply by contact. And specifically, high OHC does not by itself insure that there will be a high heat flux from the ocean into a hurricane. A thermal disequilibrium (temperature and humidity difference) between the sea surface and the lower atmosphere must be involved as an intermediary, and all else equal, the larger this disequilibrium, the larger the heat flux. The oceanic part of this is the SST. The route to a new ocean metric begins from this point of view and then requires just three premises. Premise 1, which more or less summarizes the point made just above, is that

P1: The relevant oceanic property for hurricane-ocean interaction is SST and especially the SST underneath a hurricane.

Subsurface ocean temperature (and by extension, OHC) may be very important indirectly, but only to the extent that it effects the SST. The SST underneath a hurricane is singled out in P1 because it corresponds with the high wind speed, central region of a hurricane and thus the greatest potential for heat exchange (Cione and Uhlhorn, 2003). (P1 seems to elide a role for the other important property of the sea surface, sea state, out of ignorance rather than conviction.) The second premise follows closely on P1.

P2: An oceanic region will be regarded as favorable for hurricane intensification if the initial SST is high and if the SST remains high during a hurricane passage.

SST should be considered high or low with respect to the atmosphere just above; absent specific observations, 26°C is a reasonable reference. Assuming that the initial temperature field \( T_i(x, y, z) \) is given, then the oceanic part of hurricane-ocean forecasting amounts to predicting the cooling of SST that occurs under a hurricane (taking the hurricane perspective, as is implicit in Fig. 1a) or during a hurricane passage (from the ocean perspective, Fig. 1c).

2.1 Sea surface cooling mechanisms

The sea surface underneath a hurricane is cooled by two distinct mechanisms – by hurricane-ocean heat exchange noted above, and by vertical, turbulent mixing of cooler water upward into the surface layer (Price, 1981; Jacob et al., 2000; D’Asaro et al., 2007). If the hurricane-induced sea surface cooling noted above was due mainly to heat exchange, then OHC would be an appropriate metric for representing the ocean thermal field. However, two lines of evidence appear to suggest otherwise. Leipper and Volgenau (1972) noted that the large values of OHC found over much of the deep, subtropical oceans are far in excess of the time-integrated heat flux to a given hurricane, often by a factor of 10 or more (noted also by Cione and Uhlhorn, 2003 and by Mainelli et al., 2008). In a later Sect. 3.2, the time-integrated (net) heat flux (sum of latent and sensible fluxes) to a single hurricane is estimated as \( Q_{\text{net}} \approx 5 \times 10^7 \text{ J m}^{-2} = 5 \text{ kJ cm}^{-2} \) (Fig. 5). This net heat flux will cool a water column that is 100 m thick by about only about 0.12°C, and a 10 m-thick column by about 1.2°C (Fig. 5). Thus, even a rather shallow, warm continental shelf will have greater heat content, as estimated by OHC, than will be absorbed by a single hurricane. On this basis alone it seems unlikely that OHC per se sets a significant limit on hurricane-ocean interaction (aside from the case of very shallow water environments). This does not preclude that OHC may nevertheless serve as an effective metric for the ocean thermal field in some specific conditions, viz., the warm, deep ocean conditions emphasized by Leipper and Volgenau (1972) (Sect. 3.1.1).

A number of subsequent, upper ocean field studies and model studies have found that the primary mechanism that cools the sea surface during a hurricane passage is turbulent, vertical (diapycnal) mixing (Price, 1981; Bender et al., 1993; Jacob et al., 2000; Sanford et al., 2007; D’Asaro et al., 2007). The evidence of this is that the sea surface may cool significantly without there being an appreciable change in the upper ocean heat content (suitably chosen, footnote 1). The temperature profiles of Fig. 1d are an example; during the passage of Hurricane Frances (2004) the surface temperature cooled by about 2.3°C as the temperature profile became quasi-homogeneous over very roughly the upper 100 m. A comparison of pre- and post-hurricane temperature profiles
shows that the net cooling (temperature change times thickness) caused by vertical mixing within the upper ocean is approximately equal in magnitude to the net warming caused by vertical mixing in the upper thermocline (this warming is not of direct interest here, but may have relevance over climate time scales, see Sriver and Huber, 2008). Detailed studies of the upper ocean heat budget have found that the ratio of the heat flux due to vertical mixing compared to the hurricane-ocean heat exchange is O(10) in deep water cases (Jacob et al., 2000; Cione and Uhlhorn, 2003; D’Asaro et al., 2007), consistent with the observations noted above. The principle mechanism on the ocean side of hurricane-ocean interaction can then be summarized in Premise 3 – while hurricane-ocean heat exchange is O(10) in deep water cases, the much smaller, darker shaded area near the surface in (a) is proportional to an estimate of the net hurricane-ocean heat exchange, \( Q_{h} \approx 5 \, \text{kJ cm}^{-2} \) (Sect. 3.2.2). The dashed line labeled \( T_{\text{100}} \) is the temperature profile after vertical mixing to a depth of 100 m, a typical depth of mixing by a category 3 hurricane (Sect. 2.2.1). Note that mixing to 100 m cools the sea surface of profile (a) by only about 1.5°C because the water that was mixed upward into the surface layer was only slightly cooler than the water present above \( z = -100 \) m. Either ocean metric, OHC or \( T_{\text{100}} \), would indicate that temperature profile (a) is favorable for hurricane intensification. In profile (b), the cooling effect of the same vertical mixing is much greater, \( \approx 5 \)°C, and notice that OHC is also much smaller; both ocean metrics would indicate that profile (b) is not favorable (or comparatively less favorable) for intensification than is profile (a). The dotted lines labeled \( T_{7} \) are the temperature profiles after vertical mixing from the surface to a depth of \( d = 120 \) m (a) or \( d = 85 \) m (b) (why these depths are discussed in Sect. 2.2.2). (c) and (d) The profiles from (a) and (b) but with a shallow bottom indicated at (arbitrarily) 25 m; discussed in Sects. 3.2 and 4.1.

P3: The large amplitude, 1–4° C, cooling of the sea surface that occurs during a hurricane passage is due mainly to vertical mixing of cooler water into the ocean surface layer.

2.2 A new ocean metric, depth-averaged temperature

Given P1–P3, it follows that a metric intended to represent the ocean thermal field should account first of all for the sea surface cooling effect of vertical mixing (caused mainly by the very high winds of a hurricane) and only secondarily for hurricane-ocean heat exchange. Vertical mixing is equivalent to vertical averaging, and this leads to the hypothesis advanced in this paper:

\[ T_{\sigma}(x, y) = \frac{1}{d} \int_{-d}^{0} T_{i}(x, y, z) \, dz, \]

where \( d \) is the depth of vertical mixing caused by a hurricane, i.e., the surface mixed-layer thickness.

The depth \( d \) has to be predicted or specified if \( T_{\sigma} \) is to be predicted, and two methods for doing that are discussed below. If, as will be presumed here, \( d \) is evaluated in the wake of a hurricane, then the resulting depth-averaged temperature, \( T_{\sigma} \), is an estimate of the mixed-layer temperature in the wake.

Given that SST decreases during a hurricane passage, the interpretation of \( T_{\sigma} \) is straightforward. High values of \( T_{\sigma} \), say \( T_{\sigma} \geq 28^\circ C \), would indicate even slightly higher SST during a hurricane passage and thus an ocean thermal field that is favorable for hurricane intensification (on the basis that SST remains several degrees above 26°C). On the other hand, low
values, say \( T_\beta \geq 24^\circ C \), would indicate low values of SST during a hurricane passage, and so an ocean thermal field that was comparatively unfavorable (or much less favorable) for intensification.

The dependence of sea surface cooling upon upper ocean stratification is the key property of a depth-averaged temperature metric. For example, if there is a comparatively small temperature (vertical) contrast in the water column above \( z = -d \) that is mixed vertically, as in profile (a) of Fig. 5, then vertical mixing will cause comparatively little cooling of the sea surface. If the ocean bottom is shallow and the bottom temperature is warm (Fig. 5c) then, perforce, vertical mixing will cause very little cooling of the sea surface.

The issue now turns to estimation or prediction of \( d \). At some risk of confusion there are two versions of \( d \) suggested here. The first is a very simple, empirical, fixed-\( d \) version that is based upon the CBLAST field observations of Fig. 1c and Fig. 1d and that serves the most important purpose of this paper – to contrast integrated and averaged ocean temperatures. There follows a more complex and more capable variable-\( d \) version that takes account of the spatially-variable density stratification of the initial ocean and allows for stronger or weaker hurricanes. This variable-\( d \) version is better suited for forecasting purposes.

### 2.2.1 Fixed depth, \( d=100 \text{ m} \) and \( T_{100} \)

The simplest, plausible version of \( d \) is to take a fixed value, \( d=100 \text{ m} \), or to the ocean bottom, if that is shallower. The choice \( d=100 \text{ m} \) is admittedly a round number, but is consistent with the observed depth of vertical mixing under Hurricane Frances (2004) (Sanford et al., 2007): radius to maximum winds, \( R_0 \) (35 km), translation speed, \( U_h \) (5.5 m s\(^{-1} \)), and the maximum wind stress, \( \tau \) (5.5 Pa). A variable-\( d \) metric also requires a parameterization to connect vertical, turbulent mixing in the upper ocean with the hurricane forcing. The parameterization applied here is that the bulk Richardson number of the surface mixed-layer should not be less than a critical value, \( C=0.6 \) (Price, 1981),

\[
g \frac{\delta \rho \theta}{\rho_0 (\delta U)^2} \geq C
\]

or,

\[
g \left[ \rho(z = -d) - \frac{\partial}{\partial z} \int_{-d}^{0} \rho(z) dz \right] \frac{d}{\rho_0 (\tau / \rho_0 d) S^2} \geq 0.6,
\]

where \( g \) is the acceleration of gravity. The operator \( \delta \) takes the difference between the surface mixed-layer and the value just below, as if there was a jump in density and velocity. The wind-driven current that appears in the denominator of the Richardson number, \( \delta U / \rho_0 \), has been estimated as the product of the wind stress-induced acceleration, \( = \tau / \rho_0 d \), and the hurricane residence time, \( 4R_h / U_h \). The effects of Earth’s rotation and the rotation in time of hurricane wind stress are not treated explicitly. An ad hoc similarity “constant” \( S \) is therefore required to calibrate this scale estimate with 3-D numerical ocean model solutions made with a two-dimensional, translating hurricane wind stress field. The value of \( S \) depends upon the cross-track coordinate, \( y \). In keeping with the decision to estimate the maximum mixing and cooling, \( S \) is evaluated at \( y=55 \text{ km} \) to the right of the track of Hurricane Frances (see Fig. 4 of Sanford et al., 2007) and is \( S=1.2 \). For comparison, at 55 km to the left of the track, \( S=0.4 \). This right-to-left variation of \( S \) reflects the partial resonance of the rotating wind and wind-driven current on the right side of a hurricane track compared with the left. This calibration of \( S \) is the first, specific way in which a 3-dimensional numerical ocean model has been used to develop an ocean metric. A second way is that the many simplifications inherent in this
variable-$d$ metric – omission of all advection, pressure gradients and air-sea heat exchange, the specific value of $S$ – can be checked by comparing the resulting depth-averaged temperature, $T_d$, against much more comprehensive, 3-D numerical ocean model solutions. The comparison is generally favorable, though with some reservations about the low $U_h$ limit (for details see the Supplementary Material noted at the end of this manuscript).

Given a density profile that is discretized at intervals $\Delta z$, Eq. (5) can be solved very quickly. The left hand side (lhs) of is evaluated with $d=n\Delta z$ from the surface downwards, i.e., with $n$ increasing from 1. The lhs starts with very low values, and is a monotonically increasing function of $n$ (assuming that density increases with depth). The equation is considered solved for $d$ when $\text{lhs} \geq C$, or when $n\Delta z=b$, where $b$ is the bottom depth and mixing is of course terminated. Once Eq. (5) has been solved for $d$, the corresponding depth-averaged temperature, $T_d$, is then estimated by the vertical average, Eq. (4), evaluated over the given initial temperature profile, $T_i$ (from here on $d$ and $T_d$ have this specific meaning). (The Matlab script used to evaluate $d$ and $T_d$ on this Argo data is included in the Supplementary Material available online.)

Notice that the denominator of the Richardson number, Eq. 5, depends only upon hurricane parameters that are presumed known and would presumably be fixed for the evaluation of a given map. The numerator depends only upon the pre-hurricane ocean density profile and will likely vary regionally. The regional variation in a map of $T_{100}$ or $T_d$ (Fig. 4) thus reflects the regional variation of the ocean temperature and salinity (density) field and, where mixing reaches the bottom, the bottom depth.

3 The comparative geography of OHC, $T_{100}$ and $T_d$

On first sight, the prescription for a depth-averaged temperature via Eq. (4) and the heat content computed via Eq. (3) do not look at all that different, and in important and common circumstances (summer, subtropical, deep ocean) they will give essentially the same forecast guidance. In other circumstances they may be quite different. A corollary of H1 is that a depth-averaged temperature will make a useful ocean metric over a much wider range of conditions than does OHC, a depth-integrated temperature. A full test of this important corollary is beyond the scope of this paper. What we can do here usefully is learn where and how OHC and the depth-averaged temperature will differ. To this end, both kinds of metrics have been evaluated using observations from the deep, open ocean (Sect. 3.1) and from an idealized continental shelf (Sect. 3.2). Salinity effects are then noted very briefly in Sect. 3.3.

3.1 The deep ocean

Two open ocean regions were considered; the first was a 20 by 20 degree region of the western subtropical North Pacific centered on 20°N and 130°E that was studied by Lin et al. (2008). The available Argo temperature and salinity profiles were acquired for the months July through October of 2007 (846 profiles in total, Fig. 6a). This region spawns some of the largest and most intense hurricanes (super typhoons) found anywhere in the world, and it is also a region having quite pronounced variability of the ocean mesoscale (Qiu, 1999). Eddies having a diameter of several hundred kilometers and sea surface height anomalies of ±20 cm are common. These mesoscale eddies are accompanied by a raised or depressed thermocline (Fig. 5) and thus by substantial variations of OHC and $T_{100}$ that are not reflected in sea surface temperature (Fig. 6b, and compare Figs. 2 and 3 and Figs. 2 and 4). As noted already, Lin et al. (2008) found that the intensification of the most intense super typhoons is spatially correlated (coincident) with warm eddies (depressed thermocline) that show up as regions of especially high OHC (see Halliwell et al., 2008 for a discussion of mesoscale variability in the Gulf of Mexico).

The second open ocean region considered here was the equivalent from the western North Atlantic, 10–30°N, and 280–320°W and for the same months of 2007. These North Atlantic data (and a few profiles from the Caribbean Sea, 697 profiles total) are almost indistinguishable from the North Pacific data, the only difference being fewer points in the range of very large OHC (Fig. 6c and d). Within both data sets there are no doubt many profiles that were significantly affected by a typhoon or a hurricane. There was no attempt to sort these out, and all of the Argo profile data were treated as if they were initial data for the next storm.

Over these deep, open ocean regions, $T_{100}$ and $T_d$ are highly correlated and approximately equal (Fig. 7a and c). This means only that $d=100\text{m}$ is not a bad approximation to the variable $d$ computed from Eq. (5) for each profile and for a typical category 3–4 hurricane. Nevertheless there is some variation of the estimated $d$ within this sample: $d$ was as large as 135 m on the most weakly stratified profiles (profile (a) of Fig. 5), and so $T_d$ is slightly cooler than $T_{100}$ in the range of cool temperatures; $d$ was as small as 85 m on the profiles that are most strongly stratified (profile (b) of Fig. 5), but the resulting $T_d$ are not greatly different from the fixed-depth version, $T_{100}$. We note here and again in Section 3.3 that this may not be the case in regions where salinity makes an appreciable contribution to the static stability of the upper ocean, and it would certainly not be the case if the storm of interest was a developing tropical depression vs. Hurricane Frances (2004).
3.1.1 Warm oceans and the high range of OHC

Both of the depth-averaged temperatures are closely related to OHC in the high range of $T_{100}, T_{100} \geq 27^\circ$C and OHC, OHC $\geq 75$ kJ cm$^{-2}$ (Fig. 7b and d). It is not surprising that an especially warm, thick surface layer will indicate high values of OHC, $T_{100}$ and $T_d$ alike. What is not obvious is that the relationship between high range OHC and high $T_{100}$ appears to be very tight, bijective (one to one), and nearly identical in the western North Pacific and western North Atlantic. Within a given map, the contour lines of high $T_{100}$ are essentially parallel with contour lines of high OHC (compare Figs. 3 and 4 over the subtropical gyre). Thus, high values of $T_{100}$ are expected to bear the same qualitative, spatial correlation with hurricane intensification as do high values of OHC (Lin et al., 2008; Shay et al., 2000; Mainelli et al., 2008). A depth-averaged temperature, either $T_{100}$ or $T_d$, thus repeats the most useful, demonstrated property of OHC, i.e., high values of $T_{100}$, roughly $T_{100} \geq 27^\circ$C, will identify open ocean regions where the thermal field is especially favorable for hurricane intensification. This was not accommodated after the fact, but follows straightforwardly from the definition of a depth-averaged temperature, Eq. (4), and the empirical relation between high range OHC and $T_{100}$ seen in these data (Fig. 7b and d).

Indeed, the relation between high-range OHC and $T_{100}$ is so tight that if only warm, deep ocean conditions were relevant, then there would be very little practical motive to...
continue on (though in light of P1 and P2 we might still ask why there is a correlation between high OHC and hurricane intensification). As discussed in Sect. 3.2, there may be shallow water regions that are equally favorable for hurricane intensification as assessed by a depth-averaged temperature, and yet that have comparatively low OHC. Cool, deep ocean regions are also relevant and interesting.

3.1.2 Cooler oceans and the low range of OHC

OHC and $T_{100}$ are not closely related in the range of low OHC, OHC $\leq 50 \text{kJ cm}^{-2}$ and low temperatures, $T_{100} \leq 26.5^\circ \text{C}$ (Fig. 7b and d). As noted in Sect. 1.1, neither is there a statistical correlation between hurricane intensity and OHC within this low range of OHC (Lin et al., 2008; Mainelli et al., 2008). This loss of correlation is somewhat puzzling because it has been observed that hurricanes are significantly damped by a sufficiently cool SST (Monaldo et al., 1997; Walker et al., 2005). On the face of it then, an ocean
thermal metric would be expected to have a low range within which hurricane intensity is damped.

A partial resolution of this low OHC puzzle may be as close at hand as P1 and Eq. (3). And specifically, the loss of the tight relationship between high range OHC and the depth-averaged temperatures results in part from a slightly peculiar property built into OHC, i.e., that all ocean temperatures less than the reference temperature 26°C are treated the same, effectively as zero. For example, if the temperature of the entire water column was 0°C, then the estimated OHC would be zero, and if the temperature of the entire water column was 26°C, then the OHC would again be exactly zero. Thus, insofar as OHC is concerned, T=0 and T=26°C are one and the same. As a consequence, roughly a third of the open ocean temperature profiles considered here (Fig. 7) map into one point in OHC-space, OHC=0, which might be termed a cool degeneracy. In maps of OHC, this cool degeneracy appears as broad regions that are at or near zero and so horizontally uniform. There is just a hint of this cool degeneracy along the northern boundary of the North Pacific OHC map computed in late September (Fig. 3) and it becomes quite prominent once seasonal cooling has developed in late October (see Goni and Trinanes (2003) and http://www.aoml.noaa.gov/phod/cyclone/data/go.html for examples).

In Sect. 1 it was noted that the reference temperature of OHC, 26°C, had a significant empirical basis. But whether there is a literal cutoff in hurricane-ocean interaction for SST≤26°C as occurs with OHC seems unlikely, if only because the dew point temperature of the hurricane lower atmosphere is typically a few °C less than the air temperature, and so some latent heat flux would be expected even for SST≤26°C. What appears to be certain is that OHC defined by Eq. (3) will have poor (or no) resolution in regions where the upper ocean temperature is less than 26°C and hence OHC could not be expected to provide a nuanced account of the possible damping effect of still lower SST. This limitation of OHC is not shared by a depth-averaged temperature, which can always be referenced to 24 or 26°C. For example, maps of \(T_{100} \rightarrow 26\) or \((T_i + T_{100})/2 \rightarrow 26\) (discussed in Sect. 4.3) would give a much more vivid impression of a warm or cool sea surface than does \(T_{100}\) alone.

3.2 The coastal ocean

OHC and the depth-averaged temperatures can be quite different when evaluated over shallow water regions. The consequence for forecasts of hurricane-ocean interaction may be more or less significant depending upon the extent of the shallow water area affected and the relationship of a hurricane track to the coastline (incidence angle). The shallow water limit is of interest in the present context because it clearly shows the difference between integrating and averaging. The shallow water limit is of considerable practical importance for hurricane forecasting since it occurs in conjunction with hurricane land fall.

To illustrate the effects of bottom depth, OHC and \(T_7\) were evaluated over an idealized continental shelf that was constructed along the lines of the West Florida Continental Shelf (Fig. 8a). The bottom slope was taken to be \(\partial b/\partial x = 10^{-3}\) and constant, with \(b\) the bottom depth, and \(x\) the across-shelf coordinate. The hydrography of continental shelves varies a great deal from region to region and on a given shelf with time (Allen et al., 1983) with important consequences for what follows. But given that the goal here is to illustrate bottom depth effects alone, the thermocline was presumed to be level so that \(T_i(x, y, z) = T_i(z)\) and horizontally homogeneous for \(z \gtrless -b(x)\). i.e., upwelling neutral. The temperature profile \(T_i(z)\) was taken from the West Florida Shelf in summer (Hu and Muller-Karger, 2007) and had a warm and quasi-uniform surface layer about 25 m thick, and a comparatively large vertical gradient of temperature, 0.15°C m⁻¹, within the seasonal thermocline. This kind of shallow, strongly stable seasonal thermocline is typical of subtropical shelf regions that are not directly influenced by deep ocean currents, e.g., the South and Middle Atlantic Bights (Schofield et al., 2008), if not impacted by Gulf Stream-derived eddies, or the shelf regions along the northern Gulf of Mexico, aside from Loop Current eddies. The metrics OHC and \(T_7\) were then sampled along a transect across the shelf (Fig. 8b and c).

3.2.1 Coastal ocean OHC

To evaluate OHC over shallow waters in which the bottom temperature exceeds 26°C, the lower limit of integration was presumed to be the bottom depth, \(b\). Given this specific shelf and hydrography, the estimated OHC begins to decrease as the bottom depth becomes less than the depth of the 26°C isotherm, which is about 50 m in the temperature profile presumed here (Fig. 8b). Assuming a consistent deep-ocean and coastal-ocean interpretation of OHC, i.e., that regions having OHC ≤50 kJ cm⁻² are not favorable for hurricane intensification (or at least less so than high OHC regions), then according to OHC, a shallow continental shelf would appear to be an unfavorable environment for hurricane intensification.

This simple example of a coastal ocean shows that OHC can vanish in two important, realizable limits: 1) over the deep ocean as \(T \rightarrow 26°C\) from above, and discussed in the previous section, and, 2) over a coastal ocean as \(b \rightarrow 0\) and regardless of the ocean temperature. If the underlying issue for hurricane-ocean interaction is SST rather than OHC per se, as we have argued it must be in P1 and P2 of Sect. 2, then it appears that OHC suffers from a second kind of degeneracy in shallow water in that very low values of OHC will be estimated in shallow-enough water even if the ocean temperature is high. Said a little differently, low values of OHC in a coastal ocean are not expected to have the same consequence for hurricane-ocean interaction as do low values of
isobath (Fig. 8c) follows from the increase of bottom temperature with decreasing bottom depth, i.e., there is less cold water available to be mixed upwards. This can be expected over a shelf on which the seasonal thermocline intersects the bottom, i.e., over shelves that are either upwelling neutral or negative, but not on shelves that are upwelling positive. The end result for an upwelling neutral shelf is that the across-shelf temperature profile $T(x)$ exhibits what might be termed a Coastal Warm boundary Layer (CWL), whose half-width may be estimated roughly as

$$W_{CWL} \approx \frac{1}{2} \frac{d_{do}}{\frac{\partial b}{\partial x}},$$

and in this case, $W_{CWL} \approx 42$ km.

An inner-coastal cool layer. Heat loss to the hurricane must become a significant process for sea surface cooling where the water is shallow enough (Shen and Ginis, 2003). To account approximately for this hurricane-ocean heat exchange, the depth-averaged temperature $T_d$ can be perturbed by subtracting a typical net hurricane-ocean heat flux, $Q_{net}$, from the water column. $Q_{net}$ is estimated from the numerical simulation of the Frances (2004) case by Sanford et al. (2007) by integrating the latent and sensible heat fluxes over a period of one day centered on the hurricane passage, $Q_{net} \approx 5 \times 10^7$ J m$^{-2}$, or in the non-SI units often used for OHC, $Q_{net} \approx 5$ kJ cm$^{-2}$. This estimate appears to be at least roughly consistent with the heat fluxes estimated by Chen et al. (2007) for the Frances (2004) case, and by Cione and Uhlhorn (2003) for other hurricanes. The revised depth-averaged temperature that takes account of this heat loss, $T_d - Q_{net}/\rho_o C_p b$, where $b$ is the water depth, is shown as the dashed line of Fig. 8c. The resulting Inner-Coastal Cool boundary Layer (ICCL), follows the qualitative expectations of OHC in the sense that the cooling is inversely related to water depth, $b$. The width of this cool layer may be estimated roughly as the region where the temperature is decreased by say $\Delta T = 1^\circ$C or more,

$$W_{ICCL} \approx \frac{Q_{net}}{\rho_o C_p \Delta T/\frac{\partial b}{\partial x}},$$

and in this case, $W_{ICCL} \approx 12$ km.

Thus the post-hurricane coastal ocean sea surface temperature computed by the $T_d$ model may show two boundary layers when compared to the outlying and otherwise similar deep ocean — a coastal warm layer (CWL, and warm compared to the outlying deep ocean) in which the characteristic process is a reduced heat flux associated with vertical mixing, and an inner-coastal cool layer (cool compared to the warm layer), in which hurricane ocean heat exchange is important. This ICCL follows the expectations implicit to OHC, and a comparison of the amplitude and width of the ICCL and the CWL gives a visual impression of the relative importance of vertical mixing and hurricane-ocean heat exchange, insofar as the SST over a continental shelf is concerned. Given the upwelling neutral shelf considered here, the outer warm layer

OHC over the deep ocean. The combined effect of this cool and shallow water degeneracy is thought to be a part of the reason that OHC does not show a correlation with hurricane intensification in the low range of OHC.

### 3.2.2 Coastal ocean $T_d$

A coastal warm layer. Given the shelf topography and stratification presumed here, the depth-averaged temperature $T_d$ increases as the bottom depth becomes less than $d_{do} = 85$ m, the depth of mixing over the deep ocean given this rather stable stratification. The increase of $T_d$ shoreward of the 85 m
is considerably wider than the inner cool layer. For typical bottom slopes and heat loss values,

\[ \frac{W_{\text{CWL}}}{W_{\text{ICCL}}} = \frac{d_{do}/2}{Q_{\text{net}}/p_0 C_p \Delta T} \approx 3.5 \quad (8) \]

### 3.2.3 Applications and coastal ocean observations

The maps of Figs. 3 and 4 show \( T_{100} \) and OHC evaluated over the broad, shallow continental shelf off of the south and east coast of China (South China Sea north to the Yellow Sea). These are depicted as regions of generally low OHC, \(<40 \text{kJ cm}^{-2}\), despite having fairly high SST, simply because they are shallow. In contrast, the estimated depth-averaged temperature (Fig. 4 is \( T_{100} \) which has the same relation to bottom depth as does \( T_\gamma \)) indicates that these shelf regions are likely to remain fairly warm during a hurricane passage by virtue of the CWL phenomenon. Hence on our P3 (Sect. 2.1) these shelf regions appear to be somewhat favorable for hurricane intensification, as seen in a depth-averaged temperature \( T_{100} \geq 27^\circ \text{C} \). Some of the affected shelf regions are as wide as several hundred kilometers and likely to be of significance for hurricane-ocean interaction, or at least for our prediction of hurricane-ocean interaction. Other shelf regions appear nearly the same when diagnosed with OHC or \( T_{100} \), notably east of the Phillippines, where the continental shelf is quite narrow. To summarize, the distribution of \( T_{100} \) indicates that some coastal oceans – those having broad, shallow continental shelves and hydrography that is upwelling neutral or negative – are expected to remain warm during a hurricane passage, and in that regard would appear to be favorable environments for hurricane intensification. This is a result at odds with a consistent deep-ocean/shallow-water interpretation of OHC.

As hurricanes cross a continental shelf they are also likely to be making land fall, which is usually expected to cause a rapid and significant decrease of hurricane intensity (but see McTaggart-Cowen et al. (2007) who note that this is not necessarily the case if the land surface is flat, warm and wet, e.g., South Florida). However, our concern here is exclusively with the ocean thermal field, and some evidence is that shallow water environments may indeed be favorable for hurricane intensification in the sense that hurricane-induced sea surface cooling has been observed to be reduced over shallow water regions compared to the cooling over outlying, deep water regions. Hazelworth (1968) analyzed the time series data from weather ships for hurricane passages and made a very brief and tentative mention of such a shallow water effect. The first explicit report was evidently made by Cornillon et al. (1987), and more recently this phenomenon has been observed on the West Florida Continental Shelf by Hu and Muller-Karger (2003). The latter two studies inferred that the principal cause of the reduced sea surface cooling over shallow water was the absence of cool water at depths that could be mixed into the surface layer, just as happens here with the depth-averaged temperature. Emanuel (1999) noted the relevance of this shallow water effect in the context of hurricane-ocean interaction.\(^2\)

### 3.3 Salt-stratified water column

In the event that salinity makes an important contribution to the upper ocean density stratification, then \( T_\gamma \) can, in principle, differ from both OHC and \( T_{100} \) which acknowledge temperature only. Important salinity effects may arise where there is a comparatively fresh ocean surface layer, which often occurs in a coastal ocean, and especially down-coast from the estuary of a major river (Bingham, 2007). There are also open ocean regions in which salinity makes an appreciable contribution to the static stability of the upper ocean, e.g., the barrier layer of the western tropical Pacific and parts of the northern Indian Ocean (McPhaden et al., 2009).

If the net salinity anomaly (thickness times salinity anomaly in the initial state) is as large as about 20 m, then the fresh layer will inhibit vertical mixing significantly. The effect upon the sea surface temperature will depend upon whether the fresh layer is warmer or cooler than the water below. If the former, then salinity stratification will act to reduce the depth of vertical mixing and thus sea surface cooling. If the latter, then vertical mixing will act to increase the surface temperature (see the Nordic Sea example of Saetra et al., 2003), a possibility missing altogether from OHC, which omits any reference to salinity (or density). This anomalous surface warming effect of vertical mixing is present in \( T_{100} \) when the temperature profile has an inversion, but in general, a salinity effect upon static stability requires an explicit treatment of density, e.g., by means of \( T_\gamma \) or something more comprehensive.

### 4 Closing remarks

#### 4.1 Summary

The standard metric of the ocean thermal field within hurricane-ocean interaction is a depth-integrated ocean temperature, upper Ocean Heat Content or OHC. OHC has been shown to provide valuable forecast guidance in warm, deep ocean conditions for which it was first formulated (Leipper

\(^2\)During the summer of 2005 there were a number of intense hurricanes that crossed over the Gulf of Mexico, including Katrina (2005), which passed over the Louisiana shelf, and Wilma (2005), which passed over Florida Bay and the southern end of the West Florida shelf. SST imagery of these significant events provides some additional qualitative evidence of a coastal warm layer and sometimes a hint of an inner-coastal cool layer, though not distinct from land effects; see the collection of GOES-12 SST images in the Supplementary Material noted at the end. A comprehensive resource is the Louisiana State University Earth Scan web site, http://www.esl.lsu.edu/quicklinks/hurricanes/. Almost needless to say, attributing the cause of SST change, given only satellite images, is very uncertain.
and Volgenau, 1972; Lin et al., 2008; Mainelli et al., 2008) but the argument made here is that a depth-averaged temperature, $T_{\text{100}}$ or $T_7$, may be more appropriate over a much wider range of conditions. The argument was made on three premises: P1, that SST and especially SST under a hurricane is the directly relevant ocean variable; P2 an ocean region is favorable for hurricane intensification if SST remains high during a hurricane passage; and P3, the observation that cooling is due mainly to vertical mixing rather than to hurricane-ocean heat exchange. The hypotheses of this paper follows: H1 a depth-averaged ocean temperature is the appropriate metric (or proxy) for SST under a hurricane, and the corollary is that a depth-averaged temperature is a more robust metric of hurricane-ocean interaction than is OHC.

The majority of hurricanes and typhoons form over the deep, open ocean in late summer when sea surface temperature is warmest. In that most important circumstance, OHC and $T_{\text{100}}$ or $T_7$ will provide essentially the same forecast guidance, i.e., that an ocean region having a warm ($T \geq 26^\circ$C) and especially thick surface layer will be a favorable environment for hurricane intensification. This has been observed to hold in forecasting practice (Sect. 1.2). This observation could be taken as a warrant for the original rationale for OHC – that a high OHC region resists cooling due to hurricane-ocean heat exchange. This is true, of course, but we have argued in Sect. 2.1 that it is not highly germane. Equally, this observation could be taken as evidence in favor of $T_{\text{100}}$ or $T_7$ – that a thick, warm surface layer resists the cooling effect of vertical mixing. This latter interpretation is espoused in most recent studies (Lin et al., 2008; McTaggart-Cowen et al., 2007; Mainelli et al., 2008) and is the interpretation that is consistent with a depth-averaged temperature metric. If only warm and deep ocean conditions were relevant to hurricane-ocean interaction, then this inference of mechanisms would be of academic interest, but would hold little practical importance (Fig. 9).  

However, there are three other fairly common circumstances in which the inference of mechanism is crucially important in as much as OHC and depth-averaged temperature will give quite different forecast guidance.

**Cool, open ocean waters.** Hurricanes form over warm ($SST \geq 26^\circ$C) ocean regions, but may later move over much lower SSTs during their lifetime (a striking example is shown by Monaldo et al., 1997). The cool degeneracy built in to OHC effectively restricts its application to warm ocean conditions. The depth-averaged temperatures do not have this property, and an analysis of $T_{\text{100}}$ or $T_7$ could, in principle, permit the forecast of a damping effect of cool sea surface temperatures upon hurricane intensity.

**Salt-stratified waters.** While temperature is a sufficient proxy for density and static stability in most conditions, salinity can have a significant and sometimes decisive effect on static stability in special locations, for example within or near estuaries. OHC and $T_{\text{100}}$ are silent on salinity effects, which can be accounted by the $T_7$ metric provided that the initial salinity is known.

**Shallow waters.** OHC and the depth-averaged temperatures can be quite different when evaluated over shallow, continental shelf regions. OHC will generally indicate that shallow regions (shallower compared to the depth of the $26^\circ$C isotherm) are an unfavorable environment for hurricane intensification, while $T_{\text{100}}$ or $T_7$ may indicate the opposite, that shallow regions (shallower compared to the depth of vertical mixing in the deep ocean) can be favorable for hurricane intensification compared to an otherwise similar deep ocean (Fig. 9). To the point – this study indicates that, land effects aside, a shallow, warm continental shelf may be as favorable for hurricane intensification as is a deep, open ocean, warm regime, e.g., the Loop Current or warm eddies of the subtropical gyre interior (compare the depth averaged-profiles of Fig. 5a and c).

### 4.2 Remarks on the coastal ocean

The variation of SST with distance offshore is at once the most readily observed property of the coastal ocean and is the property of immediate interest for hurricane-ocean interaction and forecasting. It is important to appreciate that the specific relationship between SST and distance offshore shown in Fig. 8c is by no means universal because the hydrography of any given continental shelf may be quite different from the upwelling neutral case considered in Sect. 3.2. The thermal field on most continental shelves depends upon the depth and (at least) the cross-shelf coordinate, $x$, so that $T = T(x, z)$. In shelf regions that are upwelling positive, e.g., Campeche Bank or the Louisiana-Texas shelf in late summer seen as a macro version of the inner-coastal cool layer described in Sect. 3.2.2. In other words, something akin to OHC is the relevant metric for the SST response when air-sea heat exchange is the dominant physical process, i.e., the seasonal cooling of subtropical shelves but not the upper ocean response to a hurricane.
Fig. 9. (a) Dependence of OHC (thin dark blue lines) and $T_{100}$ (thicker gray lines) upon initial ocean temperature and bottom depth. The bottom slope was as in Fig. 8a. The temperature profile had a 30 m thick mixed layer and a constant vertical gradient, 0.05 °C m$^{-1}$, typical of the open ocean. The temperature was varied by subtracting a constant, 0 to 6 °C, from the entire profile. Both OHC and $T_{100}$ increase with increasing ocean temperature. Over the deep ocean and for warm temperatures, OHC and $T_{100}$ are similar (the lightly shaded, upper right quadrant). However, the dependence upon bottom depth is quite different and reflects the difference between vertically-integrating, OHC, which has a maximum at the warmest temperature and the greatest bottom depth, or vertically-averaging, $T_{100}$, which has a maximum at the warmest temperature and a bottom depth of 30 m, the initial mixed layer thickness. (b) A scatter diagram of the data at left. The big blue dots are from the deep ocean, and the fan of red points are from the continental shelf (the spacing of these points is arbitrary). Notice that for this temperature profile (constant vertical gradient) OHC and $T_{100}$ are exactly similar for warm temperatures over the deep ocean (cf. Fig. 7b and d where this is not the case). OHC and $T_{100}$ are decidedly not similar over the continental shelf.

(Walker, 2005; see also the SST imagery of the Supplementary Material), the thermocline will be lifted toward the coast ($\frac{\partial T}{\partial x} \geq 0$ for the configuration of Fig. 8a) so that cool water may be present very close to shore and very close to the sea surface. Over such an upwelling positive shelf region there may be greater SST cooling than over the outlying, deep ocean, i.e., the reverse of the CWL phenomenon. On some shelves, e.g., the Middle Atlantic Bight, the early summer thermocline may be thin enough, O(30 m) (Schofield et al., 2008) that the width of the coastal warm layer may be no more than a few kilometers, and negligible. Given the great range and temporal variability of coastal ocean hydrography, a key requirement for forecasting hurricane-ocean interaction over shelf regions will be to observe and to model the ocean stratification in more or less real time.

The present treatment of the coastal ocean response to a hurricane (Sect. 3.2.2) was simplified to the point that $T_d$ could be characterized as a null model: the estimated (deep ocean) vertical mixing was simply stopped if it reached the ocean bottom. That must happen, of course, but so may a great deal else that was outside the scope of this greatly simplified treatment. For example, rotary inertial motions, the dominate mode of open ocean, wind-driven currents, must be inhibited near coast lines. At a minimum, there must occur transient up- and down-welling that was not accounted for in the local version of $T_d$ presented here. Surface gravity waves generated by an approaching hurricane can be very energetic, and may cause intense vertical mixing within a thick bottom boundary layer, even before the direct effect of the hurricane wind stress reaches the bottom (Glenn et al., 2008). Finally, the pre-hurricane thermal and salinity fields around continental shelves will often vary in three dimensions, with marked effects on the post-hurricane SST and salinity observed at fixed sites (Xie et al., 1997; Chu et al., 2000 and Bingham, 2007). When the possibilities of variable hurricane incidence angle and translation speeds are considered in combination with one or more of the coastal phenomenon noted above, then it becomes evident that the parameter space for hurricane-coastal ocean interaction is very extensive and well worth additional study and synthesis (Manzello et al., 2007). We certainly need to understand which map – OHC in Fig. 3 or $T_{100}$ in Fig. 4 – gives the better forecast guidance over continental shelves, and over cool, open ocean regions.
A Matlab script that evaluates an arbitrary density profile for the depth of mixing and the depth-averaged temperature, \( T_d \).

2. A description of a comparison of \( T_d \) with solutions of the 3D-PWP numerical ocean model.

3. A collection of GOES SST imagery of the Gulf of Mexico during the summer of 2005.


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4.3 A look ahead

Forecasting of hurricanes or any natural phenomenon is a pragmatic endeavor. Insight from models and observations can help point the way to new hypotheses or methods, but forecasting success can only be told from actual practice (Lin et al., 2008; Mainelli et al., 2008) which was beyond the scope of this paper. The best result of this discussion would be to stimulate a fresh look at hurricane-ocean interaction, and specifically, to encourage further testing of ocean metrics drawn from an expanded hypothesis-space. Just two examples:

A revised OHC. The conservation error of OHC (footnote 1 of Sect. 1) and the cool degeneracy noted in Sect. 3.1.2 could be remedied for most hurricane analysis or forecasting purposes simply by choosing a reference temperature that is below the depth of vertical mixing and the lower limit of relevant SSTs, e.g., \( 22^\circ \text{C} \). This variant of OHC will have improved conservation and statistical properties over a wider range of conditions than does the usual form, Eq. (3), but there is still no guarantee that heat content will be the most relevant physical quantity for hurricane-ocean interaction over shallow continental shelves (Sect. 3.2) and especially those that are to some degree salt-stratified (Sect. 3.3).

A derivative of \( T_d \). The depth-averaged temperatures estimated here were intended to be the minimum of SST expected in a hurricane wake, i.e., displaced behind the strongest winds of a moving hurricane. The SST cooling directly under a hurricane can be considerably less than the maximum cooling seen in the wake (Cione and Uhlhorn, 2003; D’Asaro et al., 2007, and see also Wu et al., 2005), and it seems likely that hurricane-ocean interaction would be better represented by, e.g., a weighted average of the observed, initial SST and \( T_i(z=0) \) (a simple average is in Fig. 10).

In a similar way, if the issue on a given day was the possible intensification of a moderate tropical storm, then a much reduced wind stress amplitude in the mixing depth model (Eq. 5), \( \tau = 1 \text{ Pa} \), would be appropriate. Treatment of very slowly moving or quasi-stationary storms would benefit from an explicit treatment of upwelling (see the remarks in the Supplementary Material) and, in shallow water, heat loss to the hurricane.

Identifying the optimum ocean metric is an important and significant challenge; OHC and depth-averaged temperatures are well-correlated in some important circumstances and, in any event, the ocean thermal field is just one of several factors that make up the complex environment of a hurricane. A thorough exploration and sensitive test of ocean metrics will require a large suite of case studies that span the full range of ocean conditions that are relevant for hurricane-ocean interaction. No doubt such a study could be aided considerably by guidance from the best possible air and sea coupled models that include a coastal ocean.

**Supplementary Material**

Supplementary material includes:

1. A Matlab script that evaluates an arbitrary density profile for the depth of mixing and the depth-averaged temperature, \( T_d \).
2. A description of a comparison of \( T_d \) with solutions of the 3D-PWP numerical ocean model.
3. A collection of GOES SST imagery of the Gulf of Mexico during the summer of 2005.

**Fig. 10.** The simple average of \( T_{100} \) and the initial SST for the data of Fig. 9a. This temperature is thought to be a better estimator of the SST under the high wind speed, central region of a hurricane than is \( T_{100} \), and in that regard may be the most relevant SST insofar as hurricane-ocean interaction is concerned. It is, of course, also much harder to observe. Notice that this temperature is slightly greater than \( T_{100} \) over the deep ocean, \( z > -b \) (cf. Fig 9a) and nearly equal to \( T_i \) over the mid-continental shelf.

\[
\frac{\left[T_{100} + T_i(z=0)\right]}{2}, ^\circ \text{C}
\]

\[
T(z=0), ^\circ \text{C}
\]

\[
\text{bottom depth, } b, \text{ m}
\]
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